

Hierarchical Computation and Communication for Distributed Sparse Operations on Supercomputers with Multi-GPU Nodes

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Preliminary Exam Committee:

Wen-mei Hwu (Chair)

Weng Cho Chew

Michale Oelze

Andreas Kloeckner

Bill Gropp

Large-Scale Sparse Applications

Conference

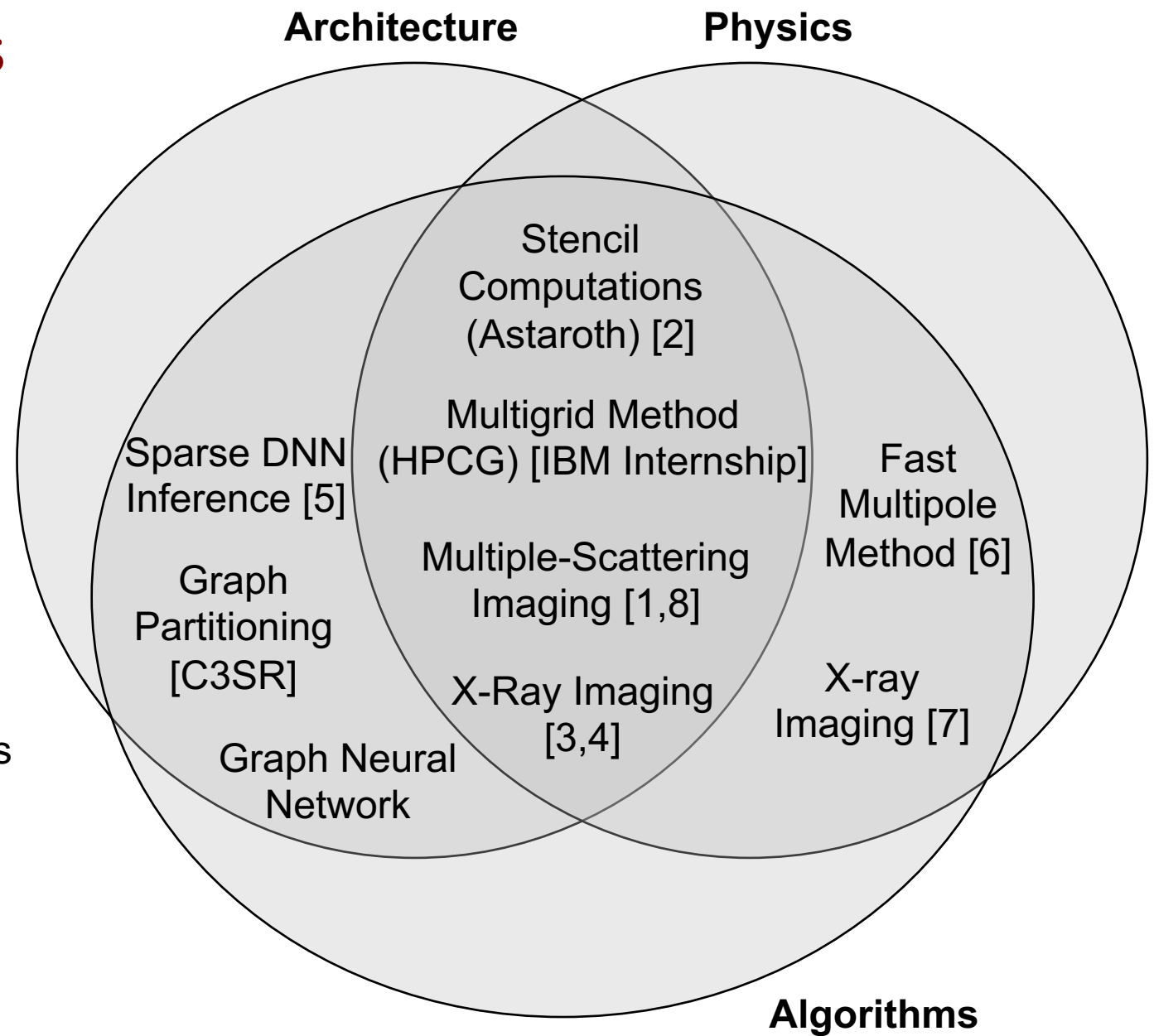
- [1] IPDPS'18 (Outstanding Presentation)
- [2] HPCC'19 (Best Paper)
- [3] SC'19 (SCC Benchmark)
- [4] SC'20 (Best Paper)
- [5] HPEC'20 (Graph Challenge Champion)

Journal

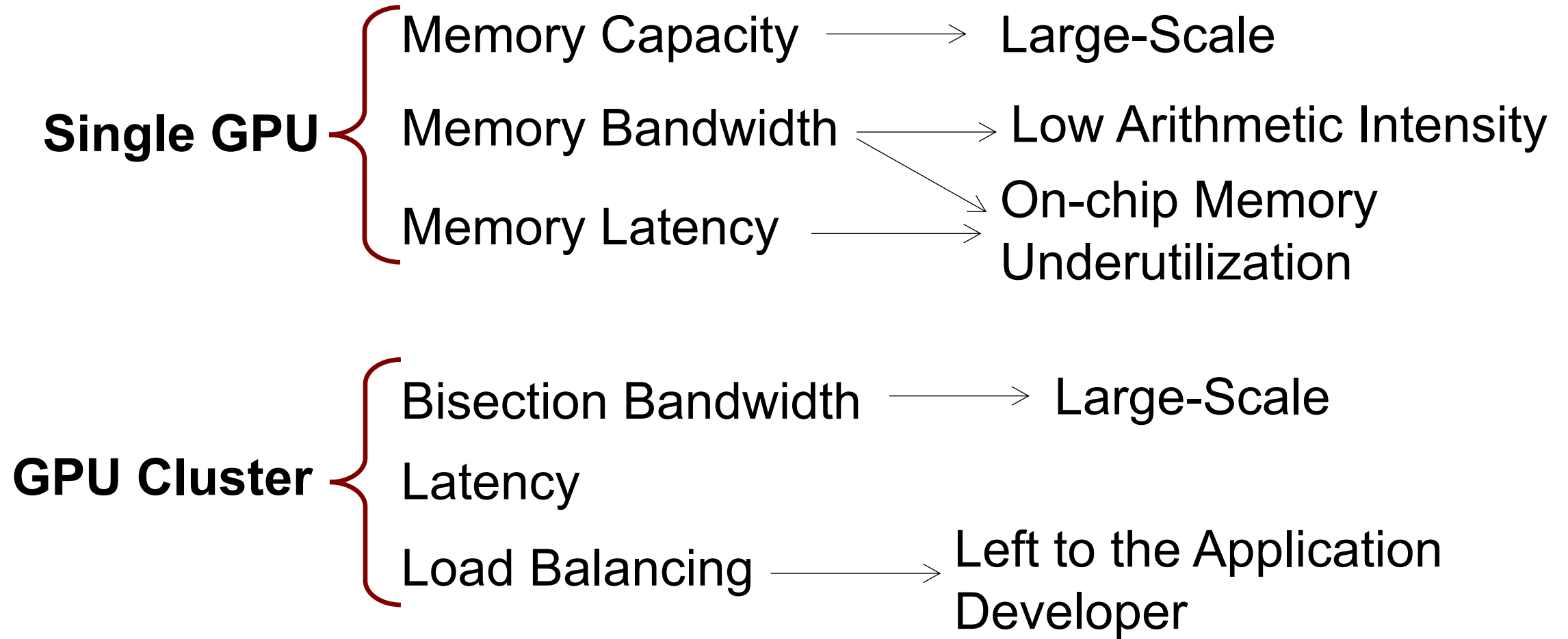
- [6] IEEE TAP (2018)
- [7] OSA Applied Optics (2018)

Book Chapter

- [8] New Trends in Computational Electromagnetics



Performance Bottlenecks



Performance Bottlenecks

Single GPU

Summit (2018) 6 GPUs per Node



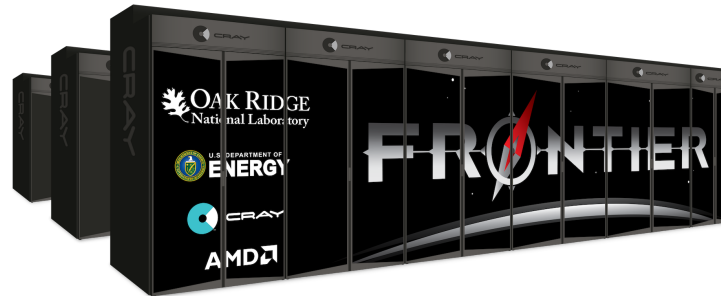
200 PFLOPS 4,608 Nodes

Aurora (2021) 6 GPUs per Node



1 EFLOPS

Frontier (2021) 4 GPUs per Node



1.5 EFLOPS

El Capitan (2024) 4 GPUs per Node



2 EFLOPS

GPU Cluster

Arithmetic Intensity

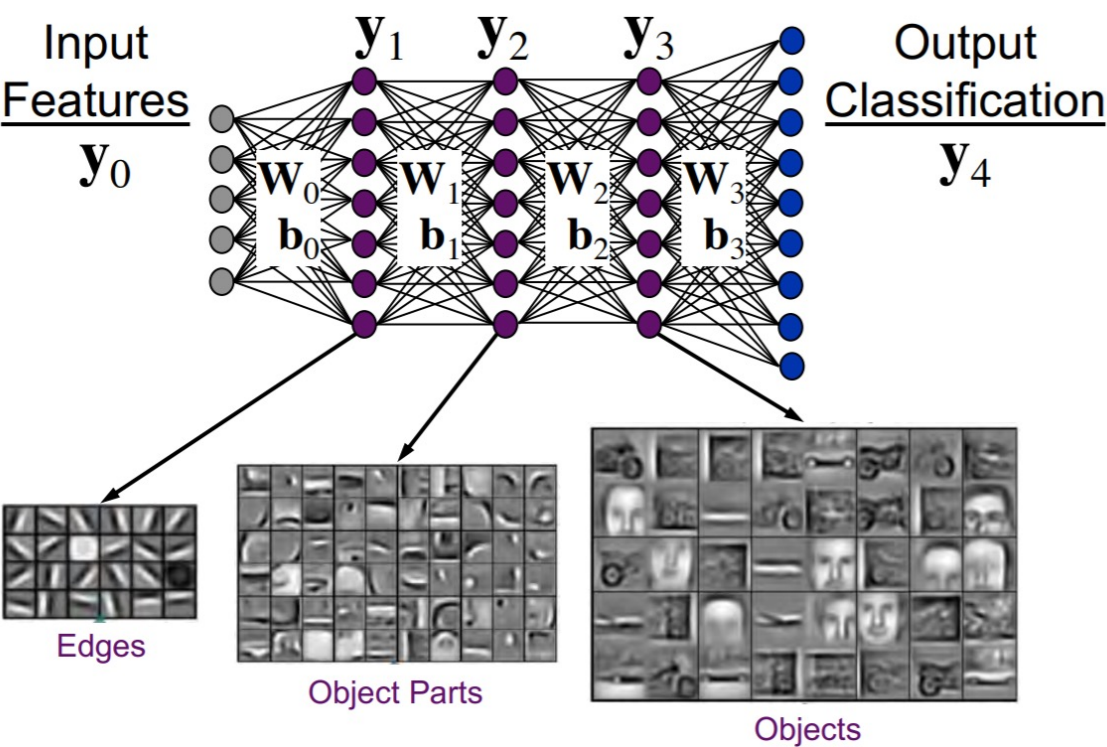
Memory

Accession

Scale

Application

Application: Sparse Deep Neural Network

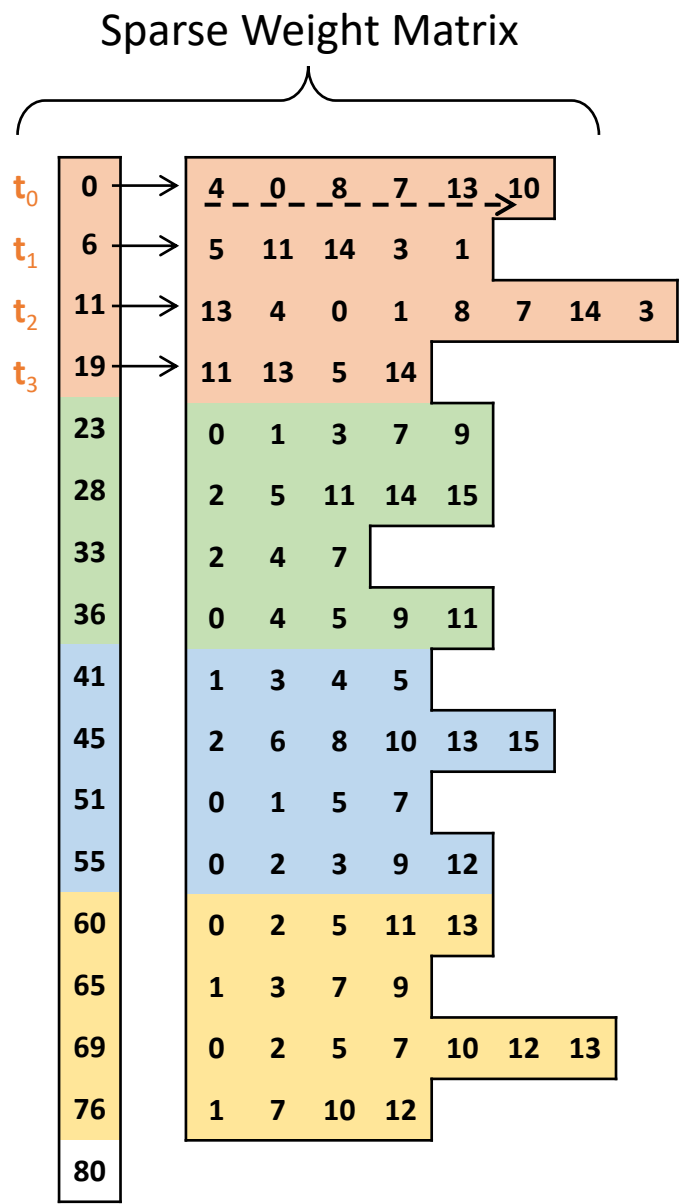
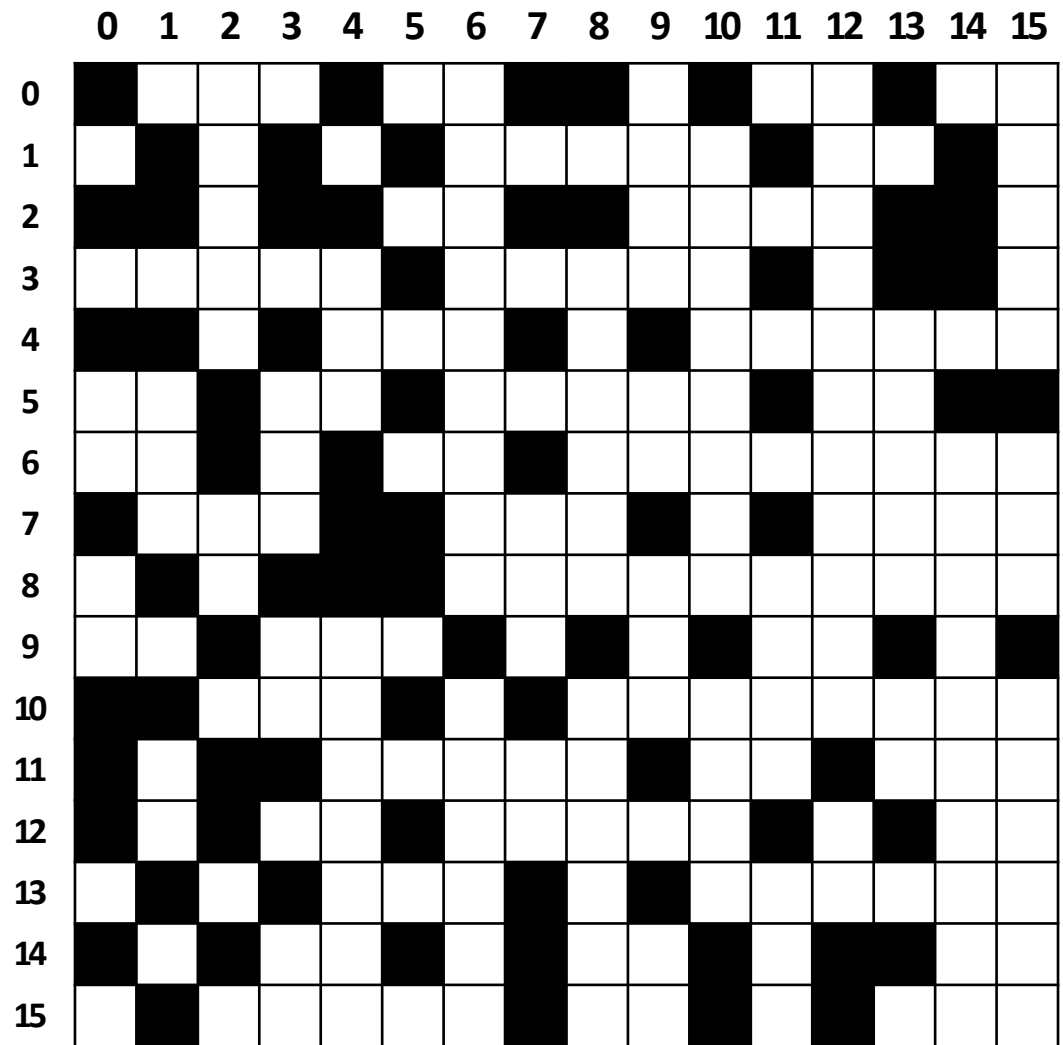


- Input Data (Y0)**
MNIST corpus of 60,000 handwritten numbers.
- 32x32 → **1,024** neurons
 - 64x64 → **4,096** neurons
 - 128x128 → **16,384** neurons
 - 256x256 → **65,536** neurons

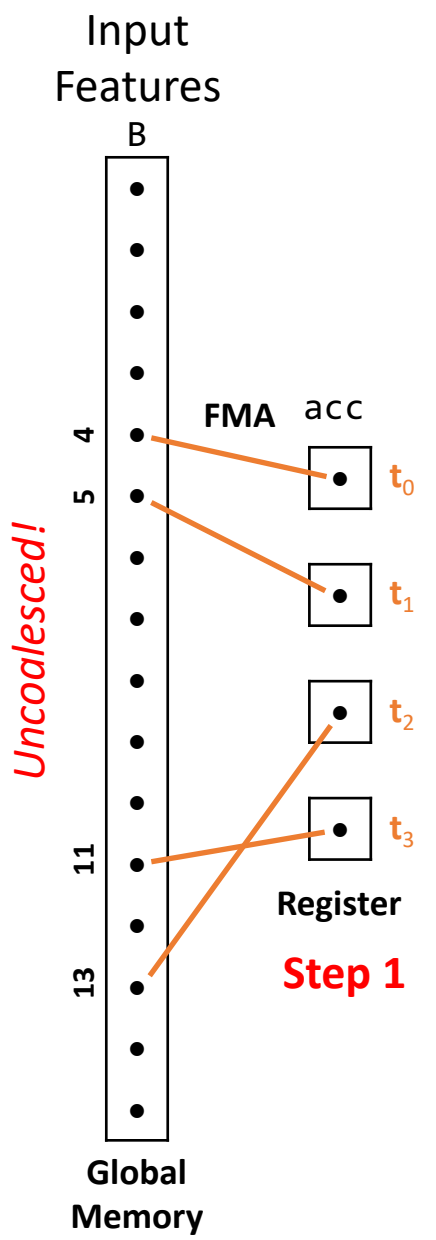
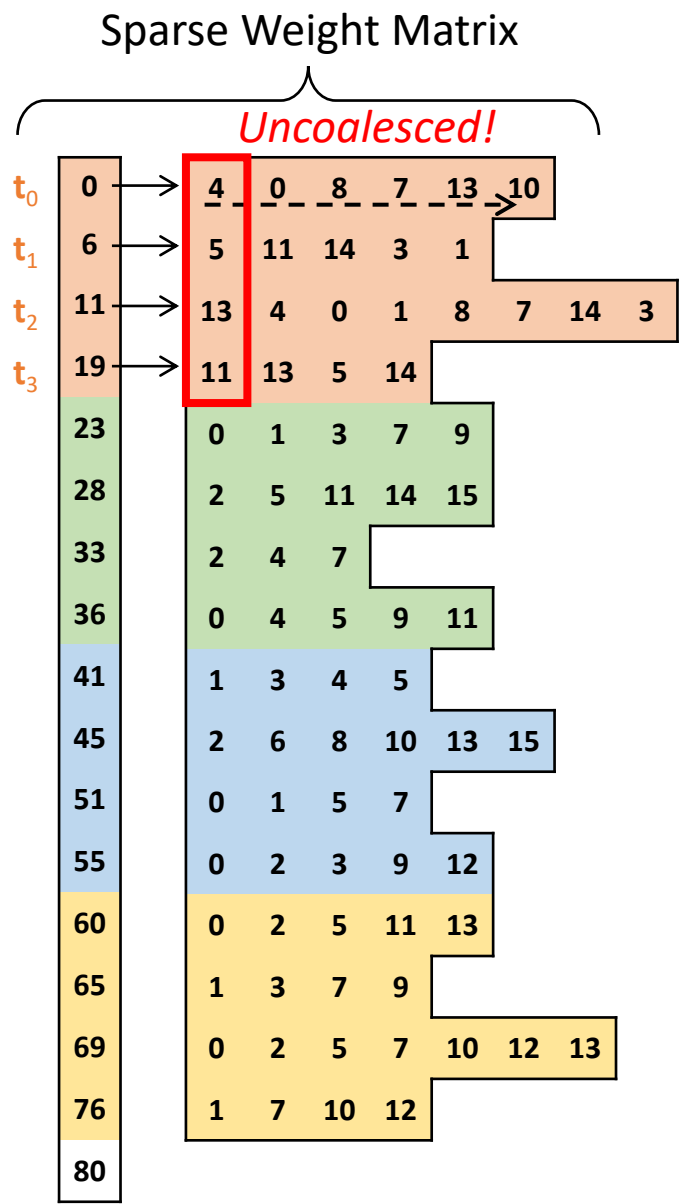
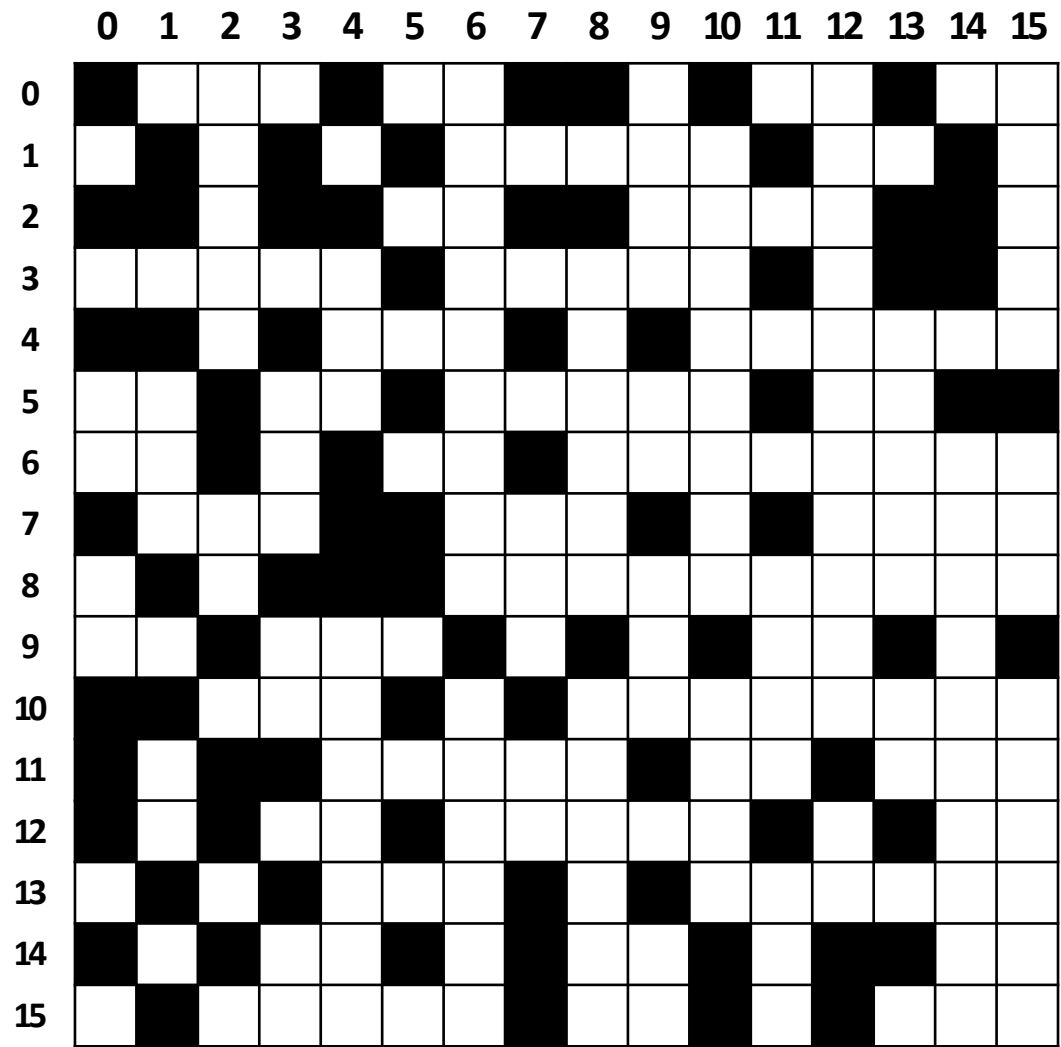
Layers	Neurons/Layer			
	1024	4096	16384	65536
120	3,932,160	15,728,640	62,914,560	251,658,240
480	15,728,640	62,914,560	251,658,240	1,006,632,960
1920	62,914,560	251,658,240	1,006,632,960	4,026,531,840

Total Edges = 32 x layers x neurons/layer

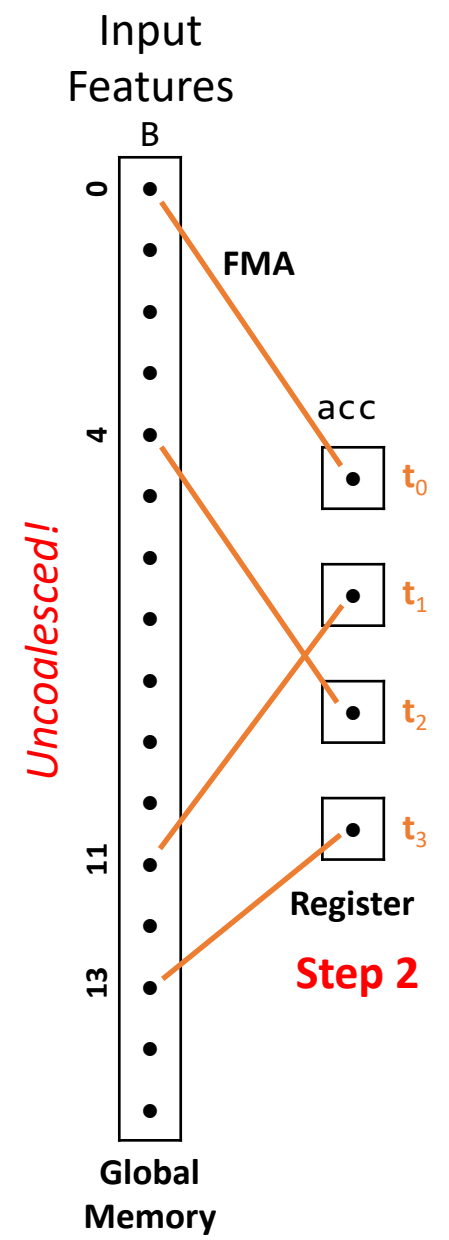
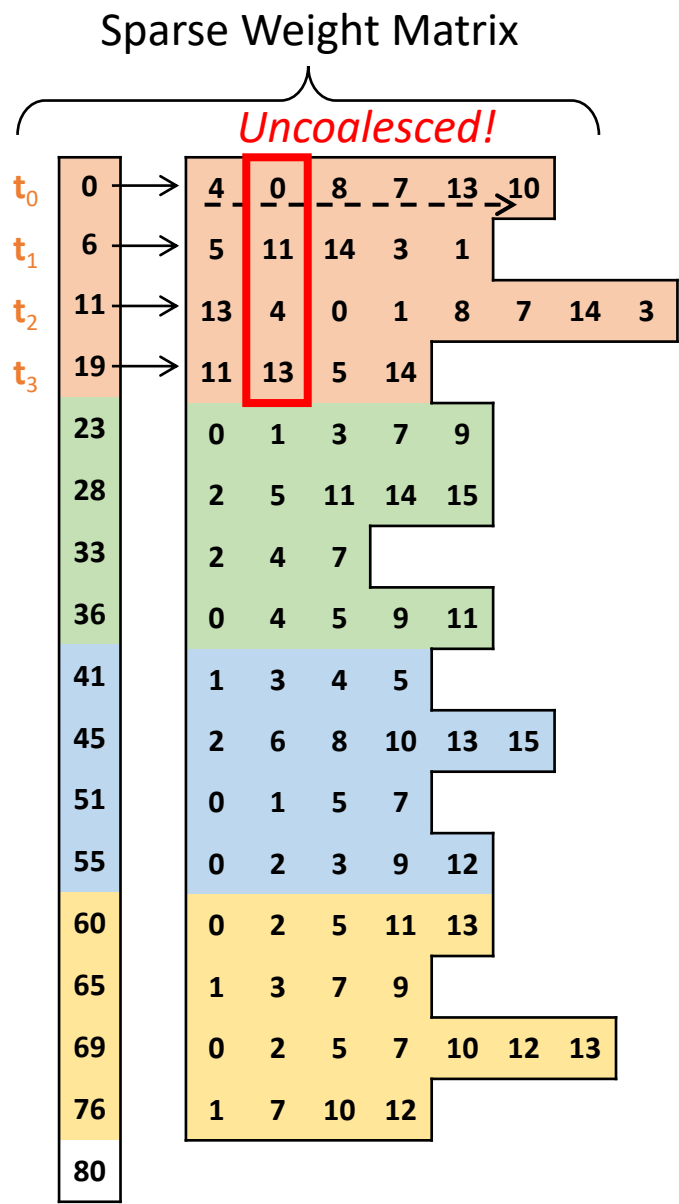
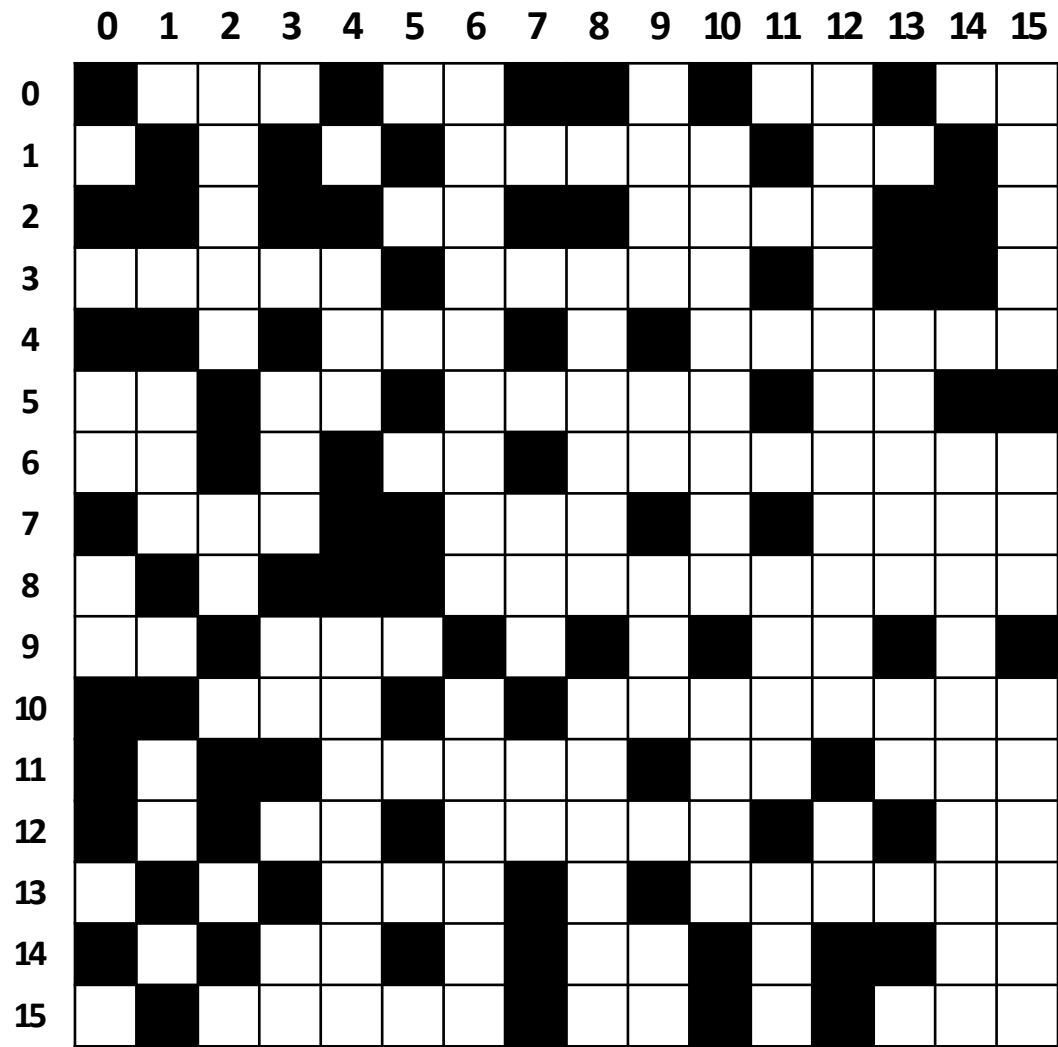
Baseline CSR SpMM



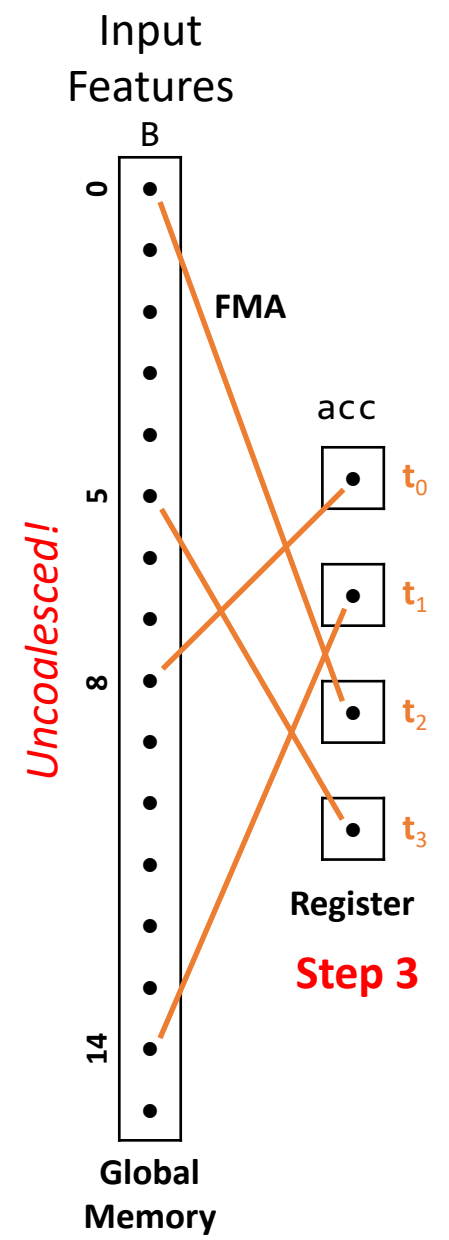
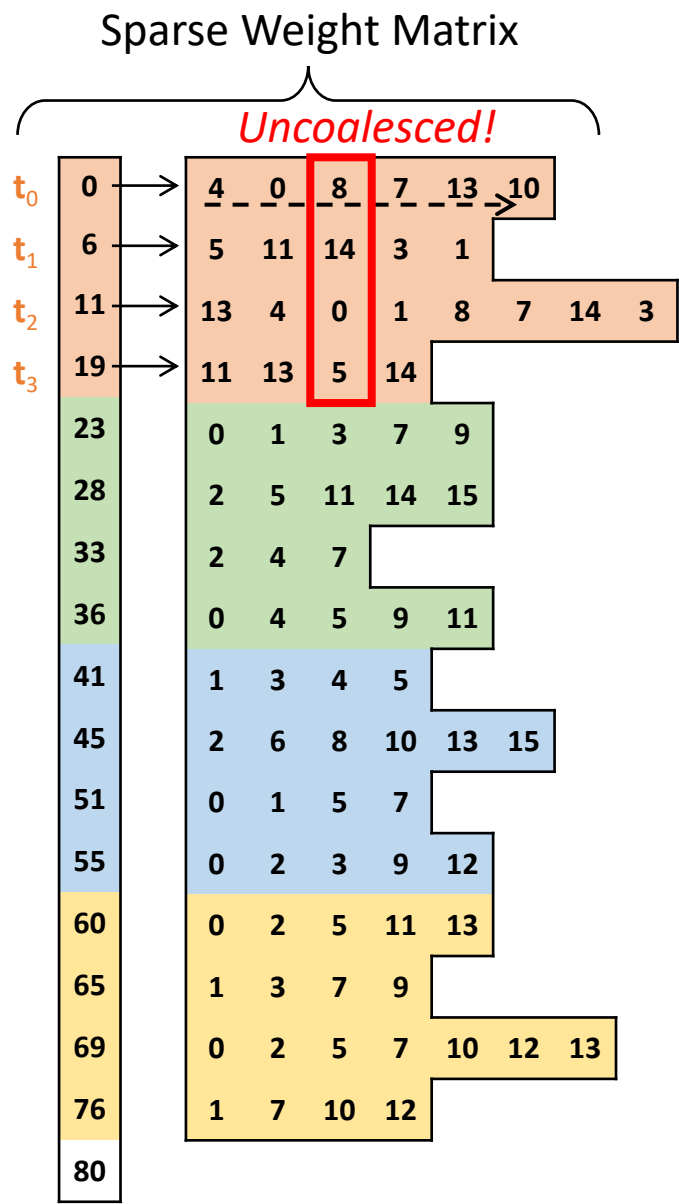
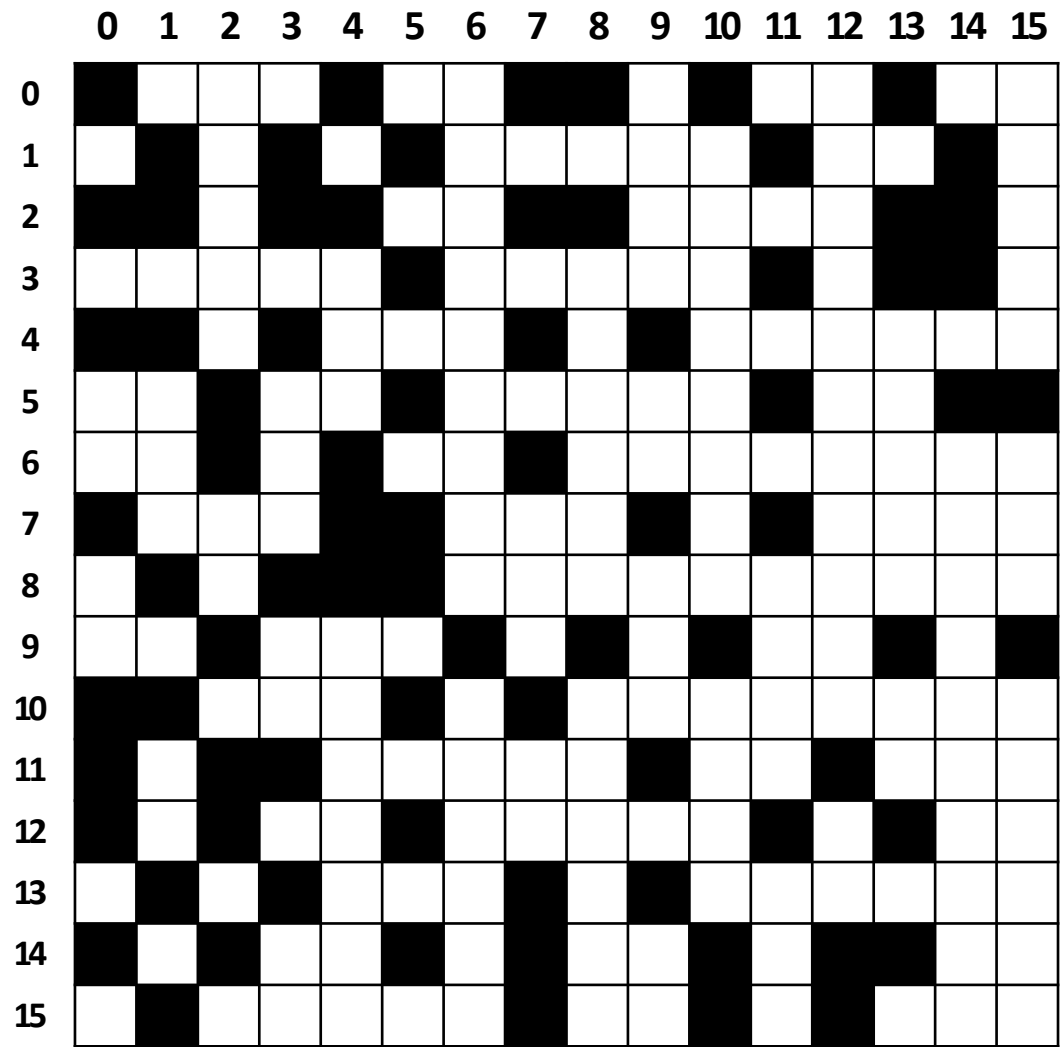
Baseline CSR SpMM



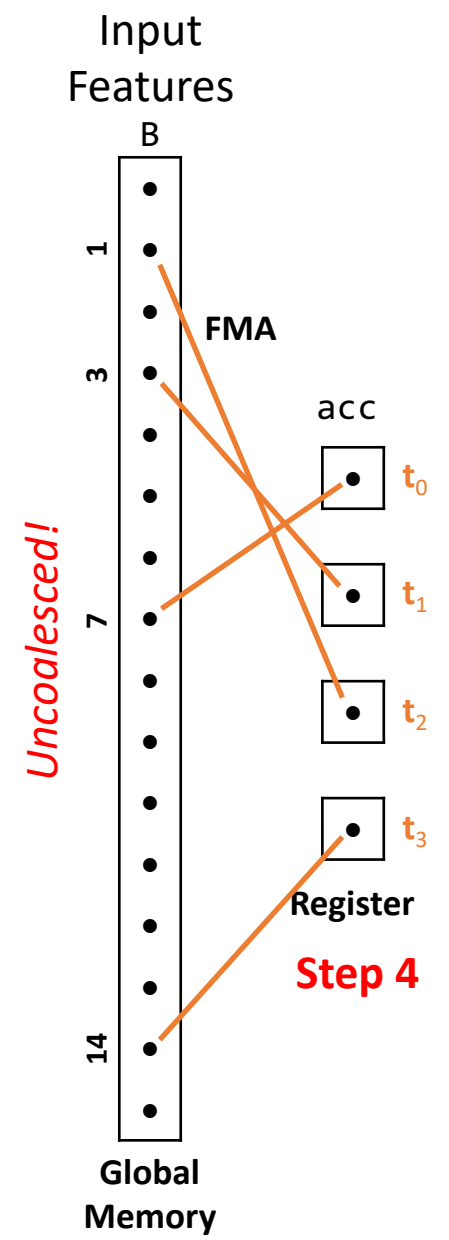
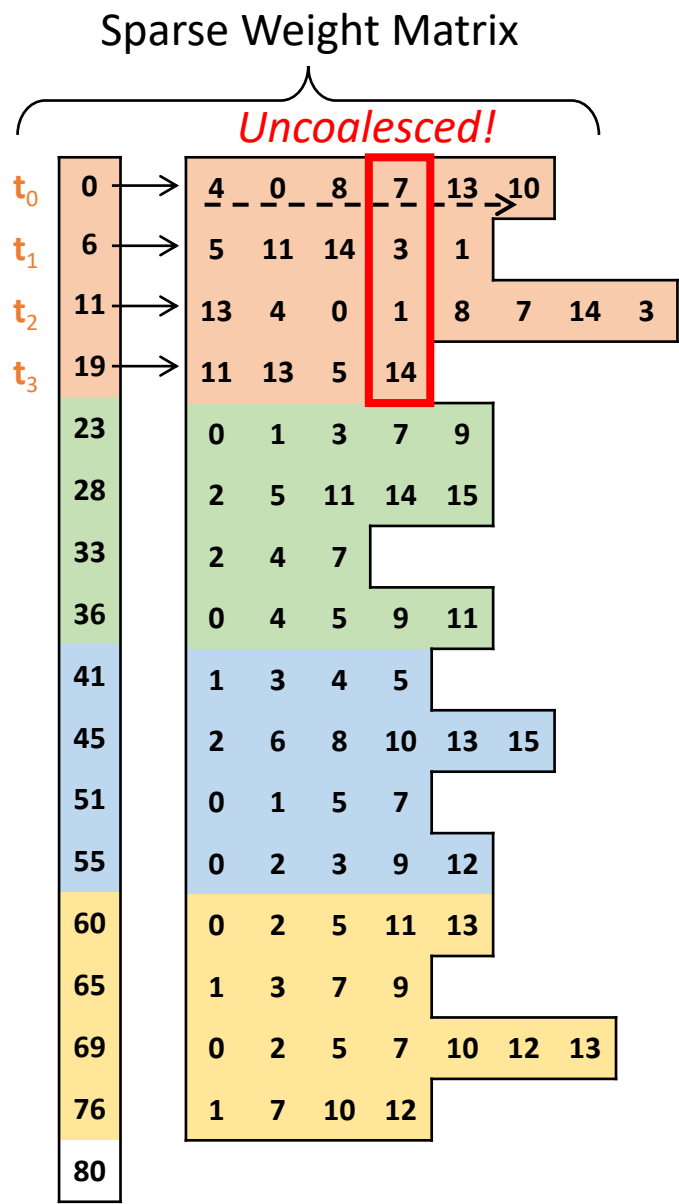
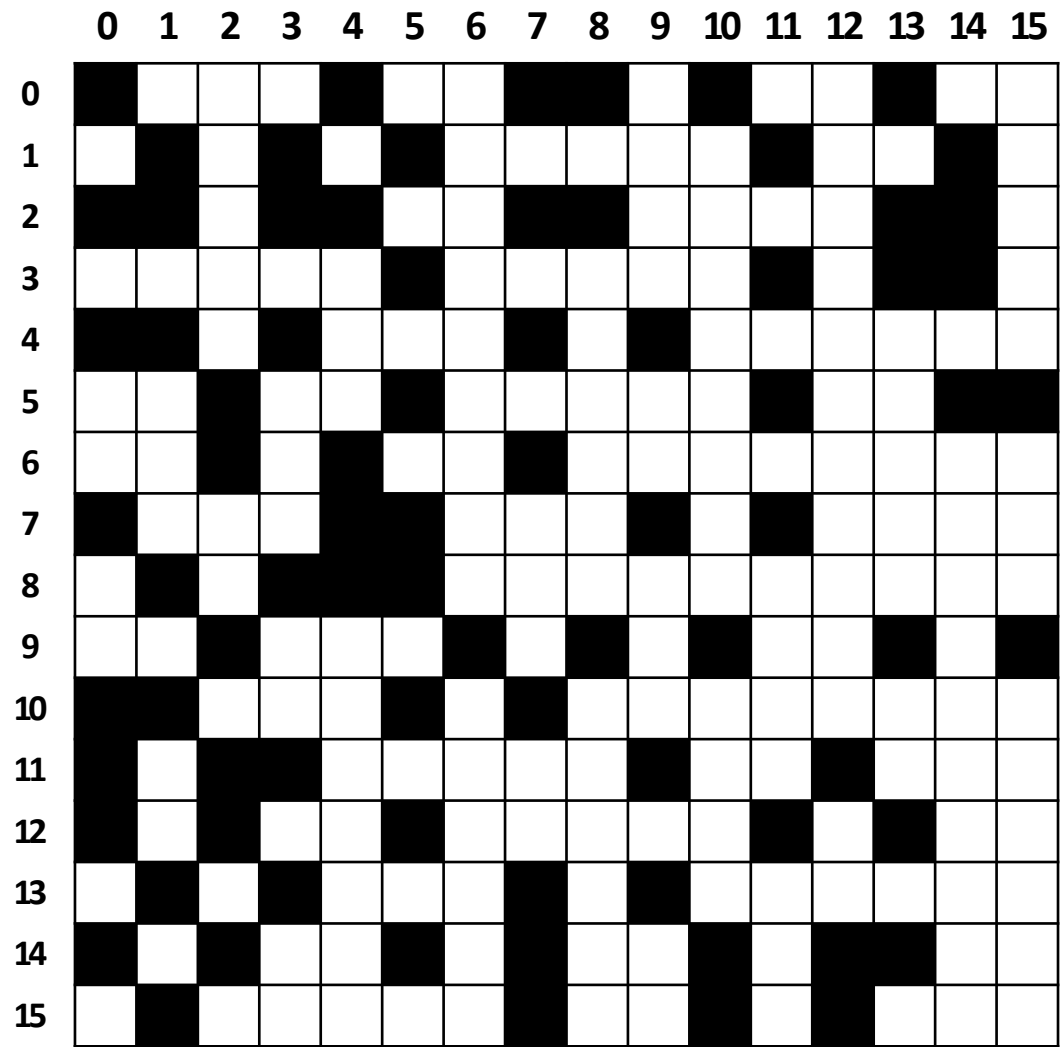
Baseline CSR SpMM



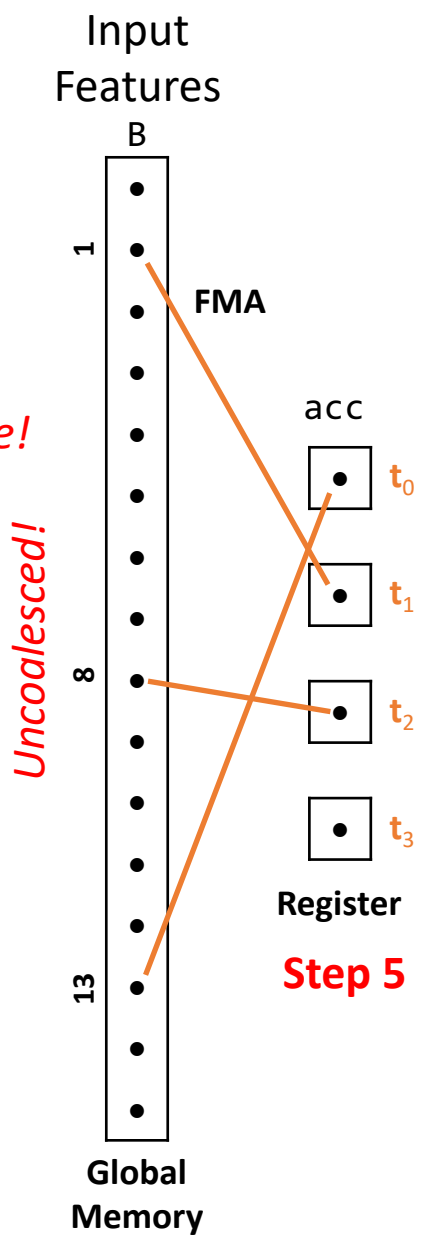
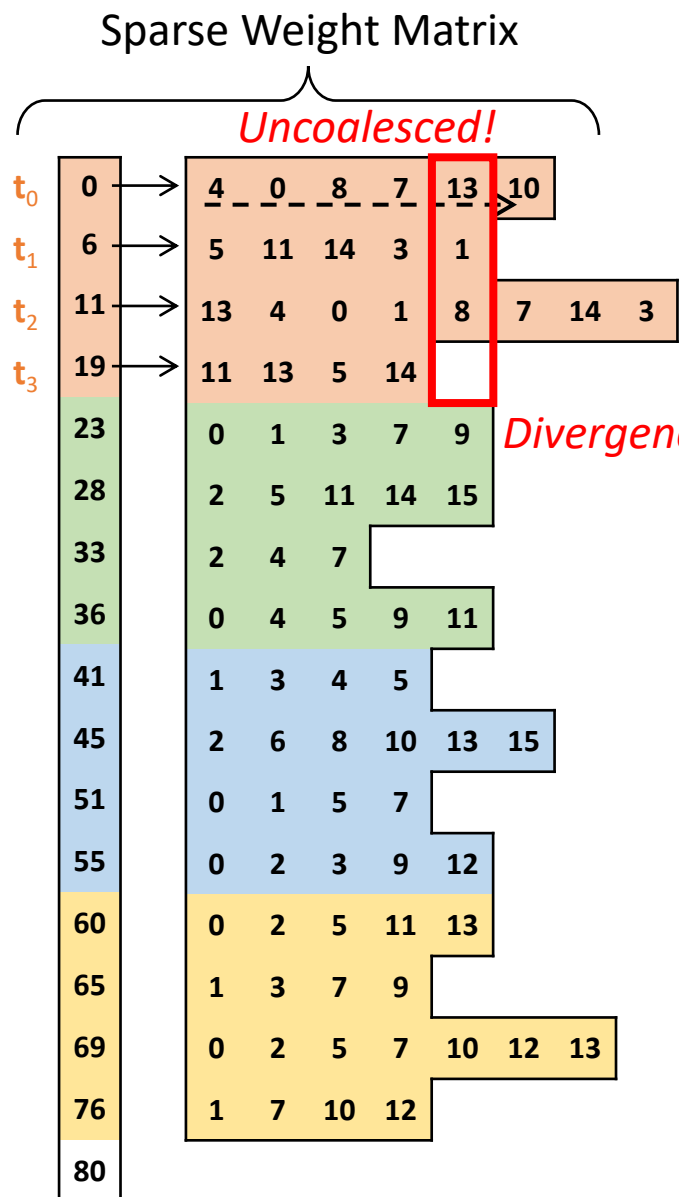
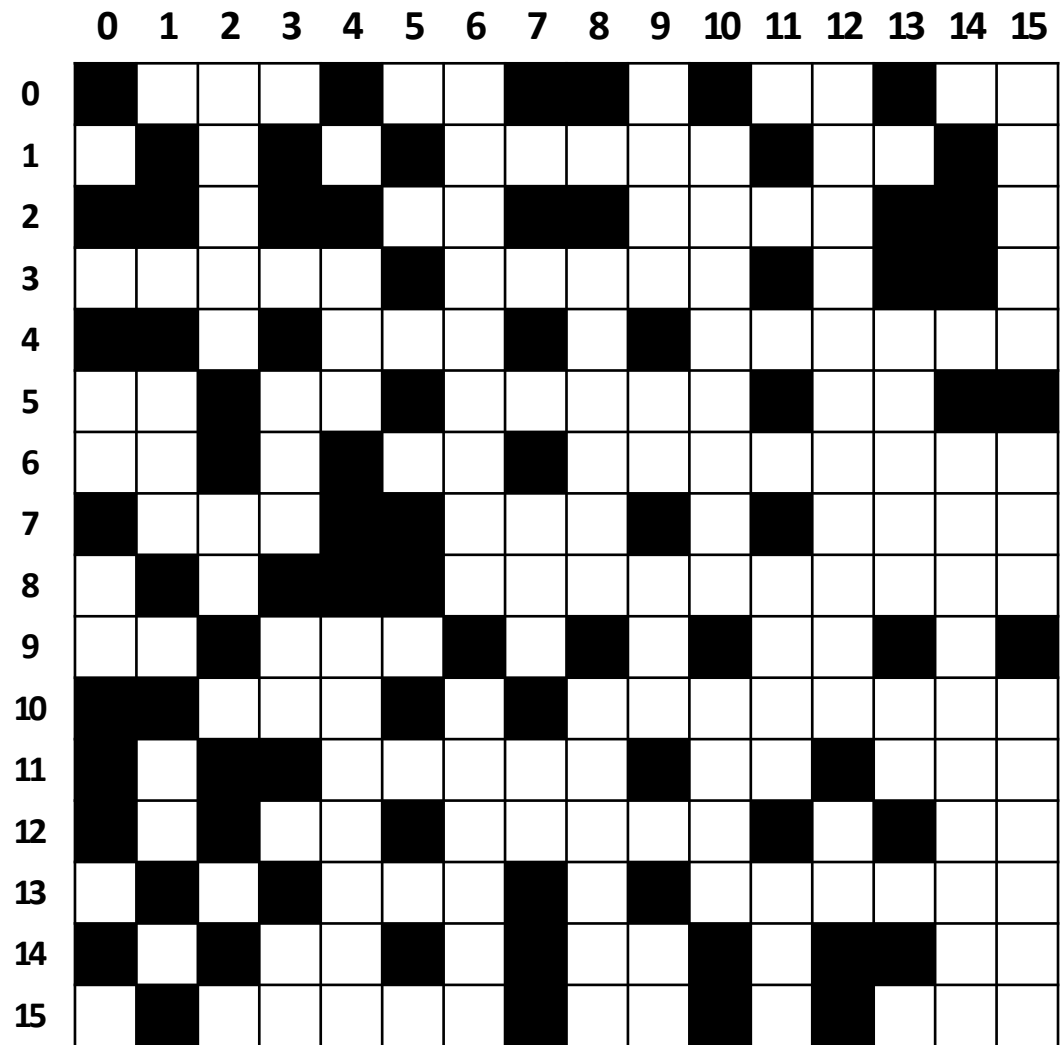
Baseline CSR SpMM



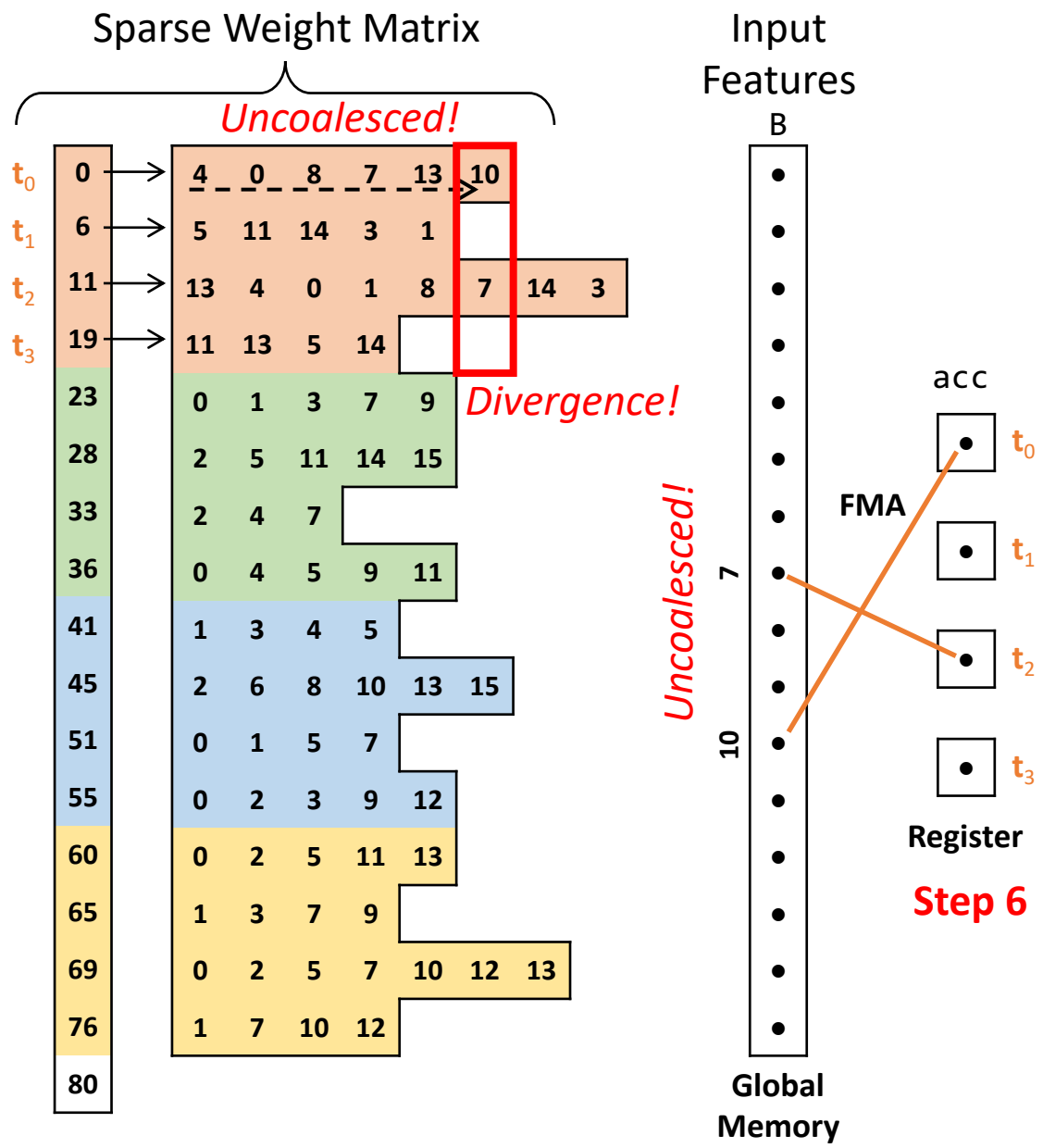
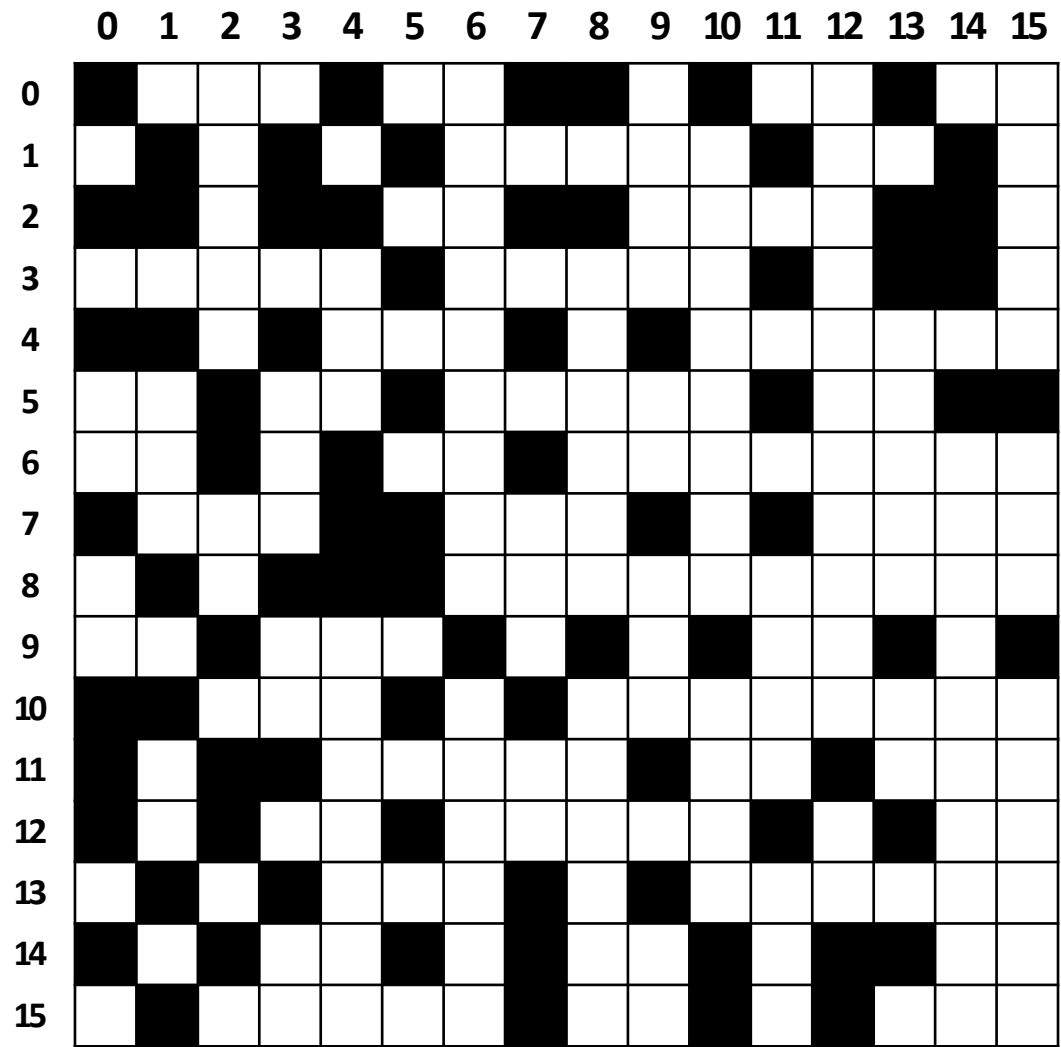
Baseline CSR SpMM



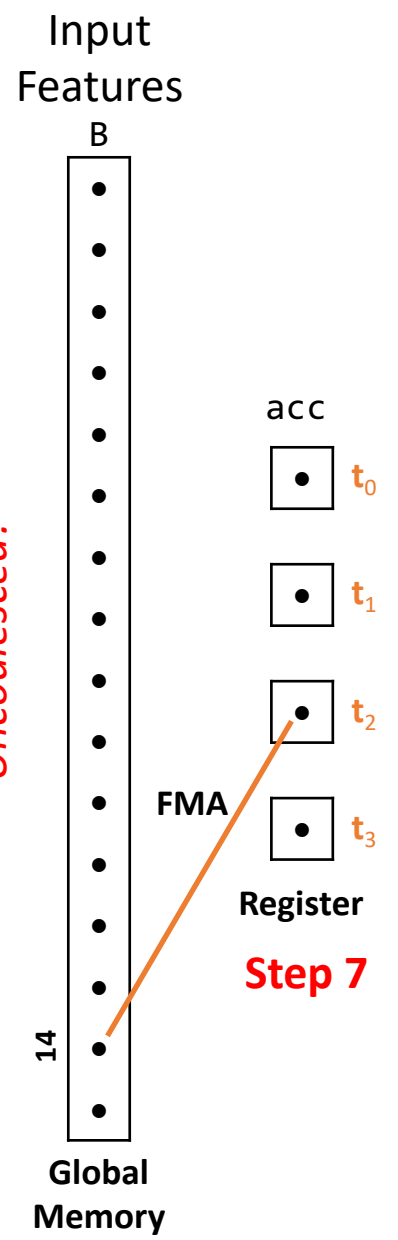
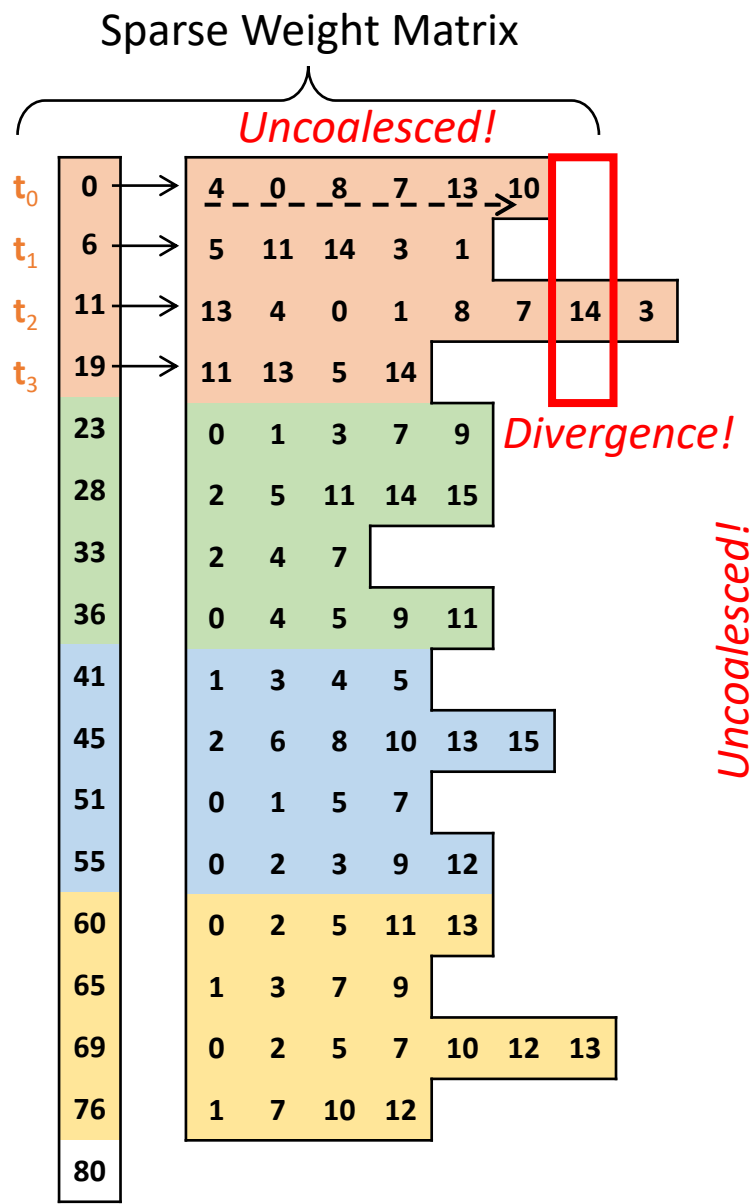
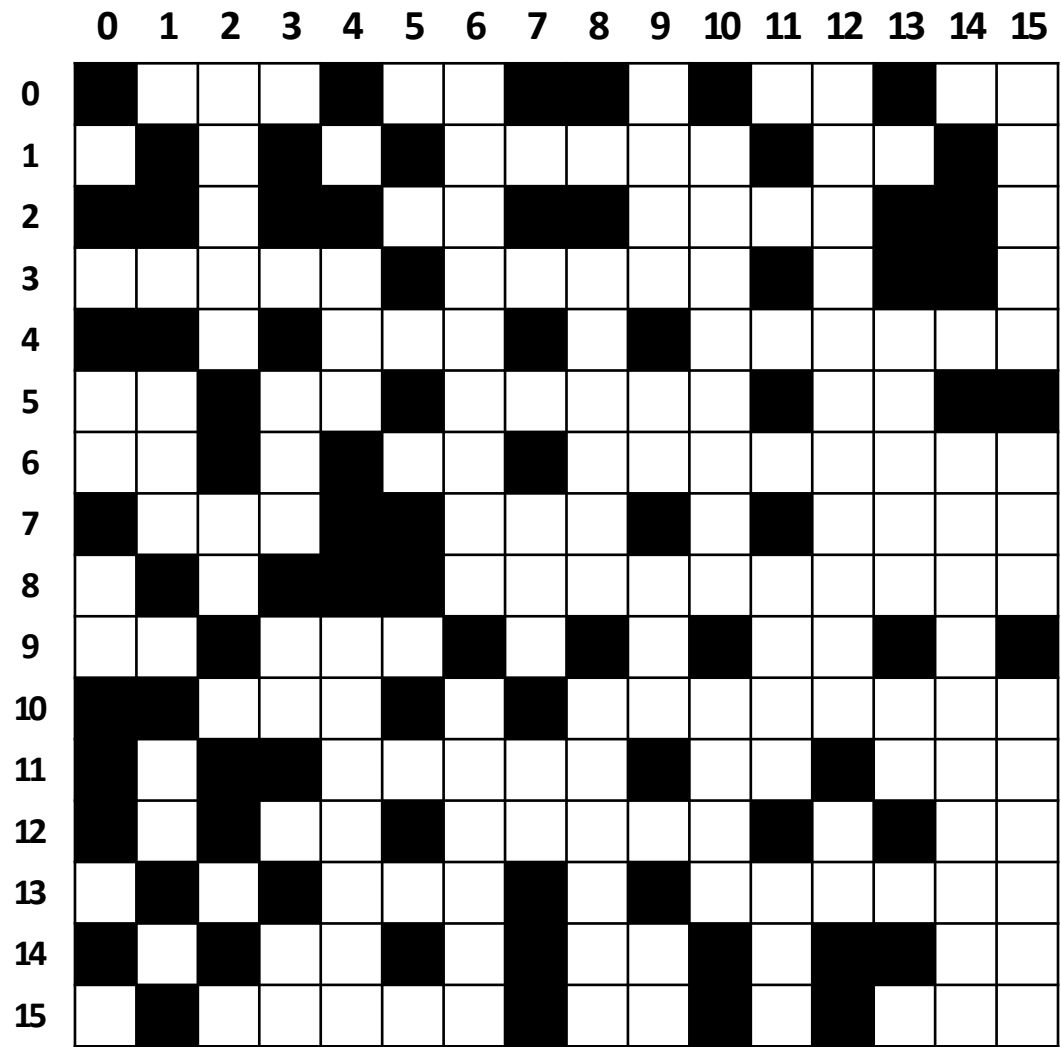
Baseline CSR SpMM



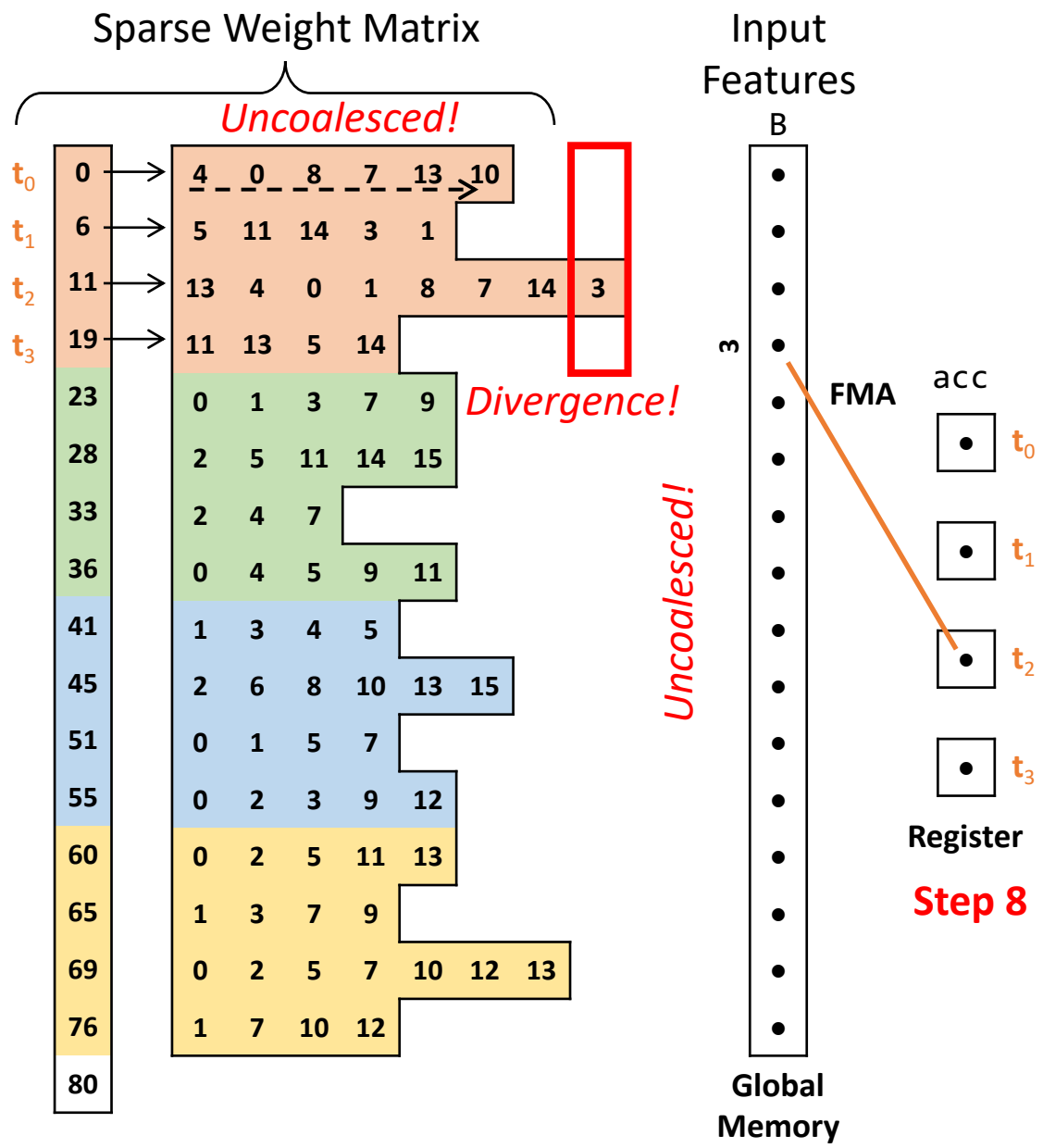
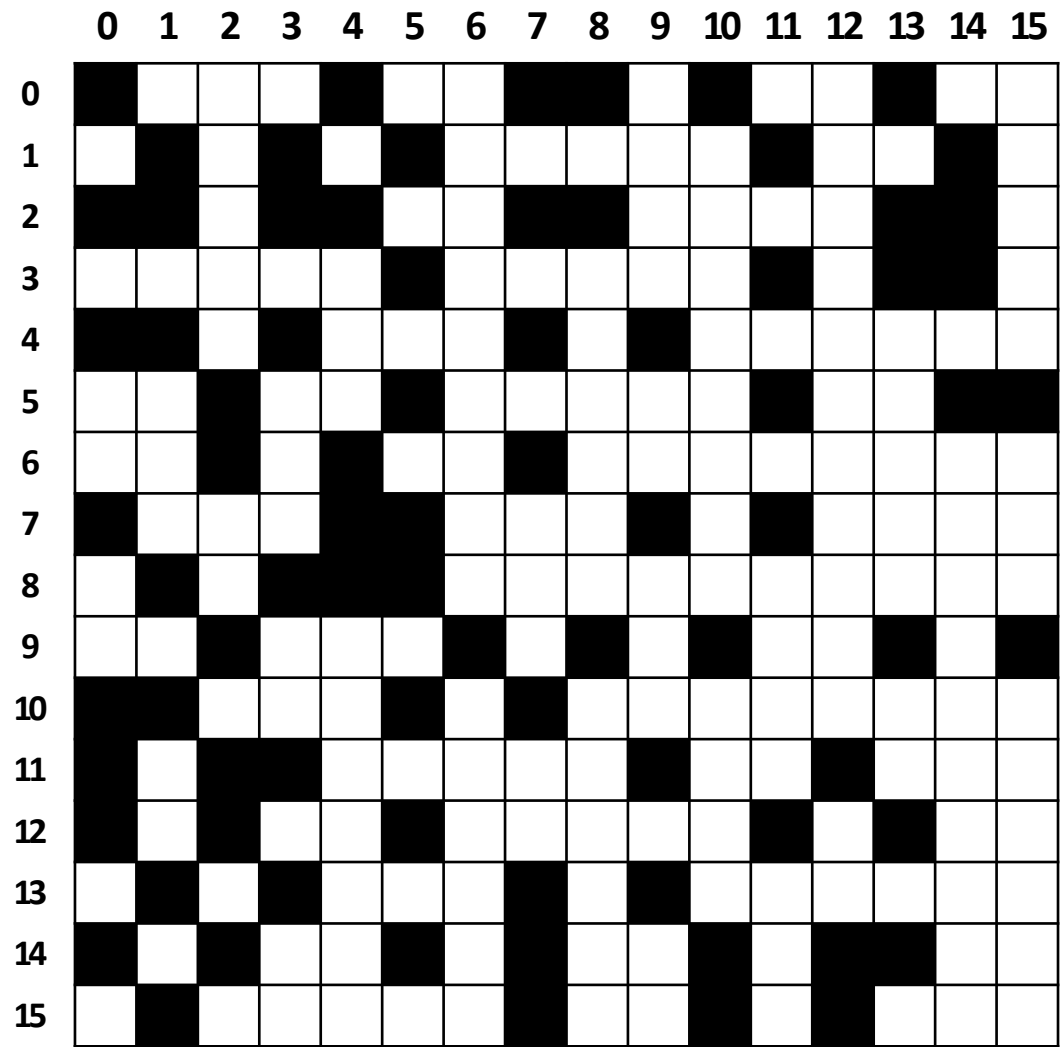
Baseline CSR SpMM



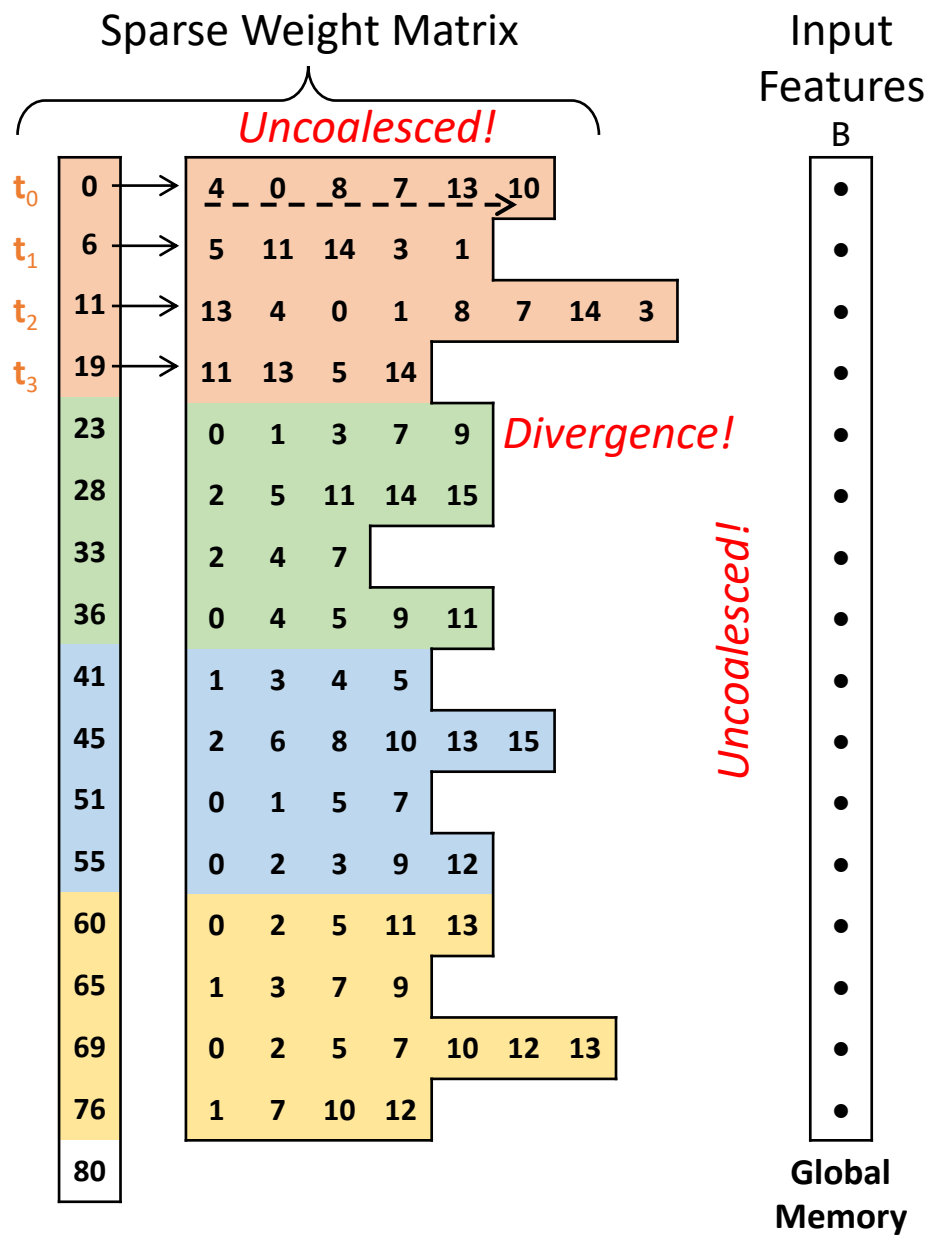
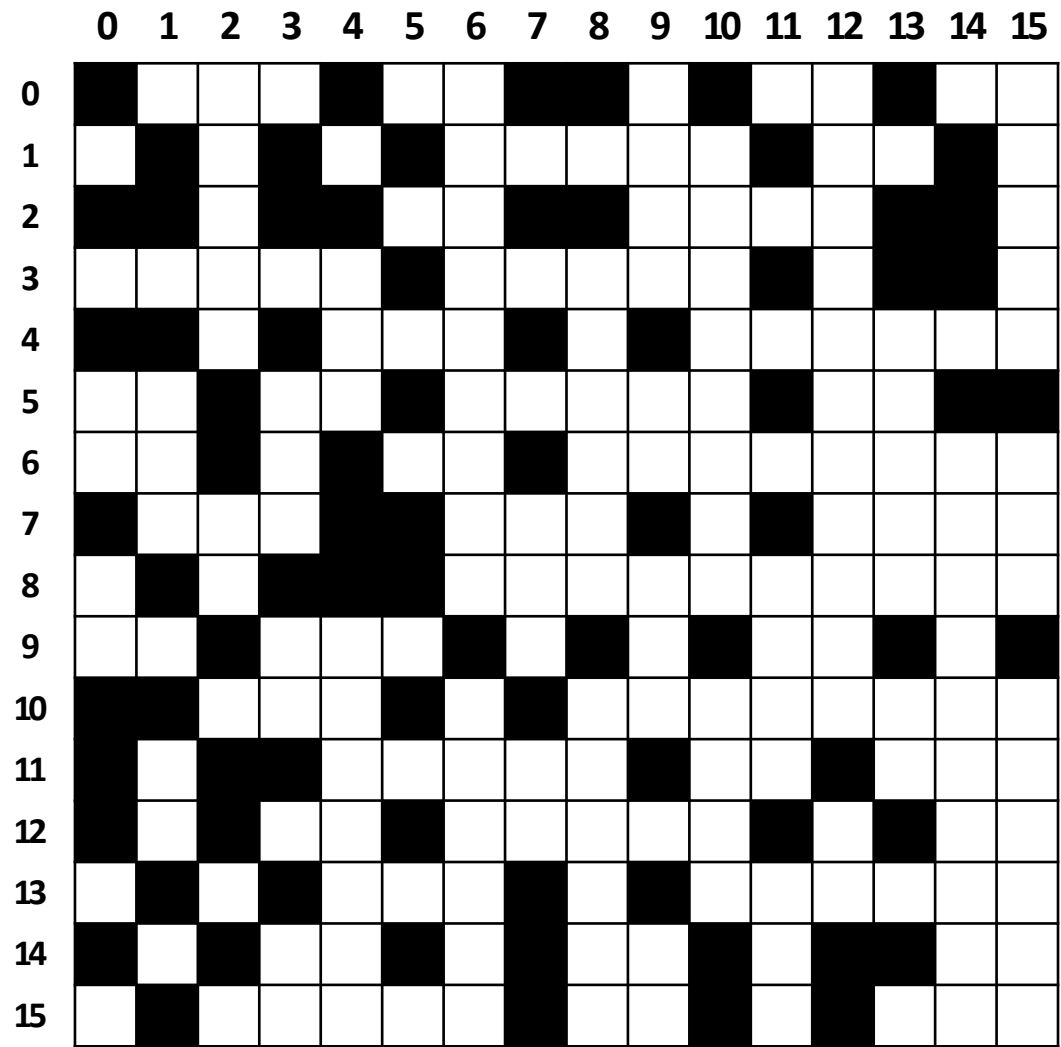
Baseline CSR SpMM



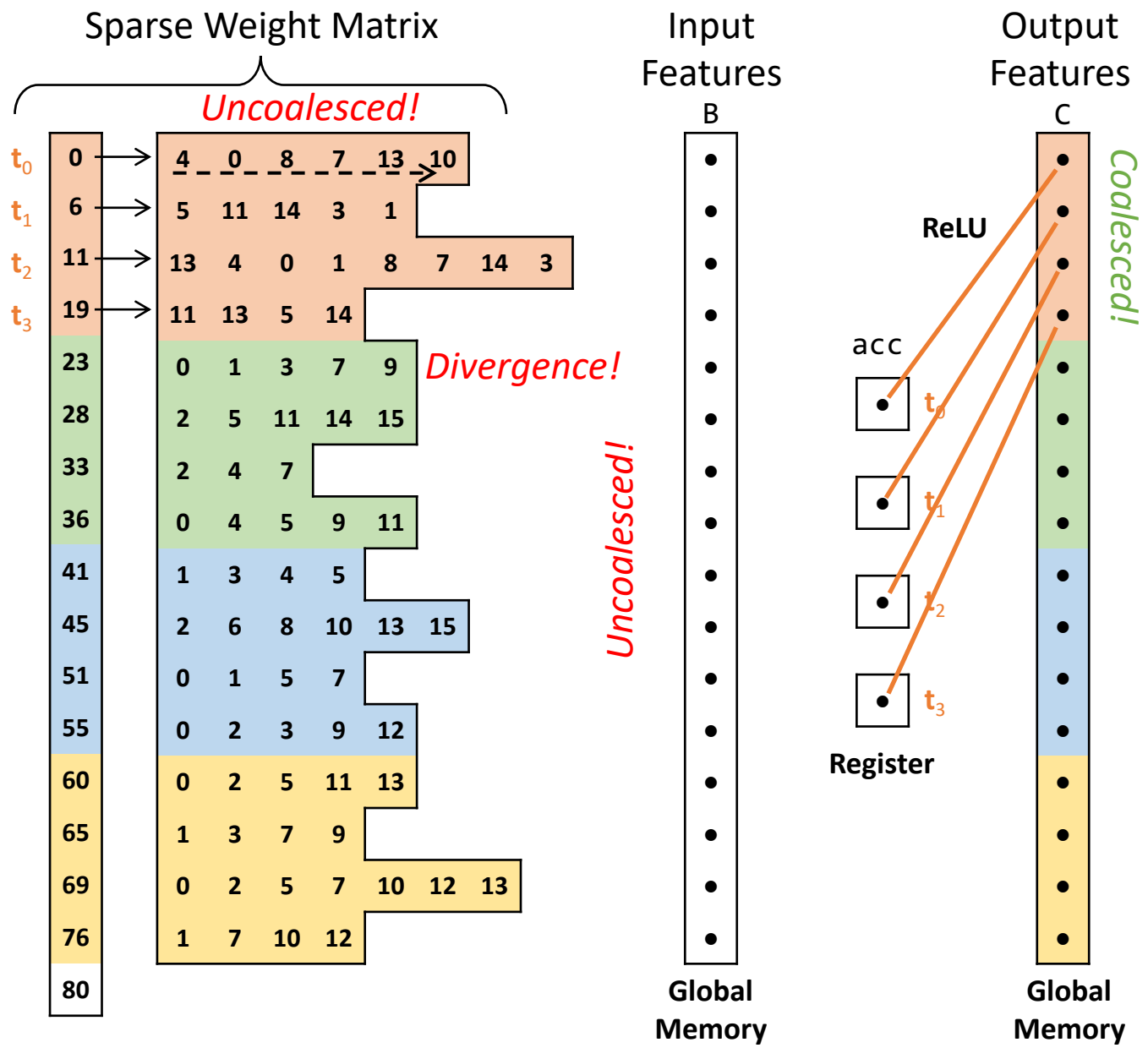
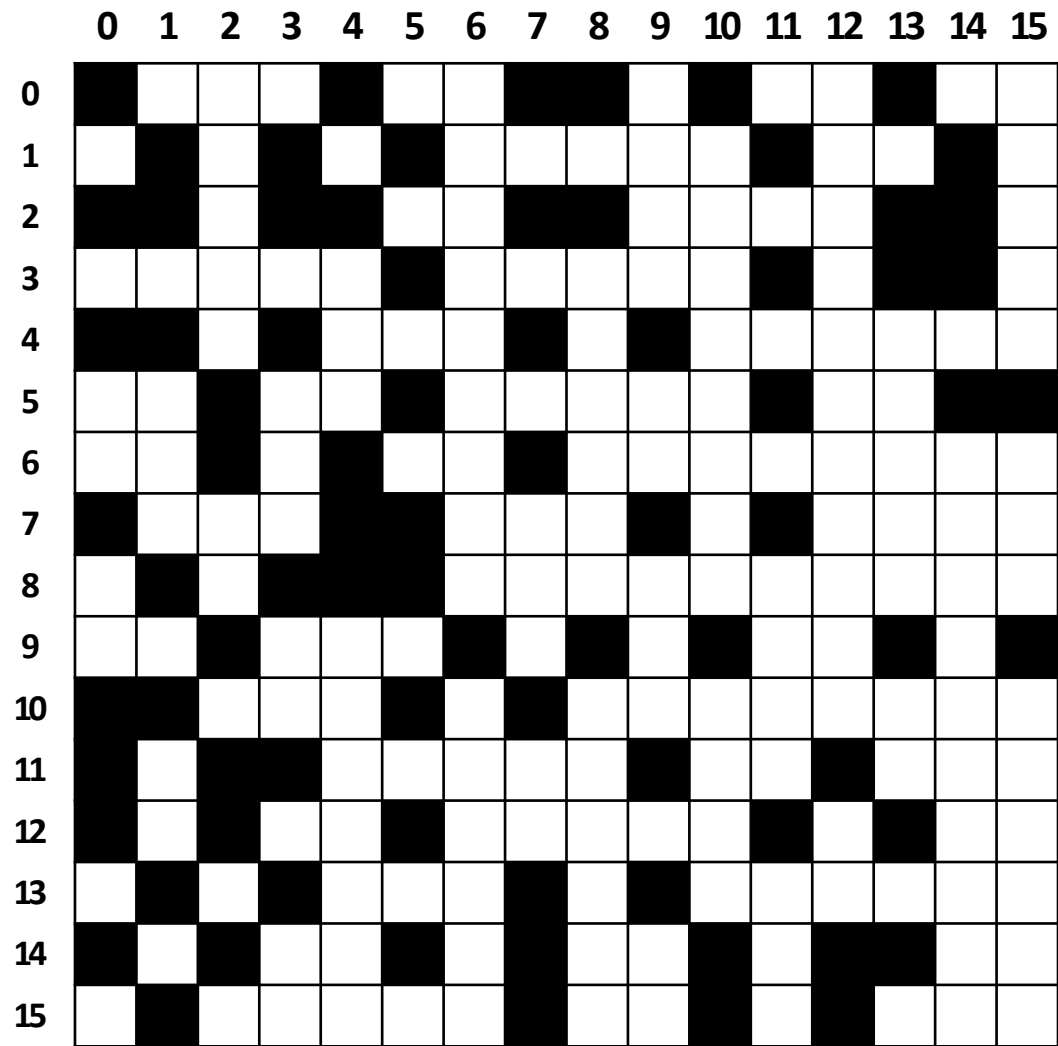
Baseline CSR SpMM



Baseline CSR SpMM



Baseline CSR SpMM



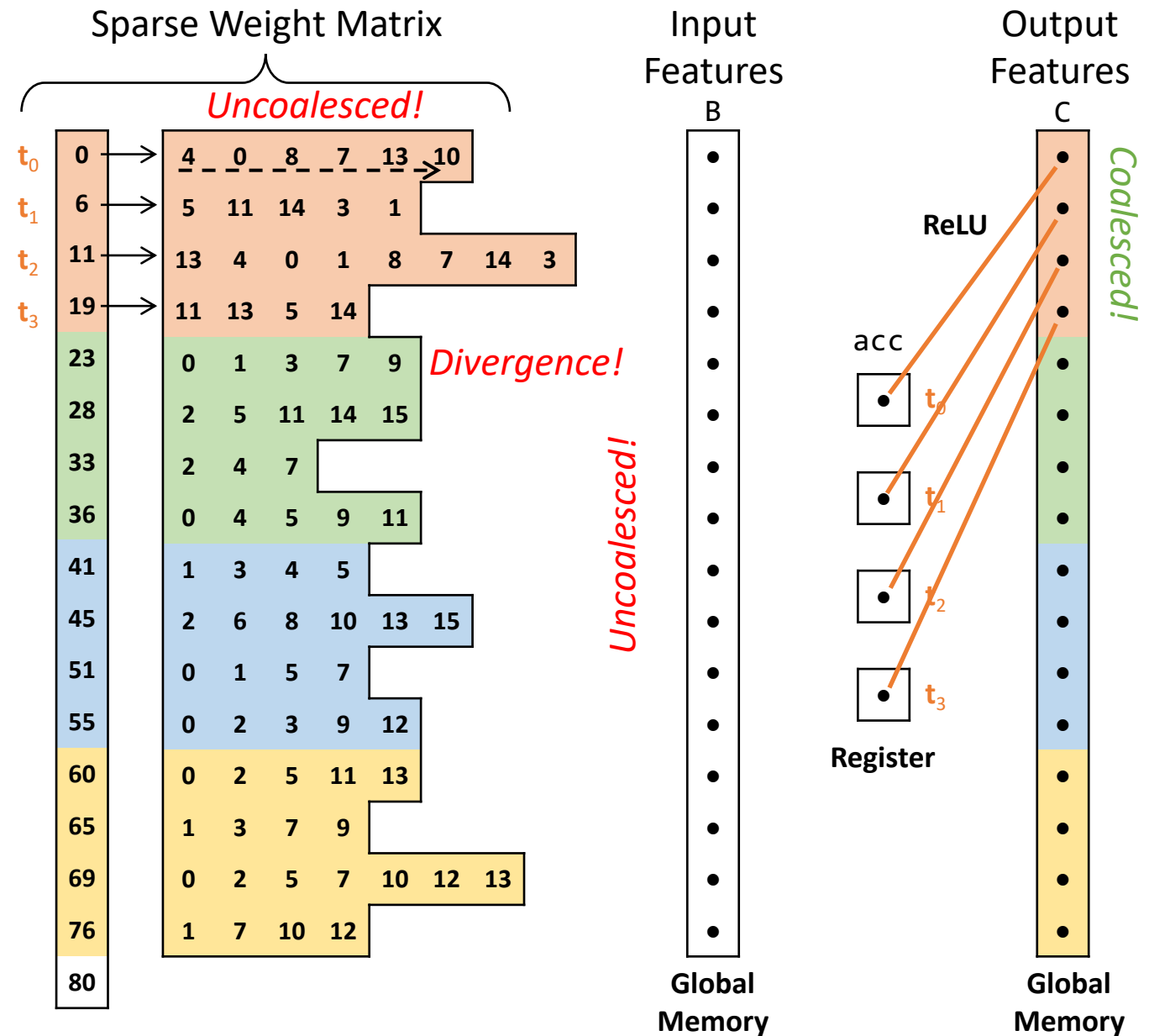
Baseline CSR SpMM

Data Access Redundancies

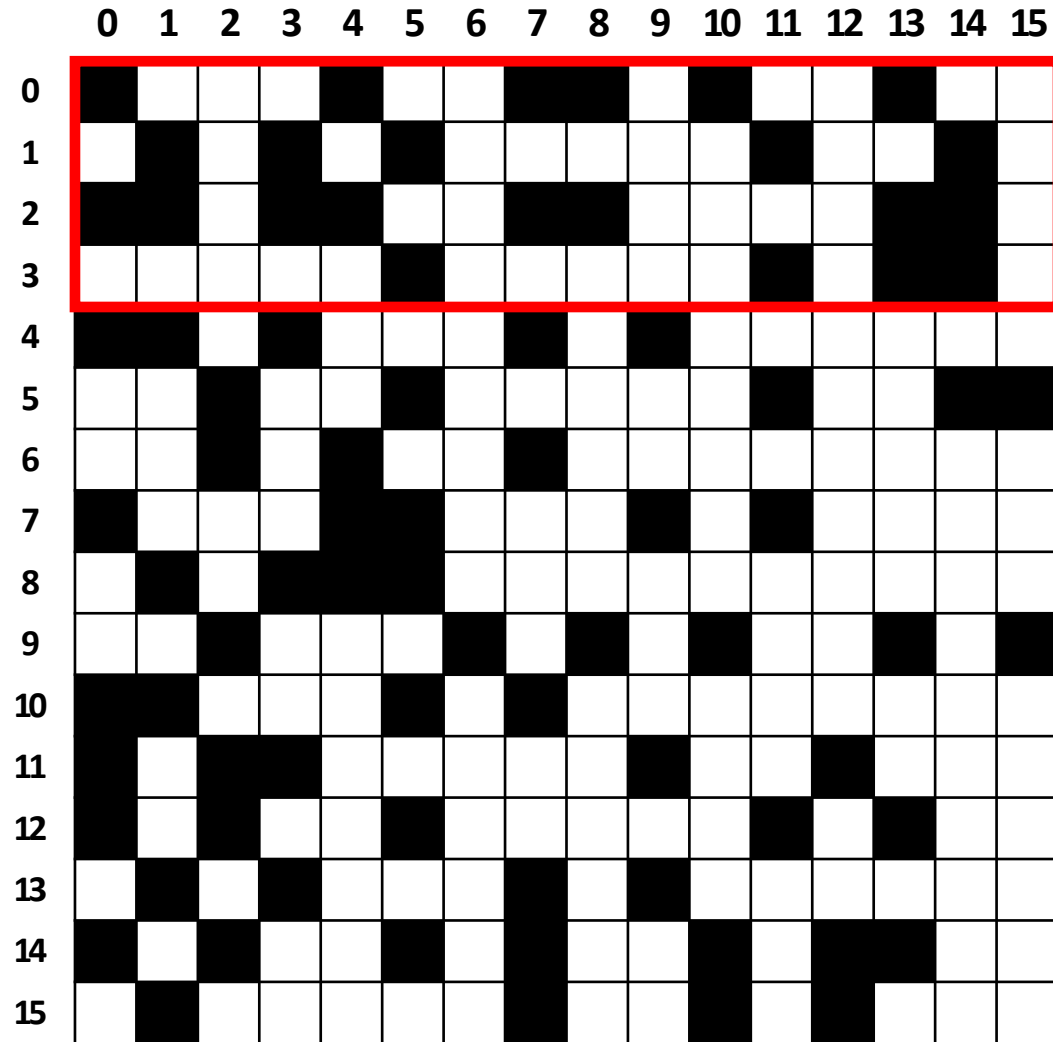
- Input features by different threads
- Weight matrix by all output features

Data Access Latencies

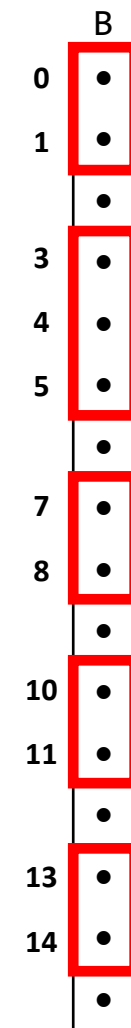
- Irregular access to input features
- Uncoalesced access to weight matrix

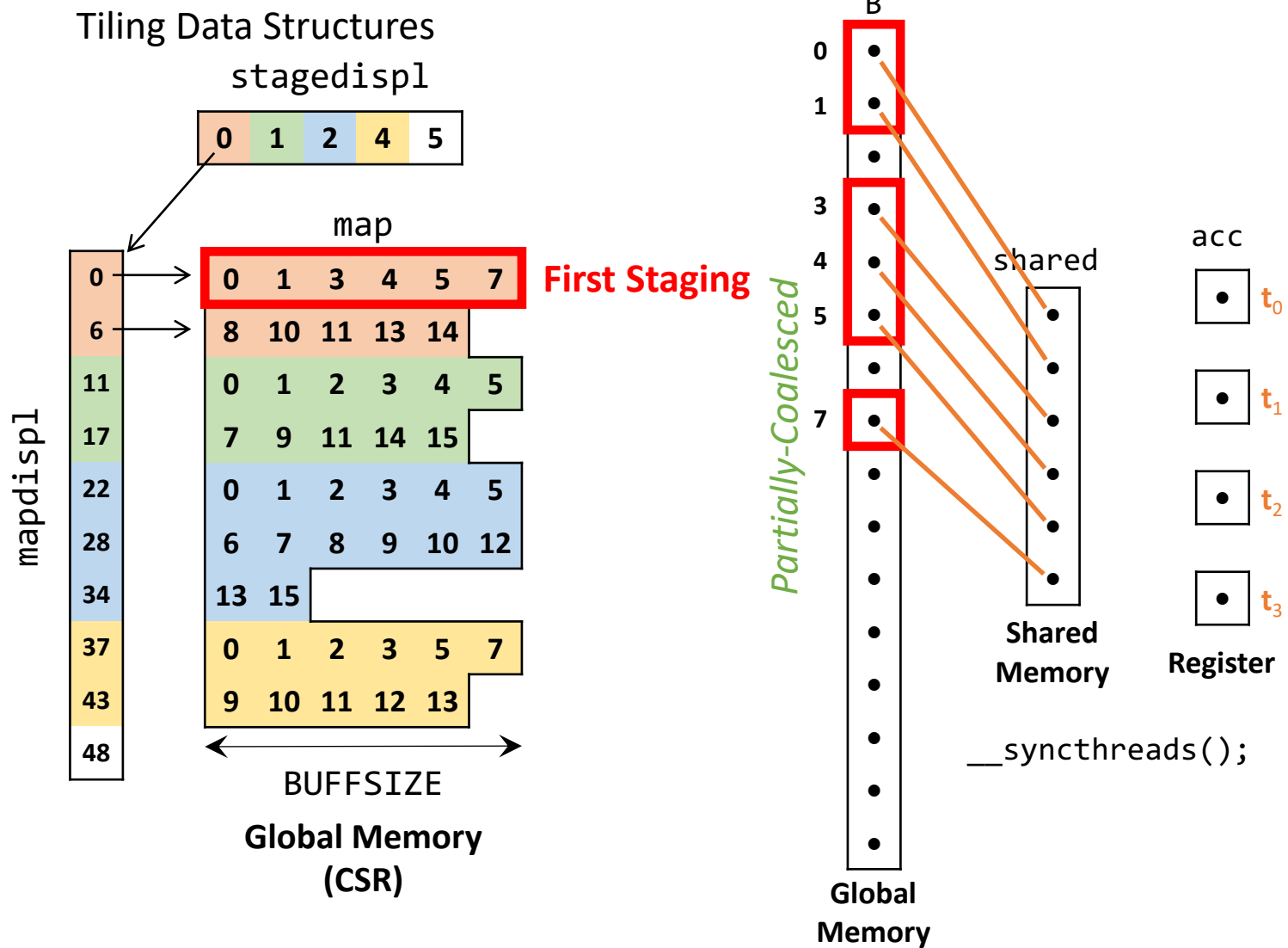


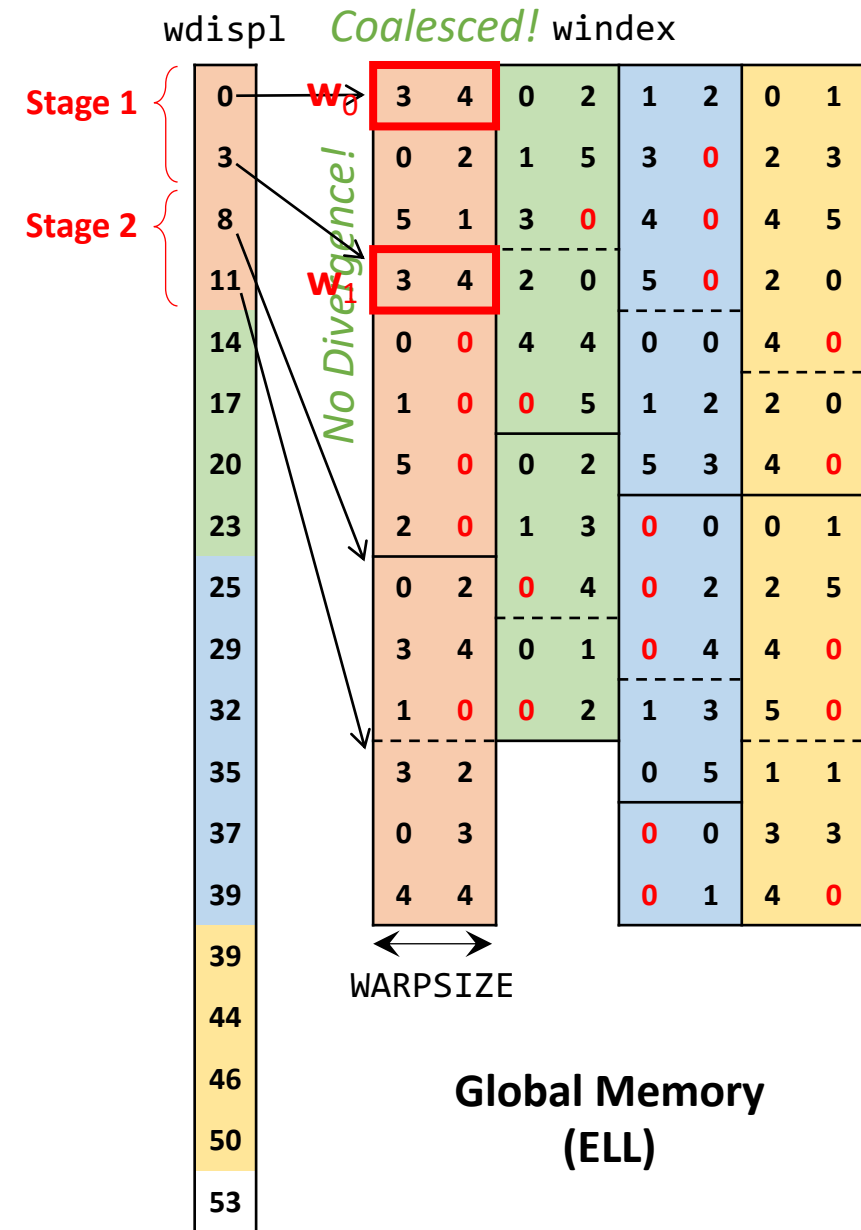
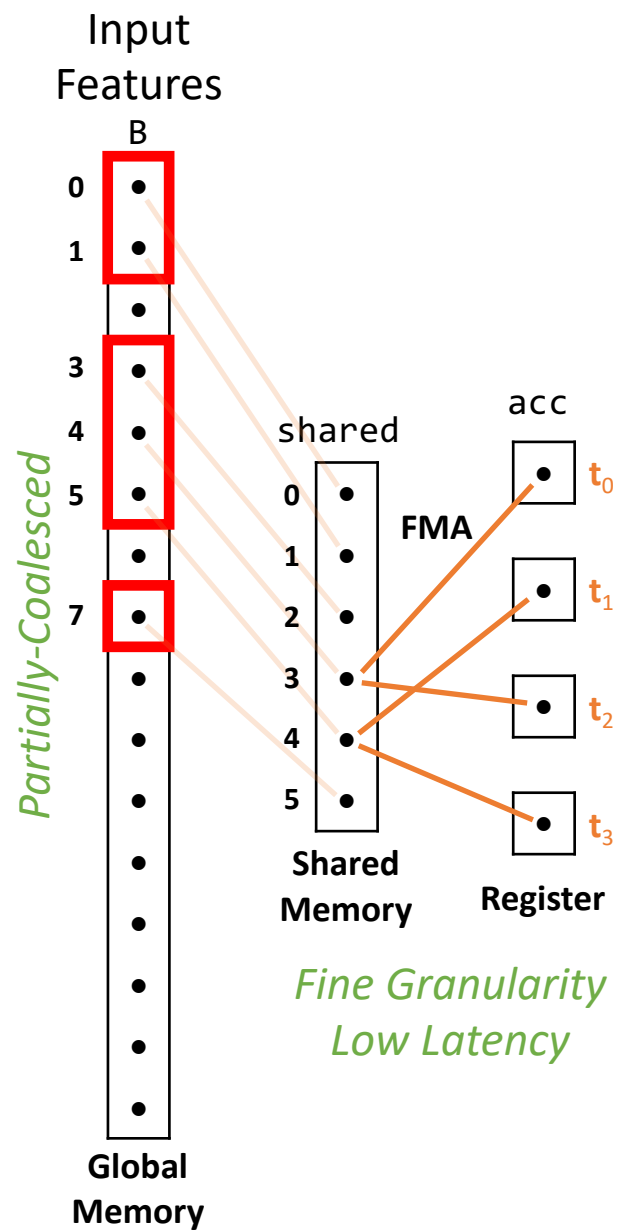
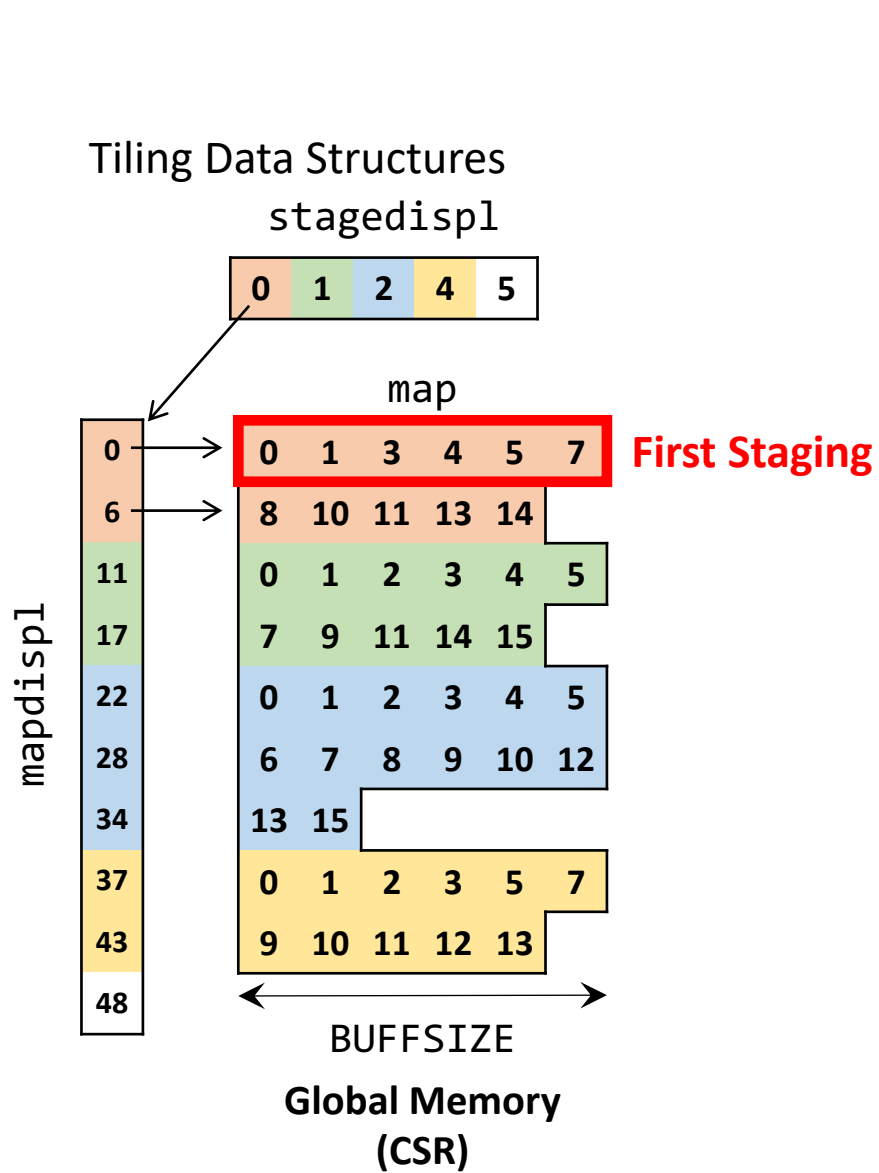
Tiled SpMM

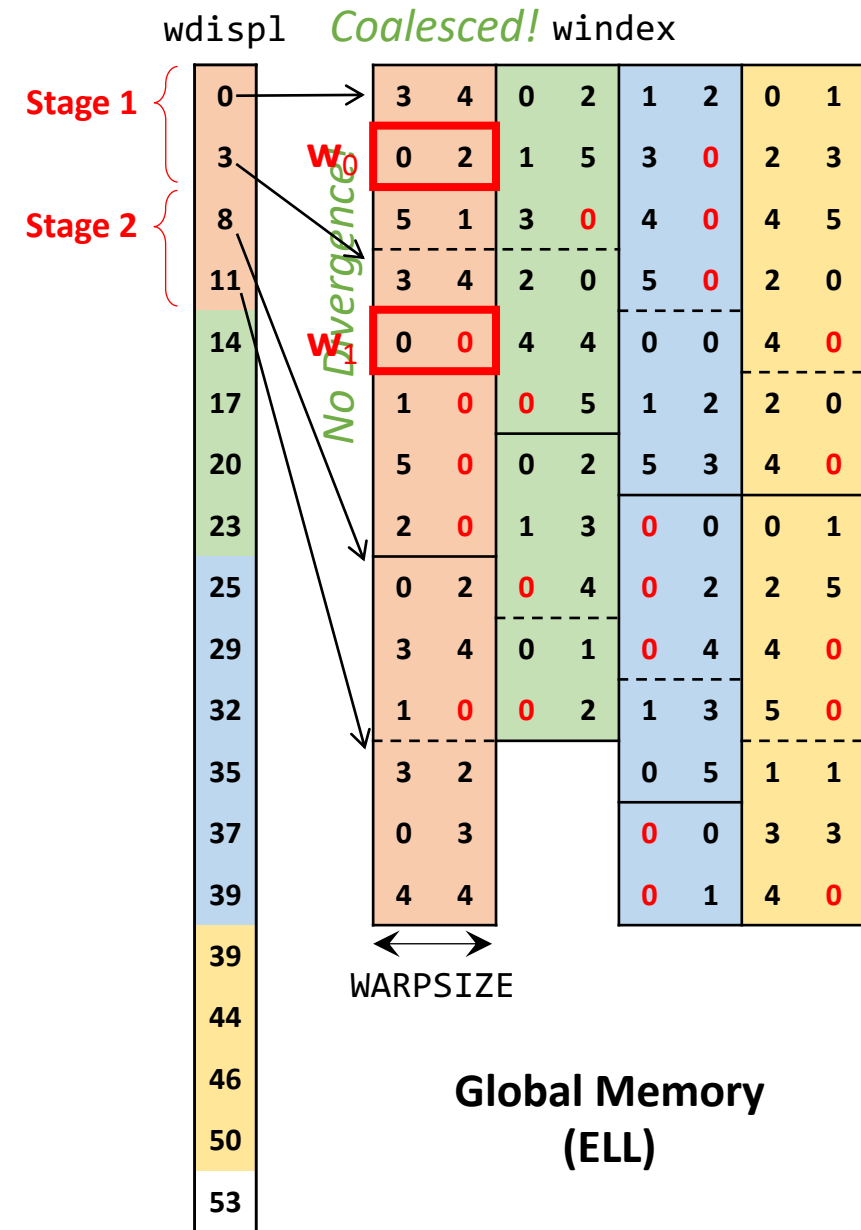
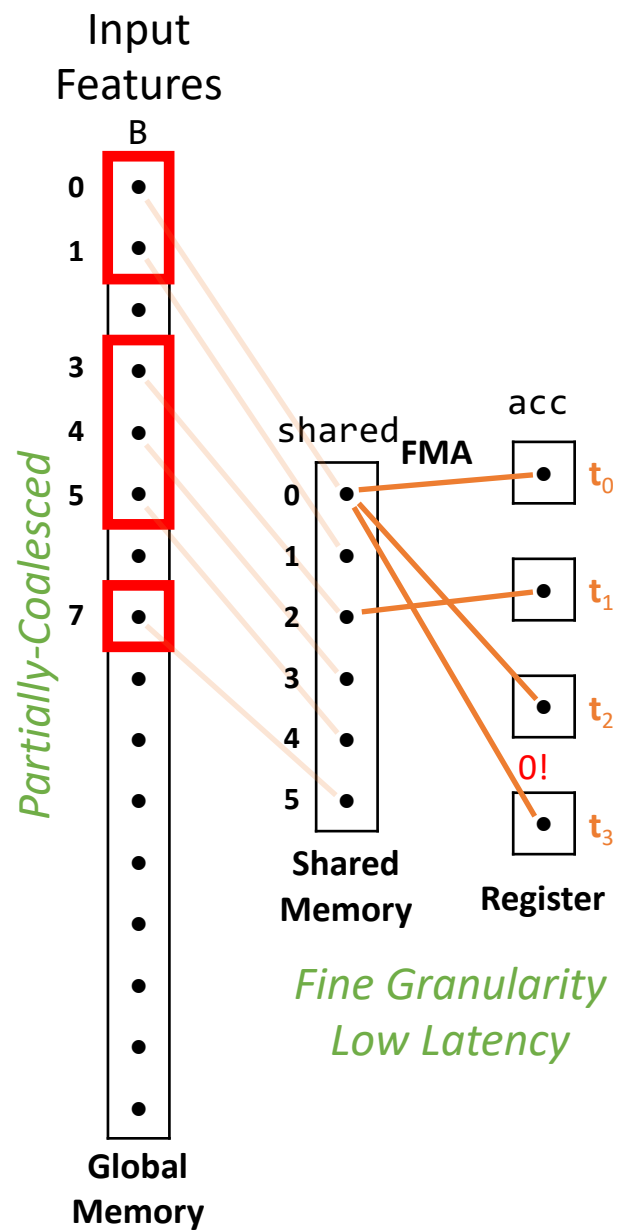
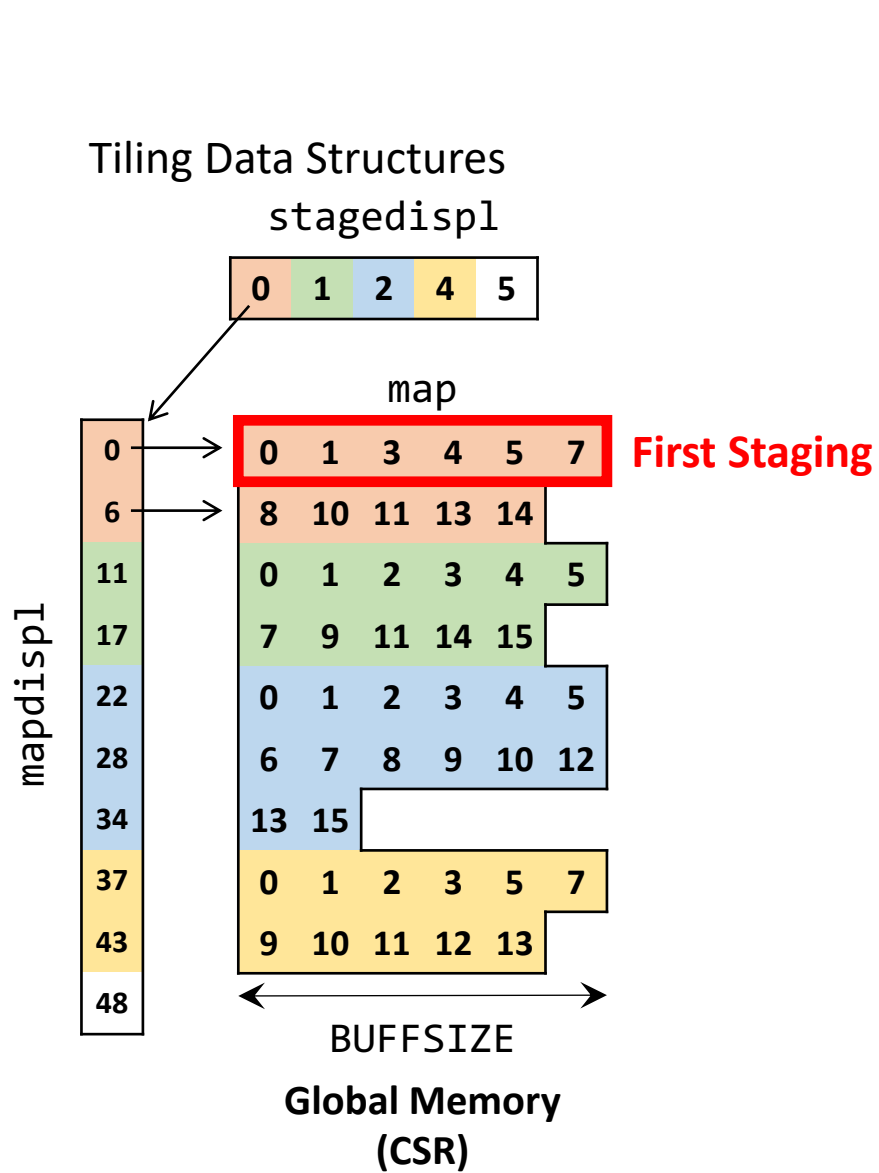


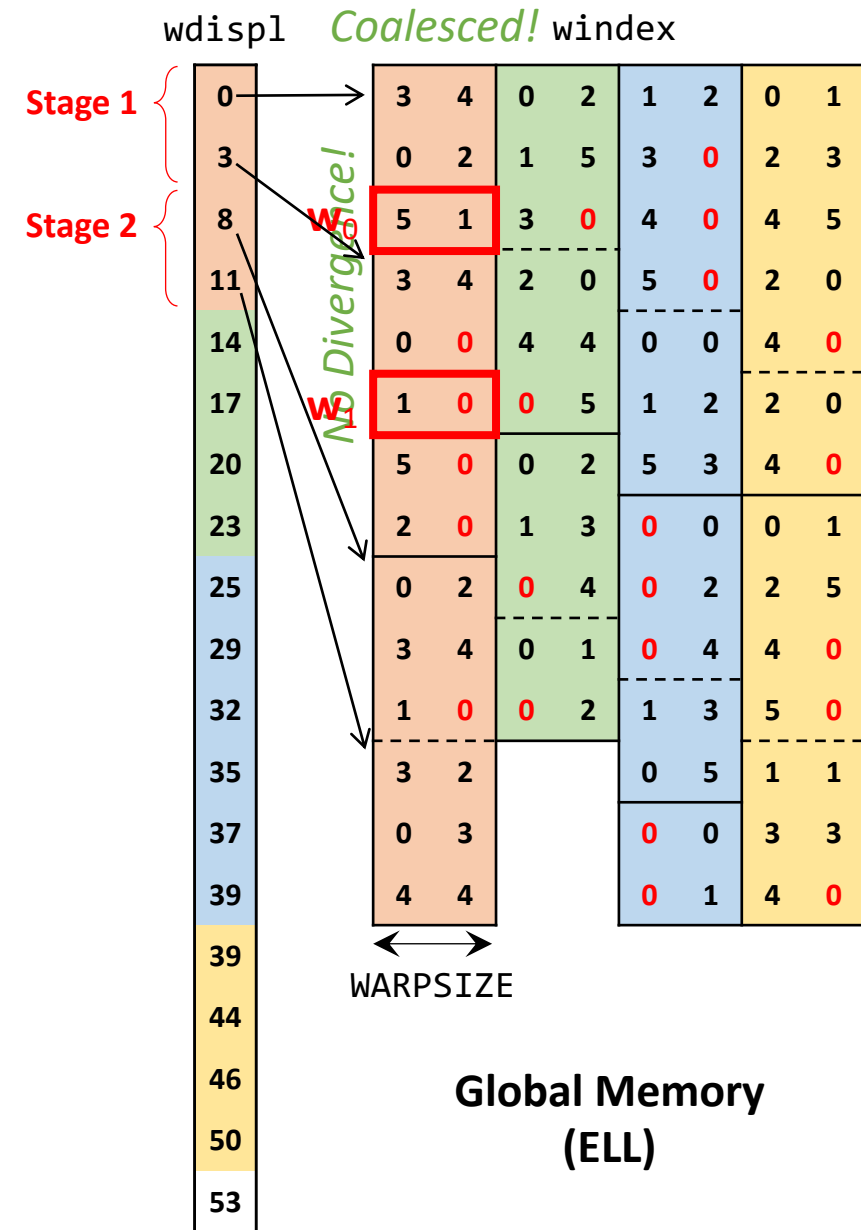
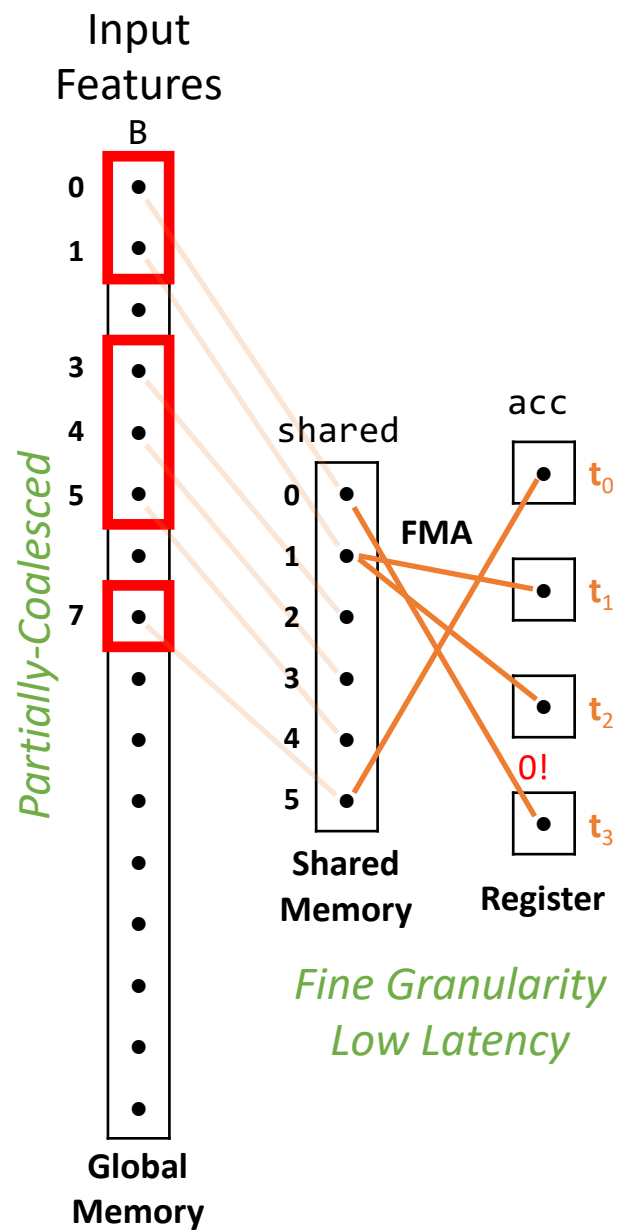
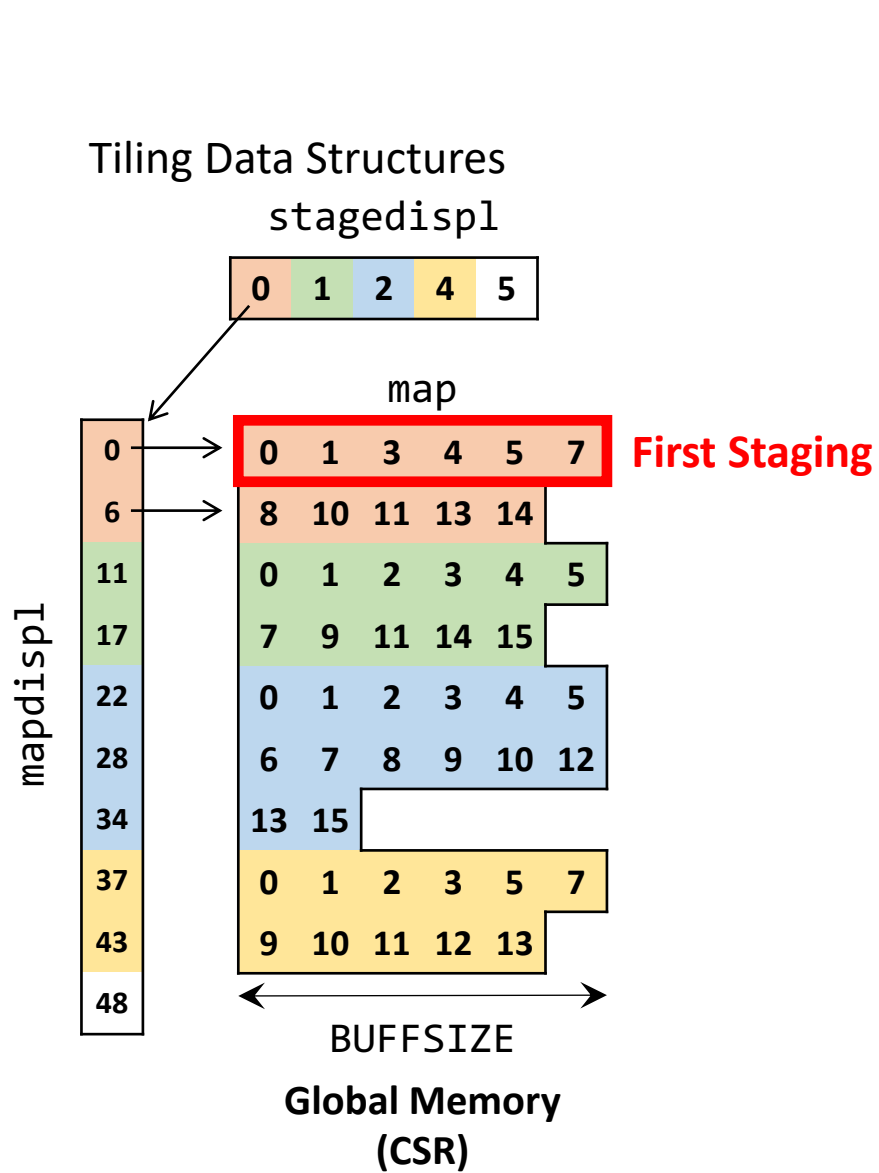
Input
Features

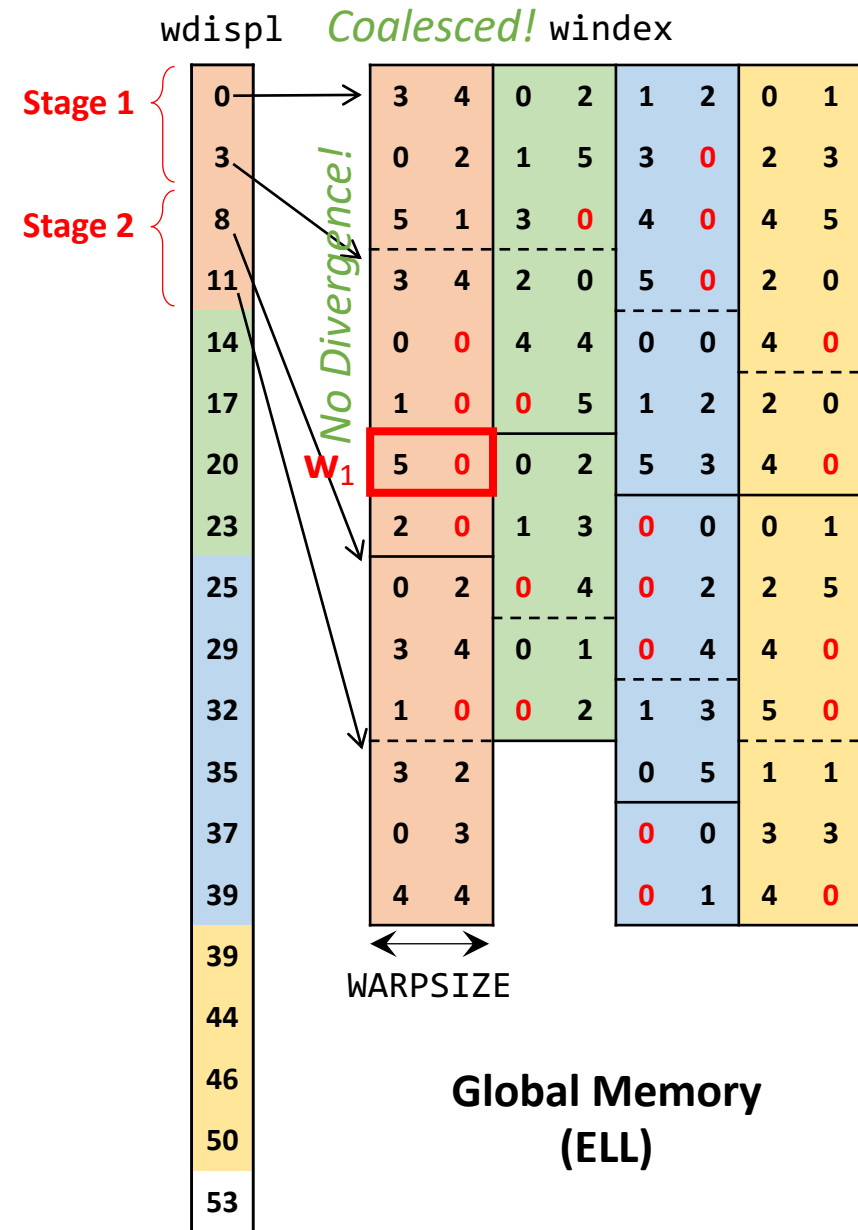
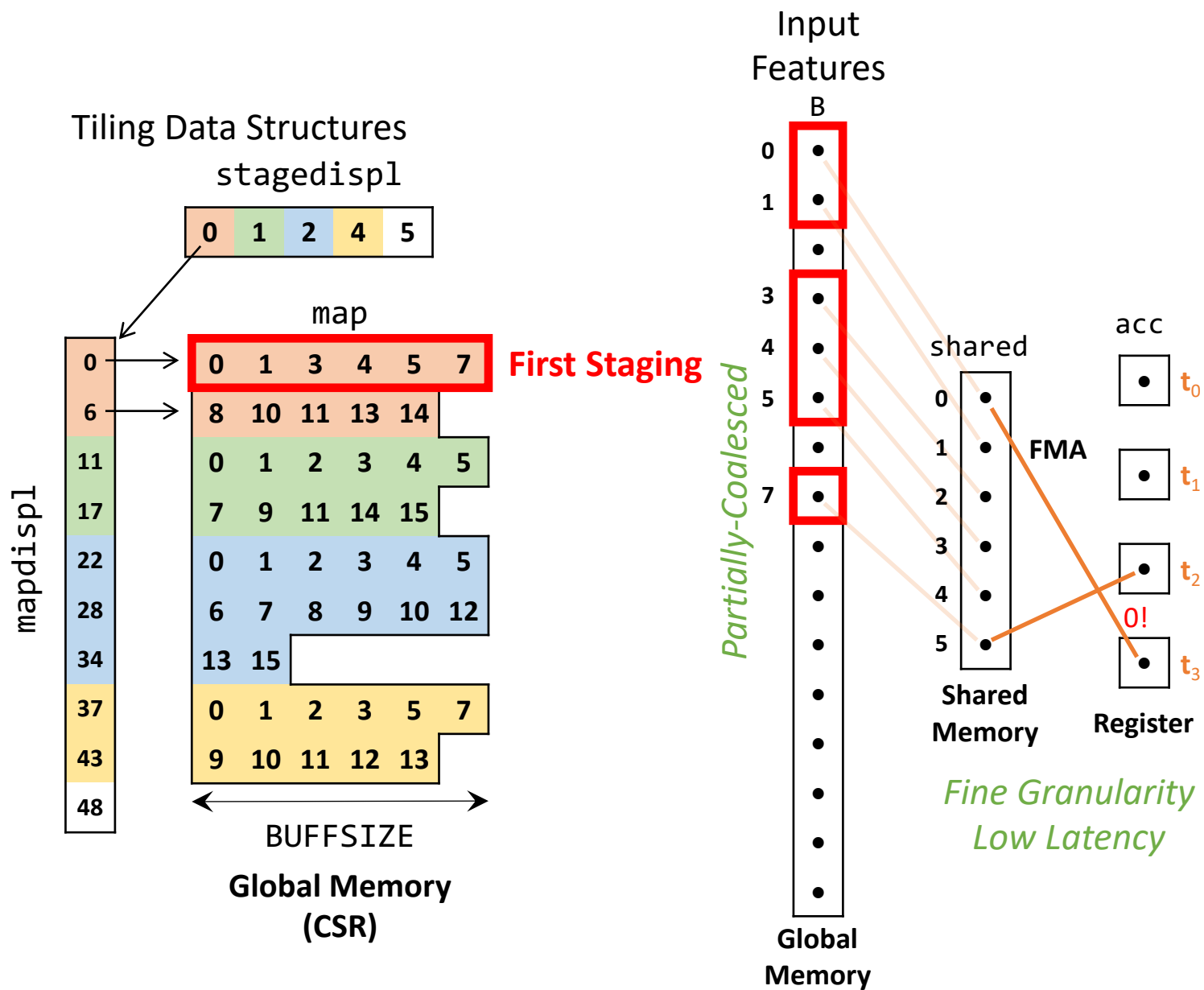


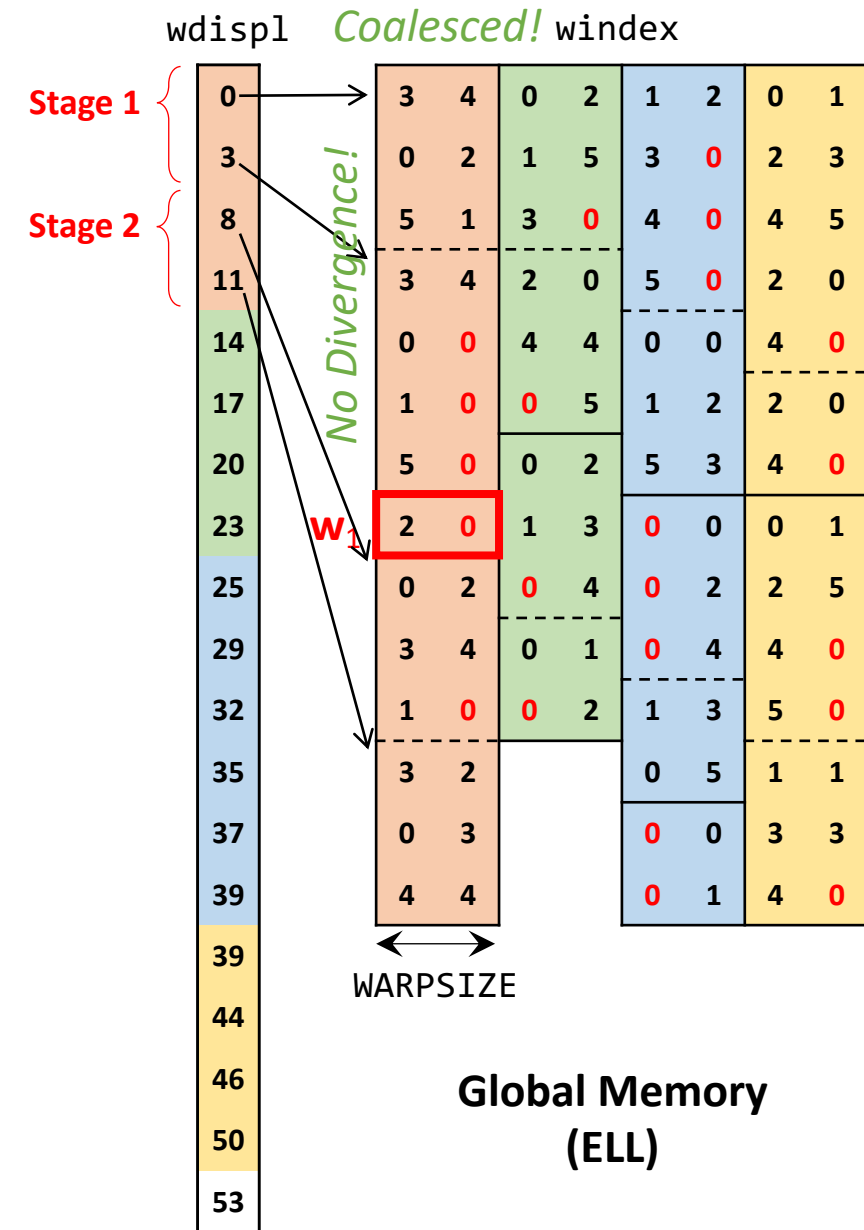
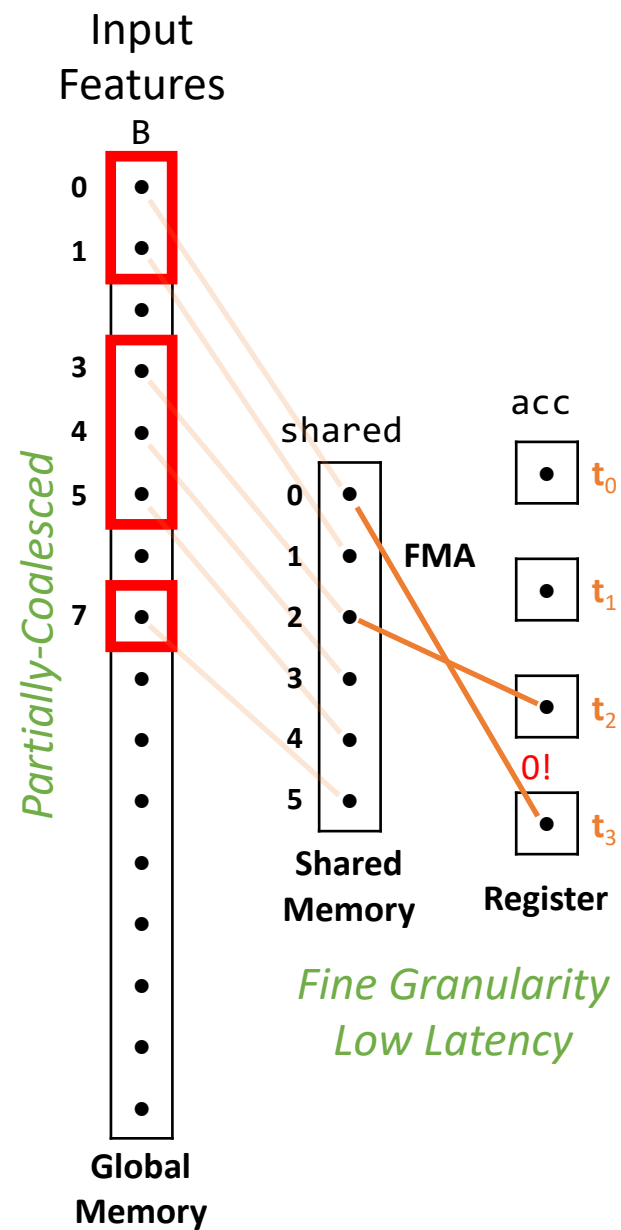
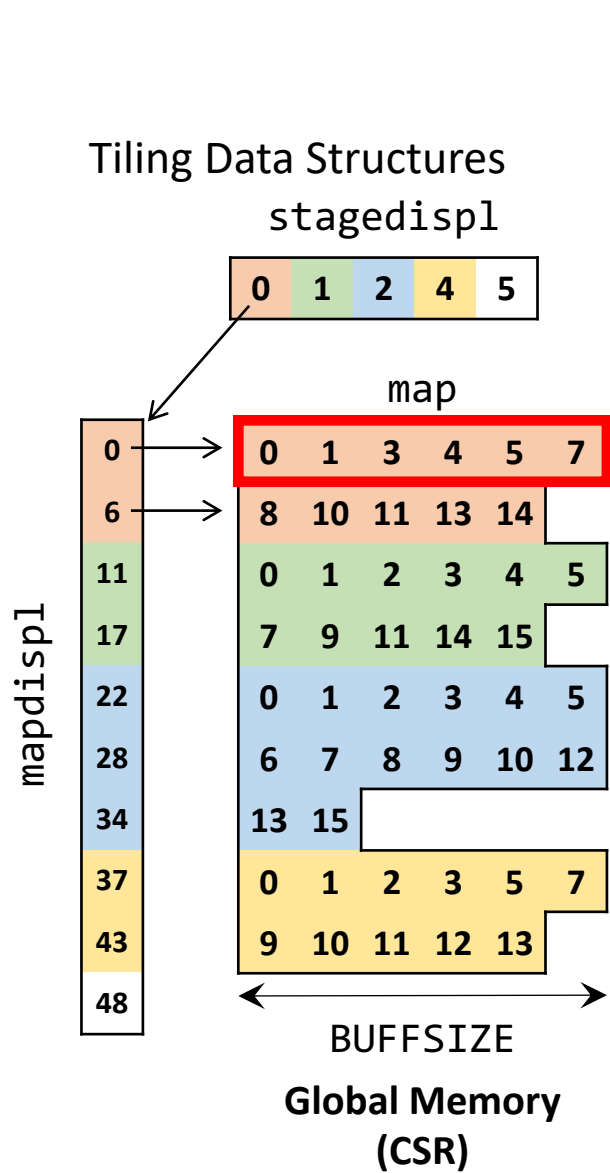


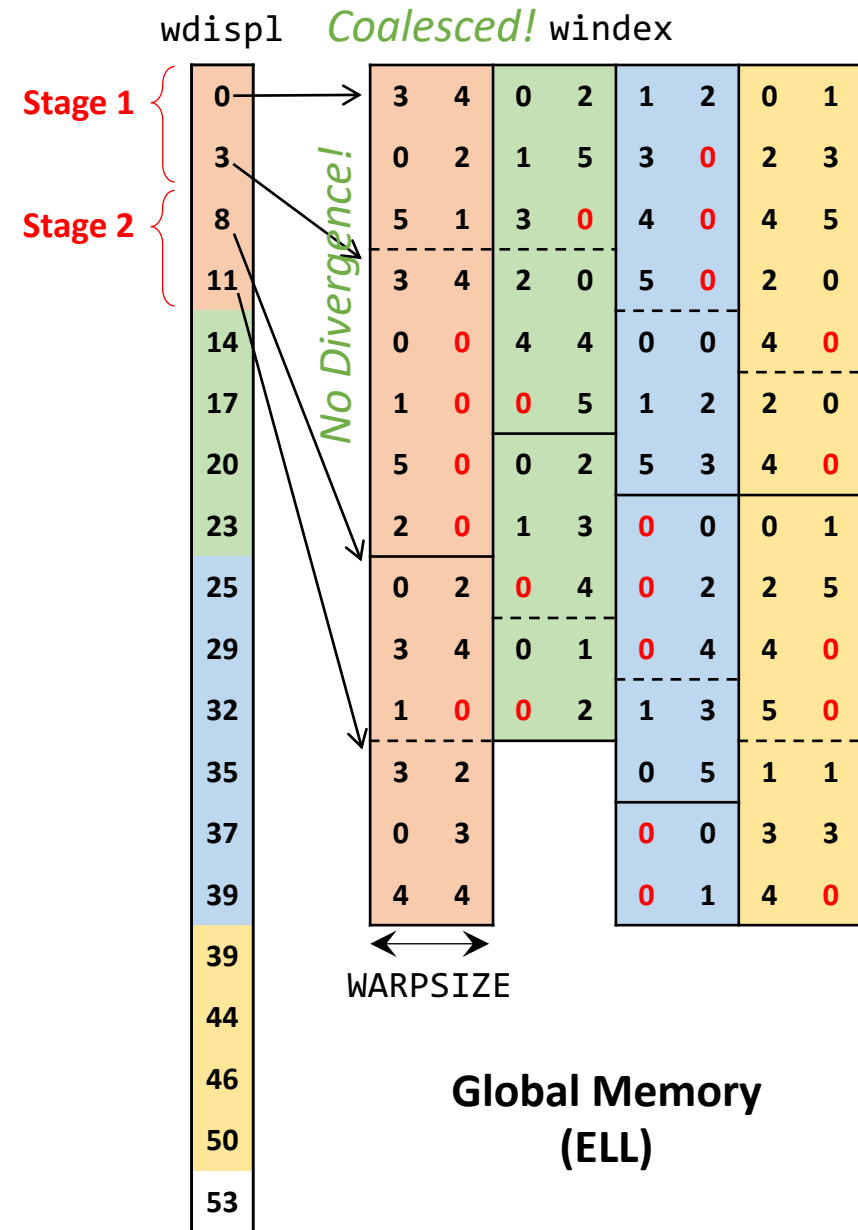
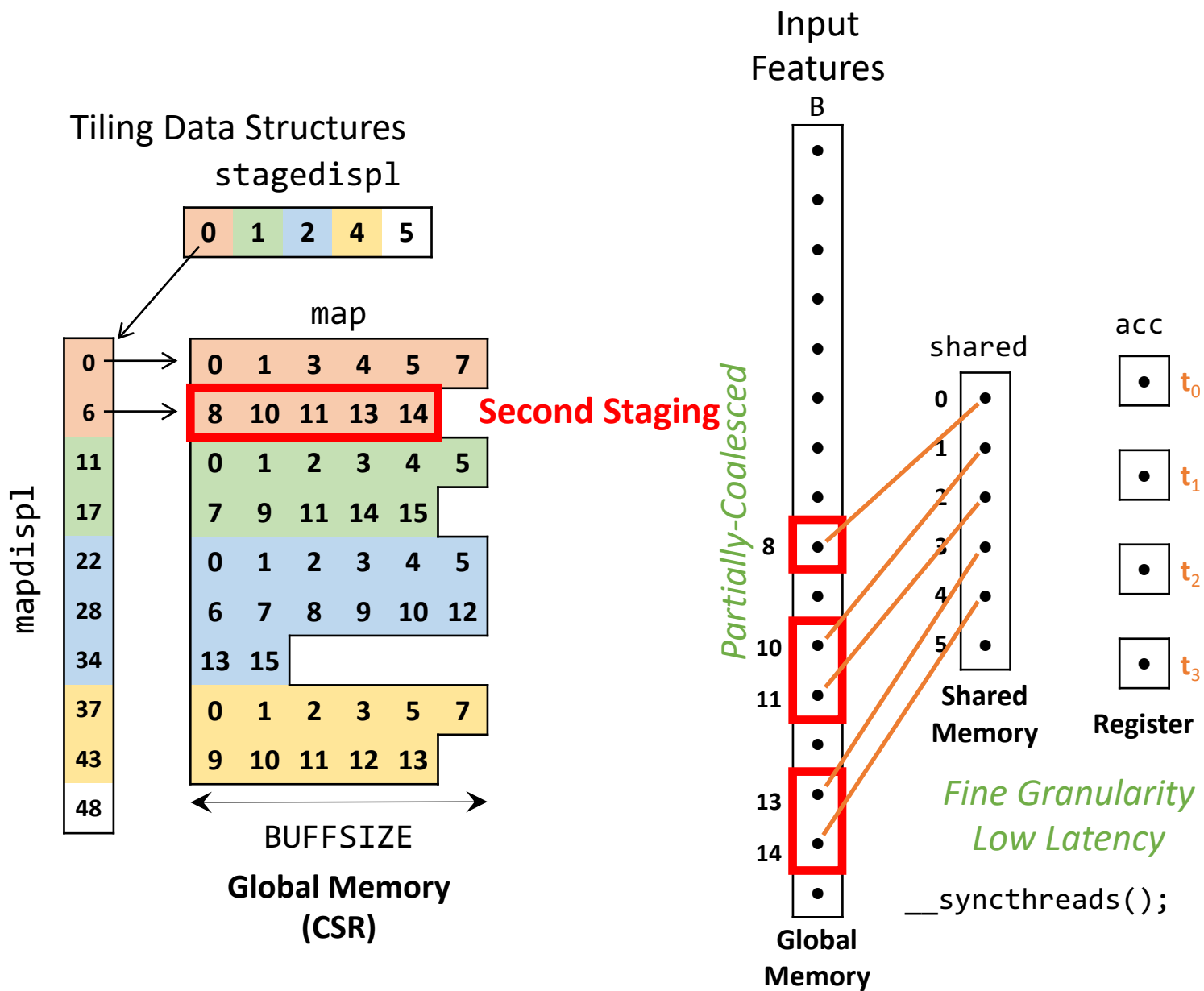


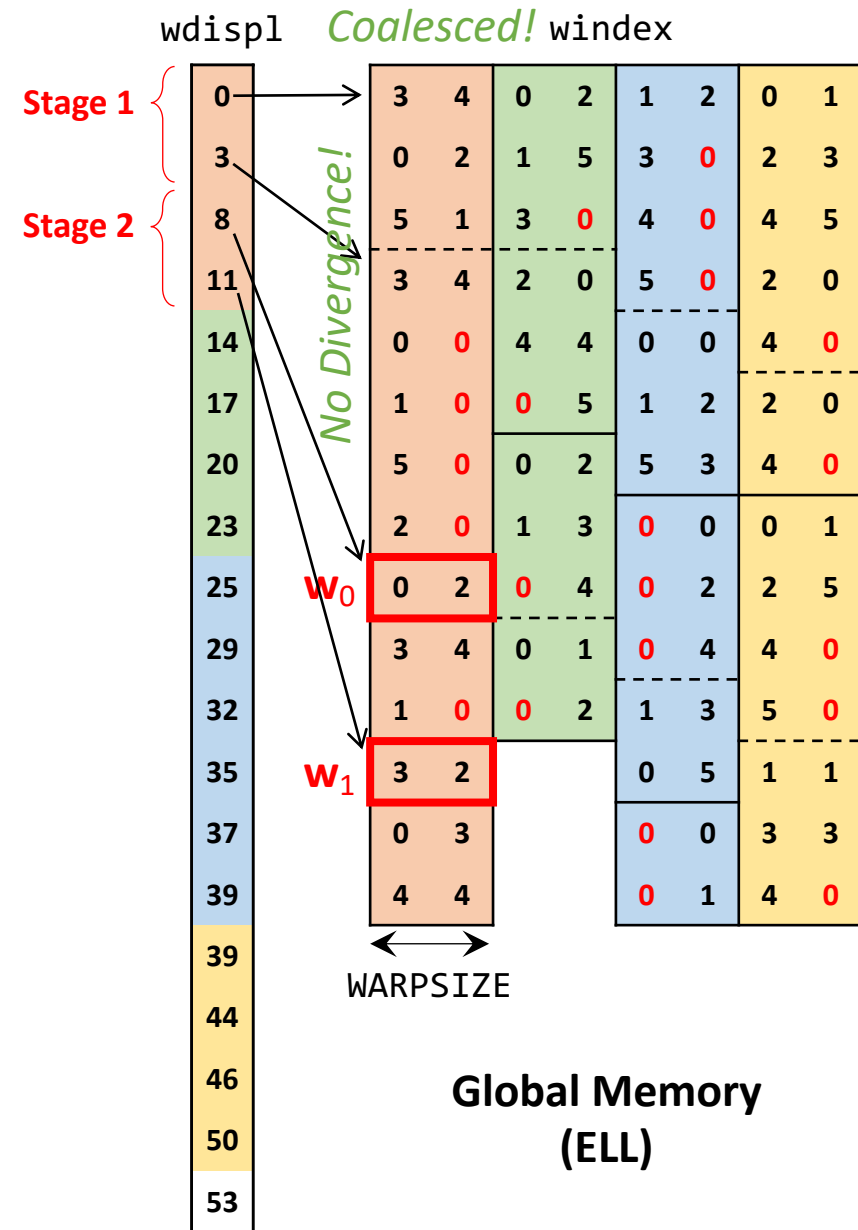
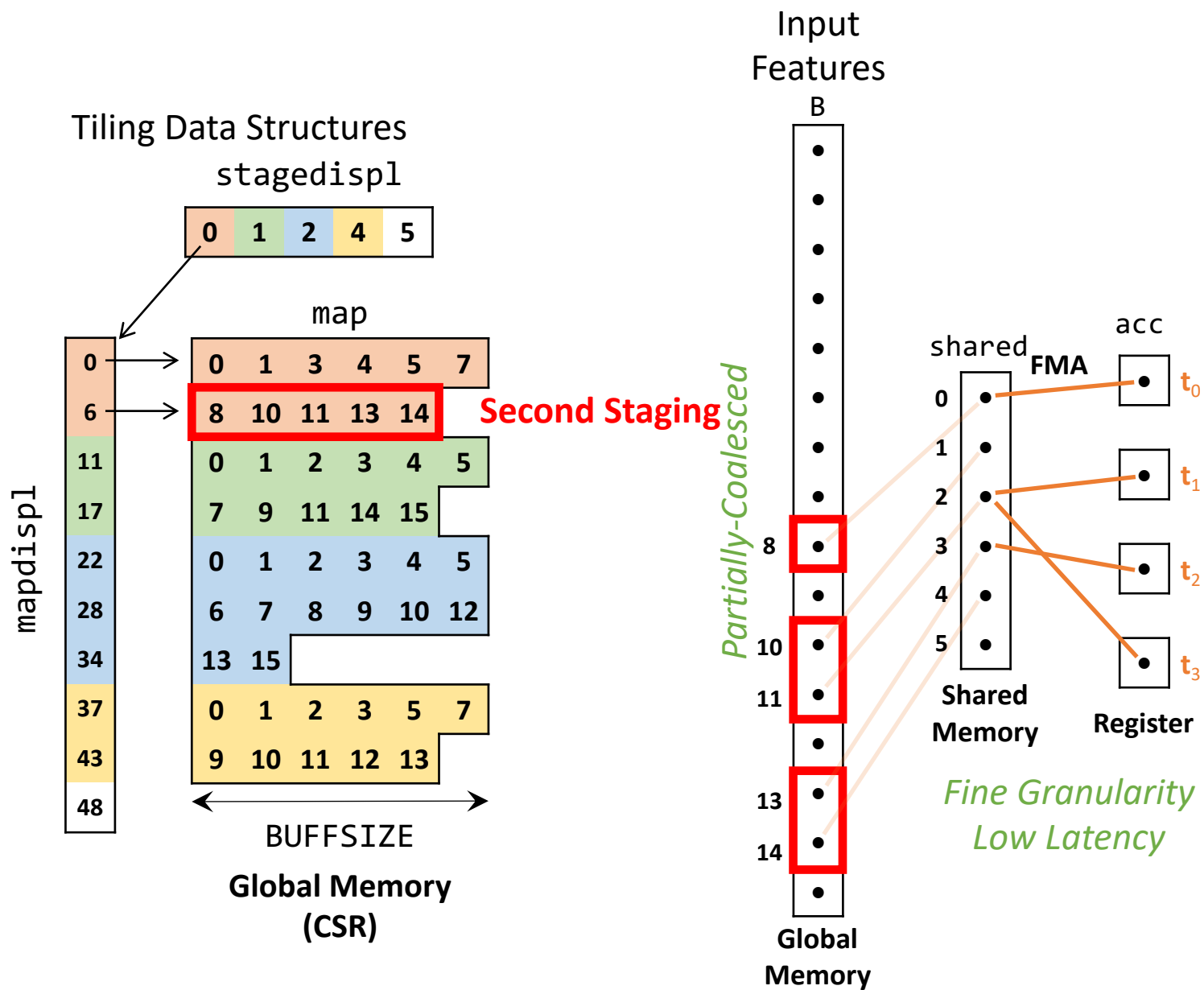


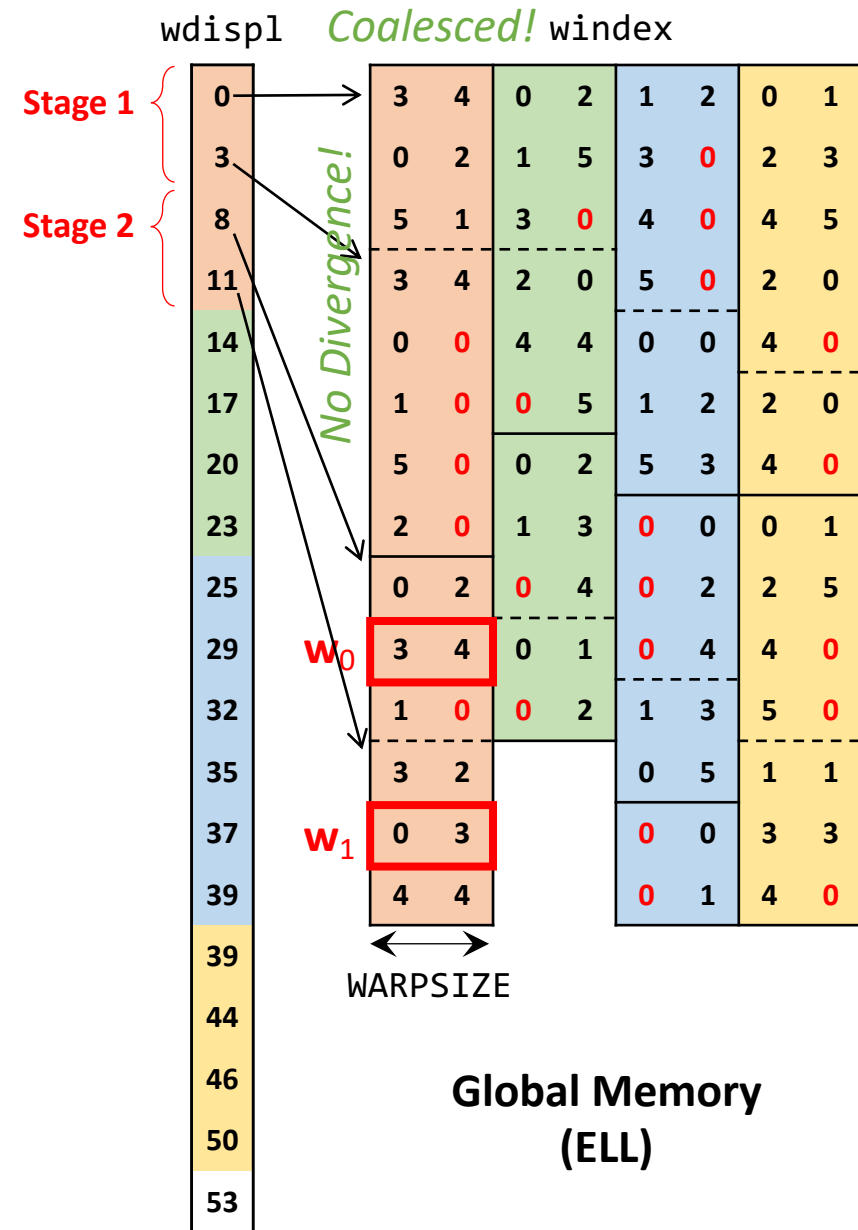
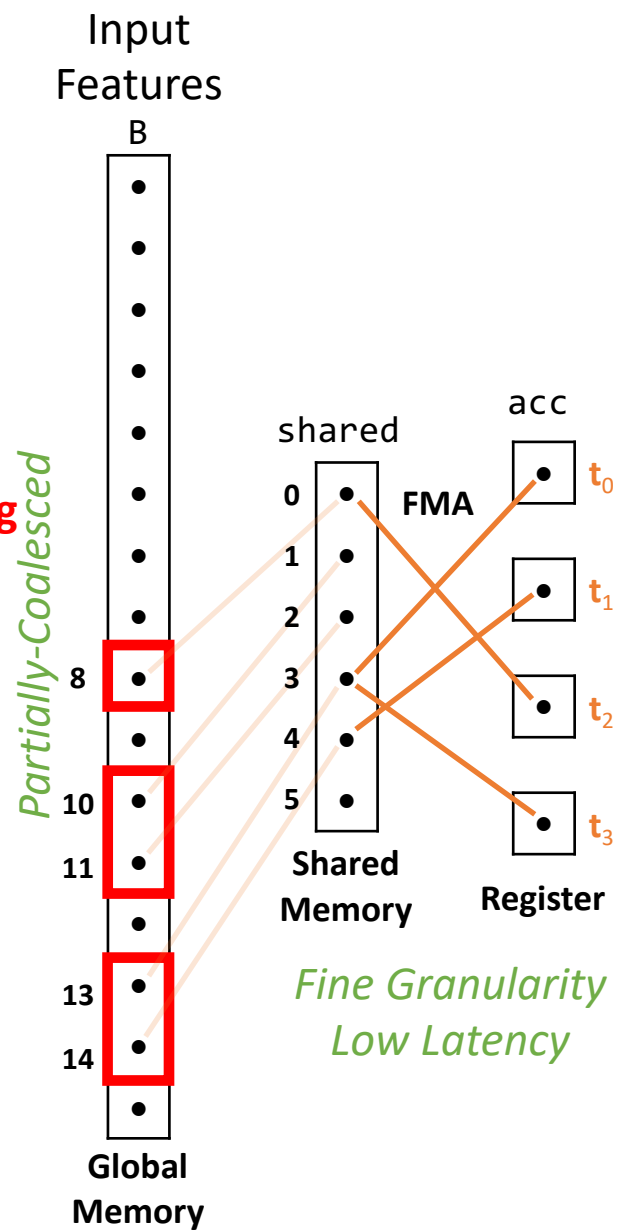
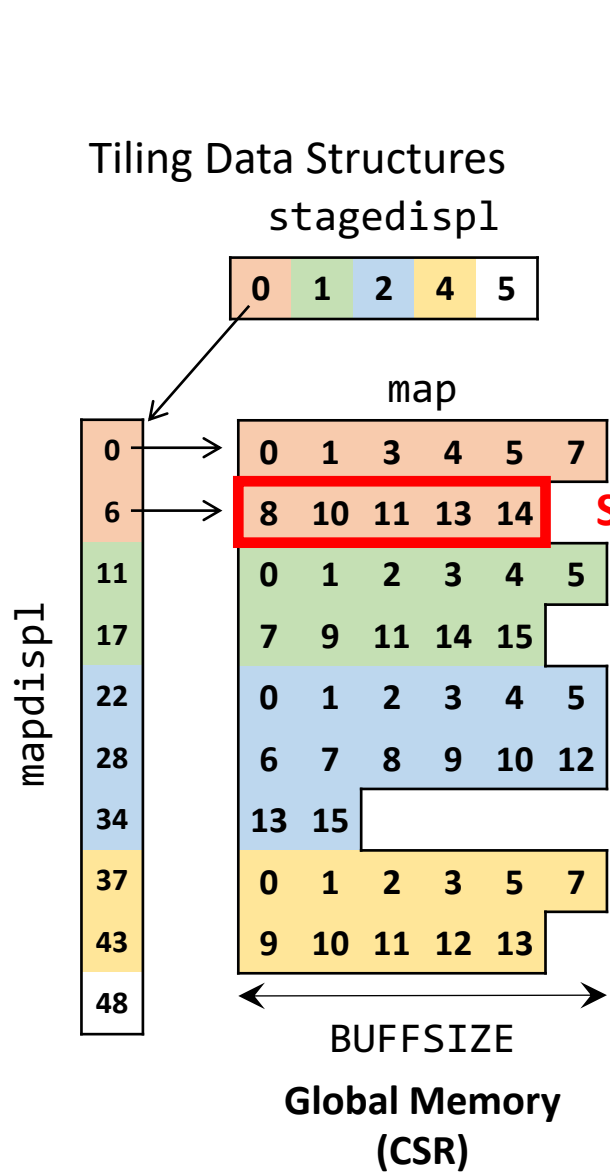


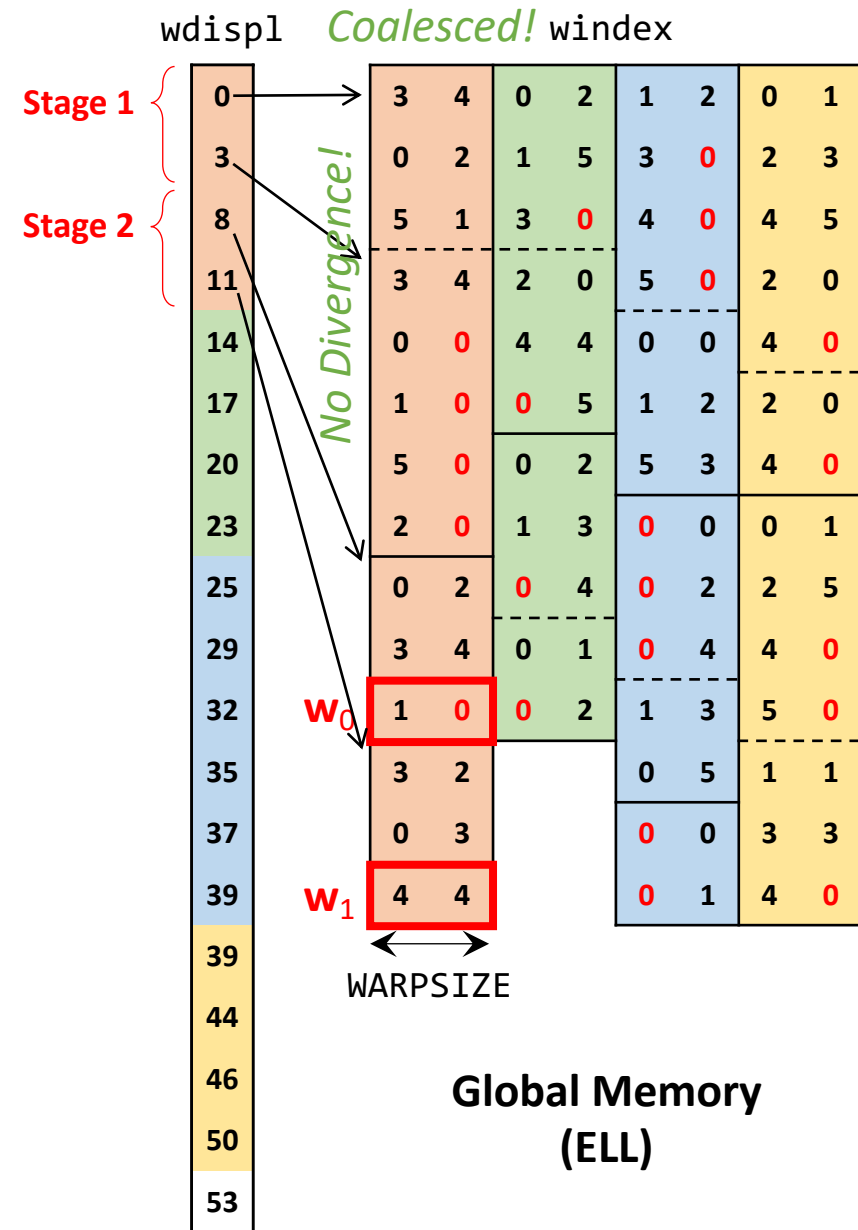
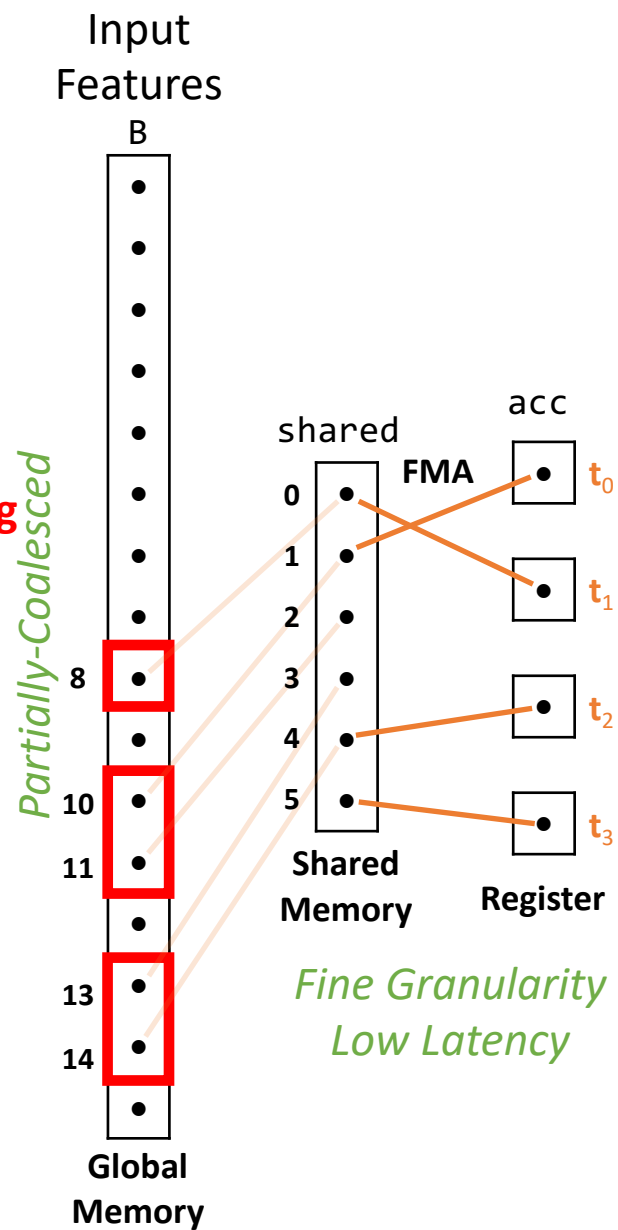
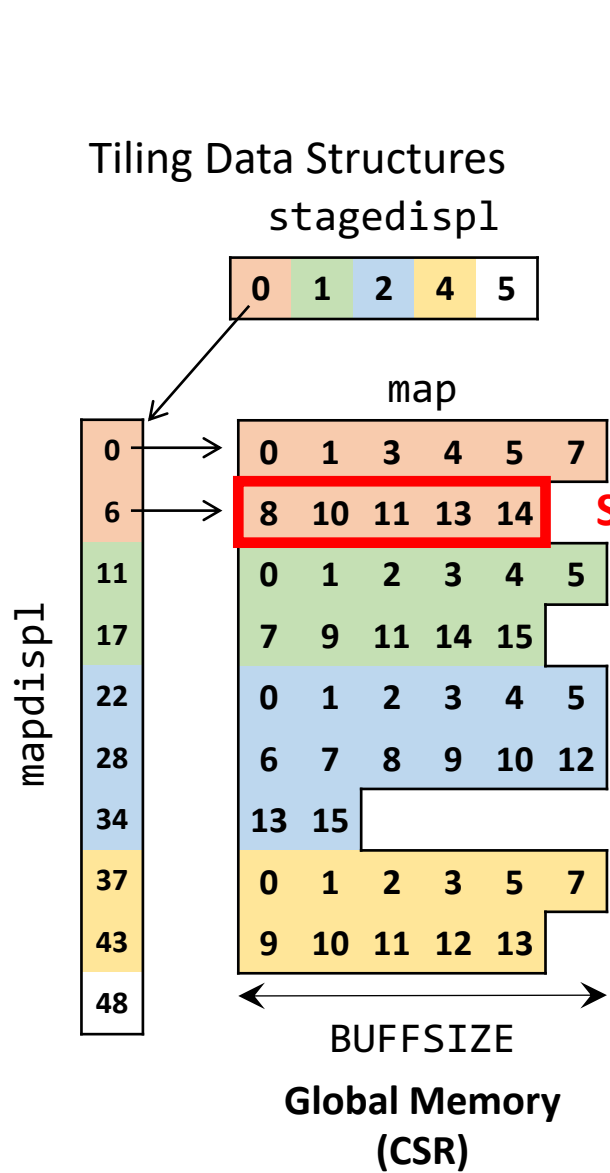




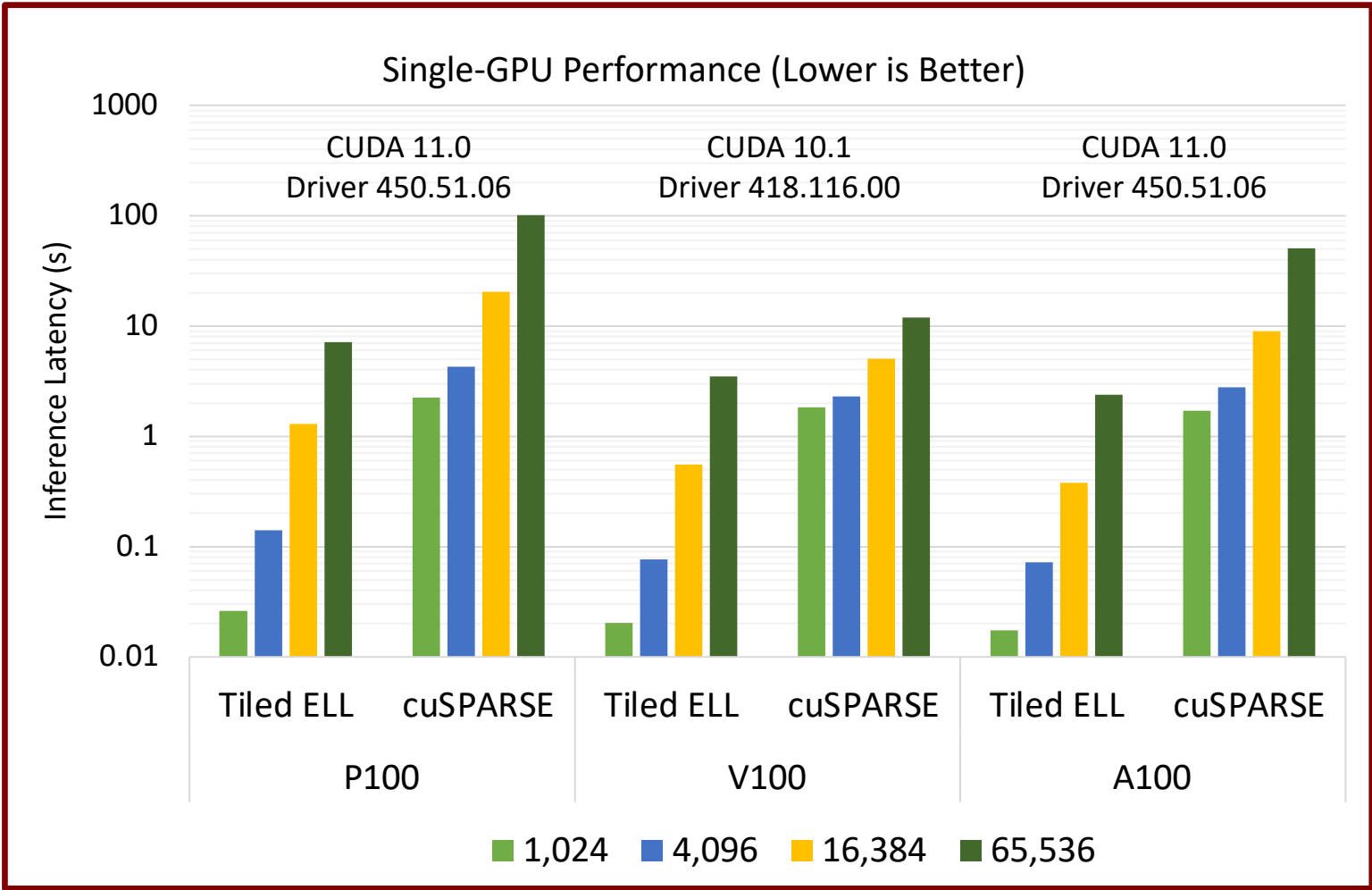








Application: Sparse Deep Neural Network



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Inference Throughput (TeraEdges/Second)

Number of V100 GPUs (Six per Node)

Neurons	Layers	Single V100	Single A100	Number of V100 GPUs (Six per Node)								
				3	6	12	24	48	96	192	384	768
1024	120	10.51 (0.225s)	16.74 (1.59×)	18.92	22.46	25.52	28.52	27.77	29.17	27.89	29.12	29.13
	480	12.87 (0.073s)	20.99 (1.63×)	21.47	24.34	26.92	28.73	28.43	29.30	28.80	29.10	23.06
	1920	14.30 (0.264s)	20.68 (1.45×)	22.26	24.77	27.33	28.70	28.58	28.60	28.73	28.83	28.83
4096	120	9.45 (0.100s)	14.27 (1.51×)	20.69	31.36	47.82	62.03	70.31	75.81	79.11	81.13	82.20
	480	11.74 (0.322s)	18.63 (1.59×)	28.18	40.58	56.54	67.63	73.16	77.27	80.02	79.97	82.22
	1920	13.88 (1.08s)	19.86 (1.43×)	30.53	44.48	62.74	72.57	73.72	76.25	79.99	80.67	82.32
16384	120	6.15 (0.614s)	11.60 (1.89×)	16.31	28.85	50.74	64.33	89.18	111.44	146.88	114.87	111.30
	480	7.45 (2.027s)	14.31 (1.92×)	19.82	32.88	50.83	71.45	95.78	112.61	138.62	138.30	139.44
	1920	7.84 (7.704s)	15.27 (1.95×)	20.86	33.62	57.08	77.73	104.83	120.63	146.11	146.30	146.40
65536	120	3.47 (4.352s)	8.15 (2.35×)	10.90	18.77	34.20	51.14	73.67	100.72	162.19	173.25	179.58
	480	3.83 (15.769s)	9.08 (2.37×)	12.13	20.39	37.63	56.66	75.29	108.06	166.15	170.26	169.30
	1920	3.93 (61.474s)	9.33 (2.37×)	12.47	20.88	38.81	58.08	77.55	112.01	167.43	170.06	171.37

Application: Sparse Deep Neural Network



center for
cognitive computing
systems research



Graph Challenge Champions

2020 Champions

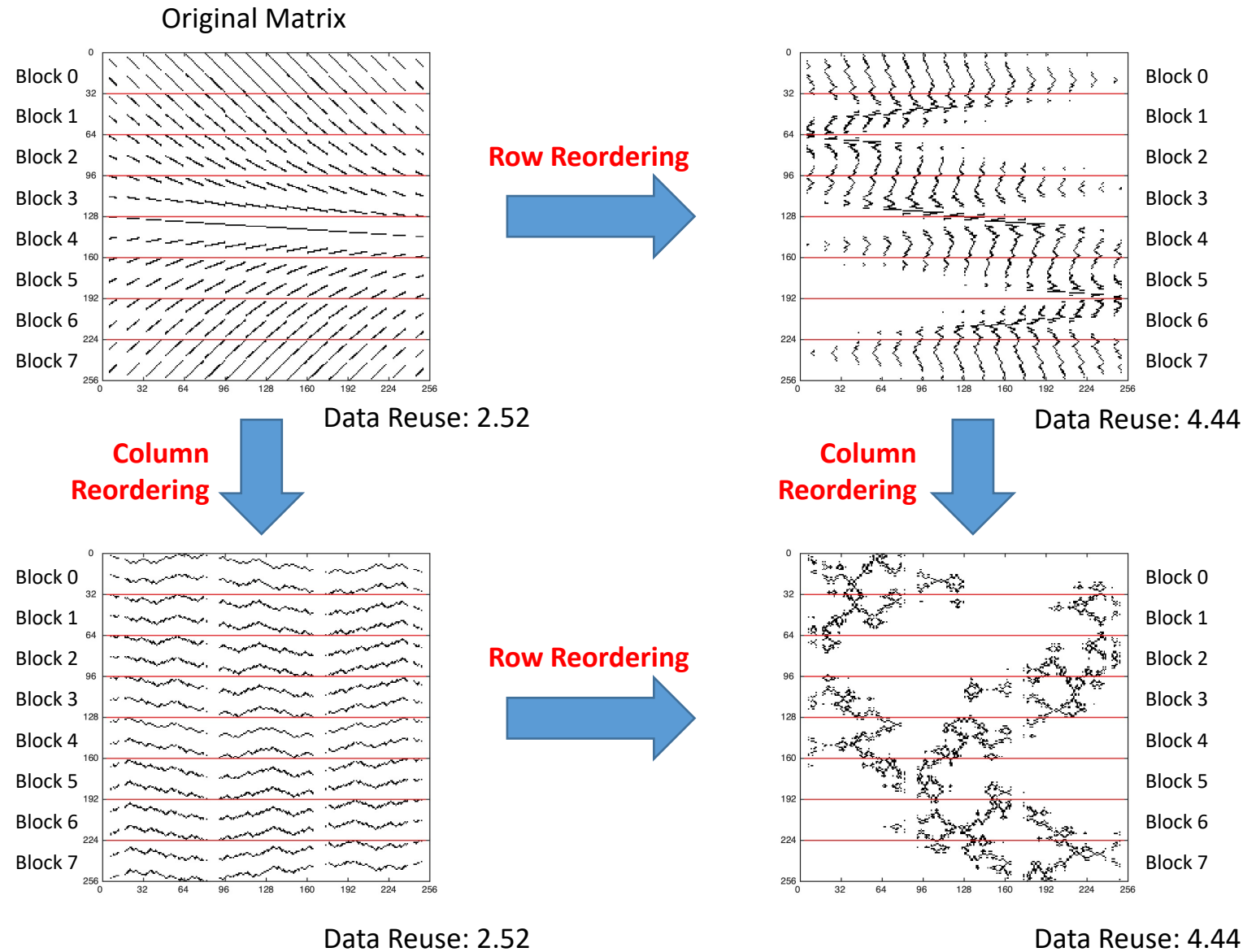
- *Scaling Graph Clustering with Distributed Sketches* - Benjamin Priest (LLNL), Alec Dunton (CU Boulder), Geoffrey Sanders (LLNL)
- *At-Scale Sparse Deep Neural Network Inference With Efficient GPU Implementation* - Mert Hidayetoglu, Carl Pearson, Vikram Sharma Mailthody (UIUC), Eiman Ebrahimi (Nvidia), Jinjun Xiong (IBM), Rakesh Nagi, Wen-mei W. Hwu (UIUC)
- *A Novel Inference Algorithm for Large Sparse Neural Network using Task Graph Parallelism* - Dian-Lun Lin, Tsung-Wei Huang (Univ of Utah)
- *TriC: Distributed-memory Triangle Counting by Exploiting the Graph Structure* - Sayan Ghosh, Mahantesh Halappanavar (PNNL)



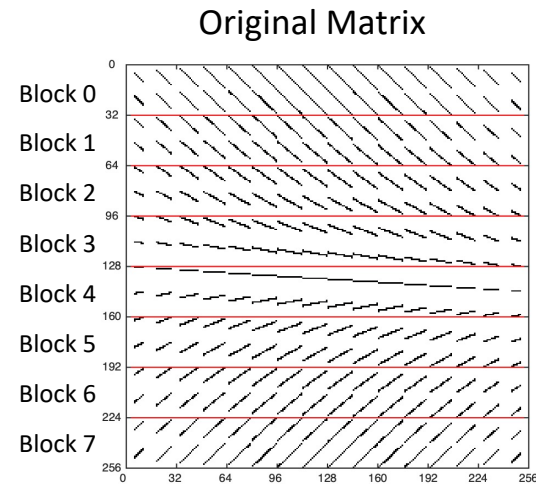
Open Source and Reproducible:

https://github.com/merthidayetoglu/SpDNN_Challenge2020

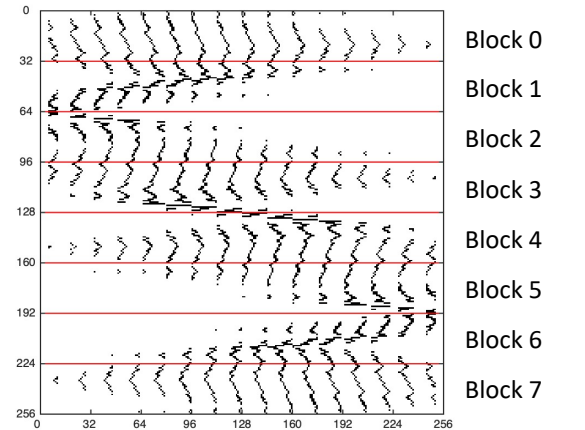
Open Problems: Enhancing Tiled SpMM by Matrix Reordering



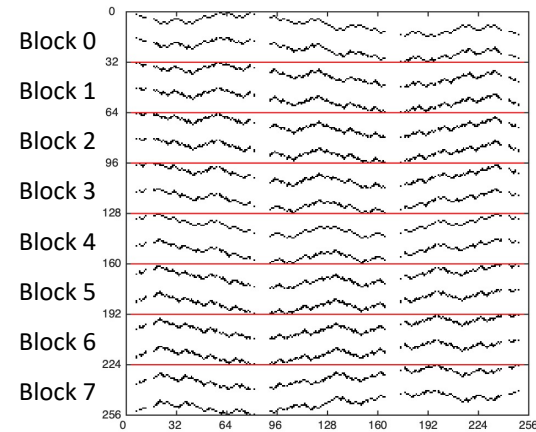
Open Problems: Enhancing Tiled SpMM by Matrix Reordering



Row Reordering



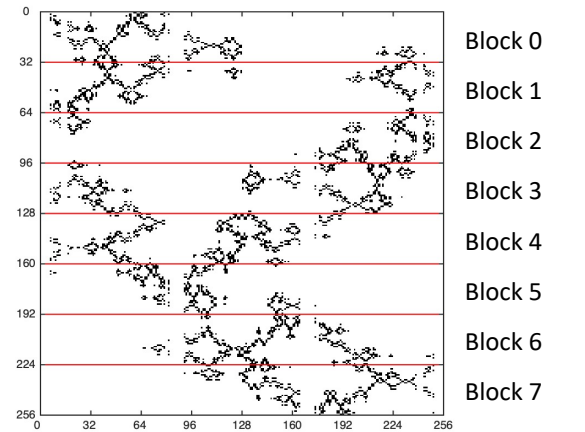
Column Reordering



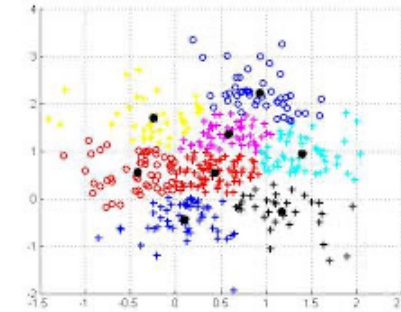
Row Reordering



Column Reordering

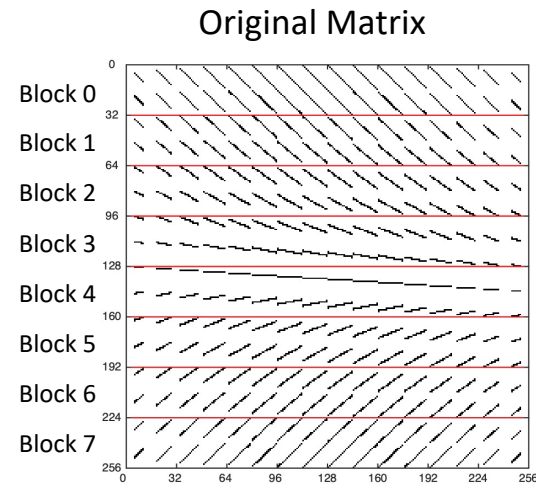


K-Means Clustering

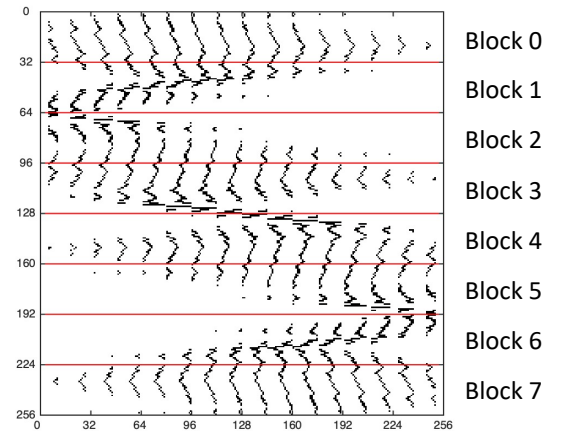


$O(kNM)$

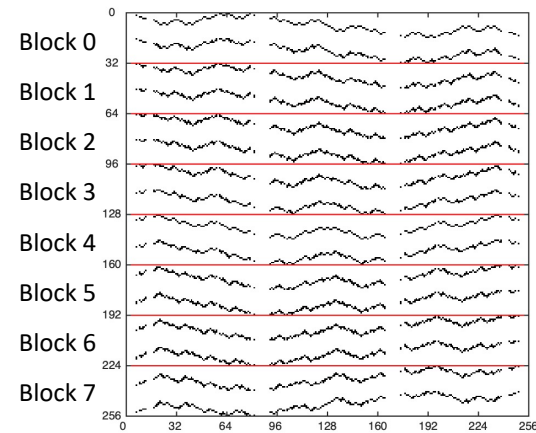
Open Problems: Enhancing Tiled SpMM by Matrix Reordering



Row Reordering



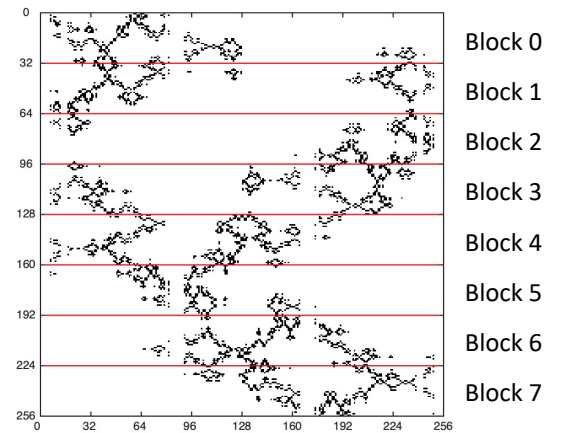
Column Reordering



Row Reordering



Column Reordering



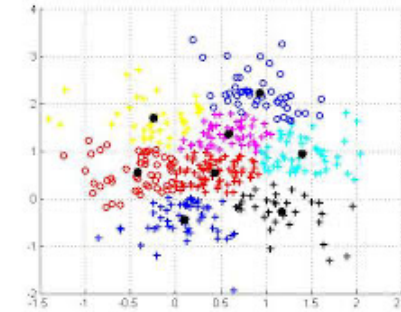
Data Reuse: 2.52

Data Reuse: 4.44

Data Reuse: 2.52

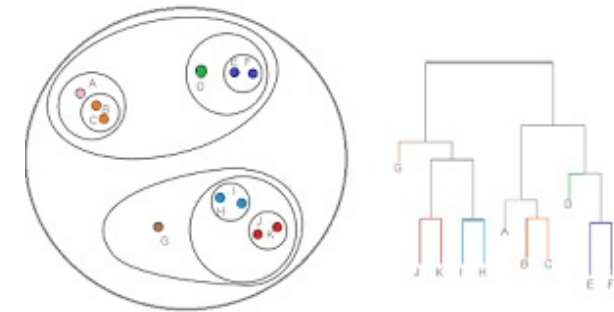
Data Reuse: 4.44

K-Means Clustering

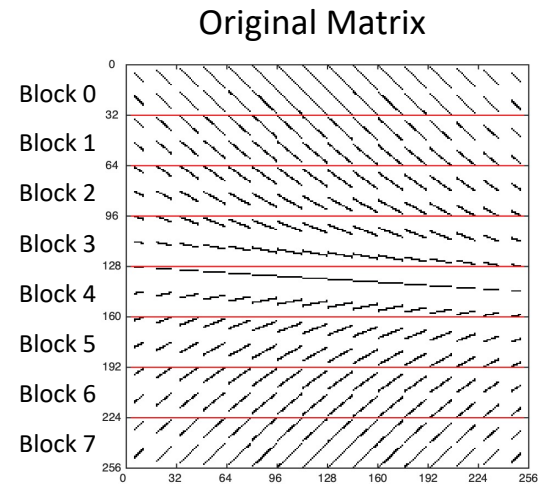


$O(kNM)$

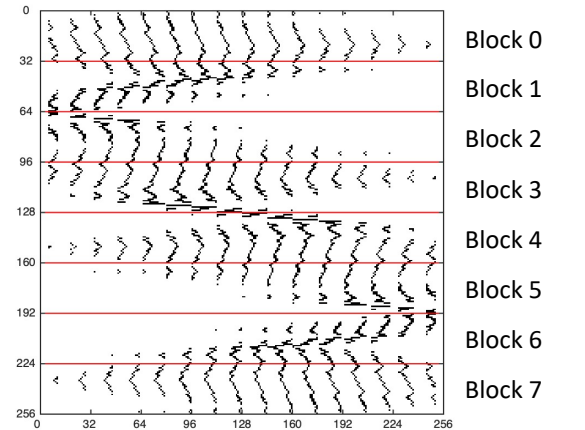
Hierarchical Clustering



Open Problems: Enhancing Tiled SpMM by Matrix Reordering

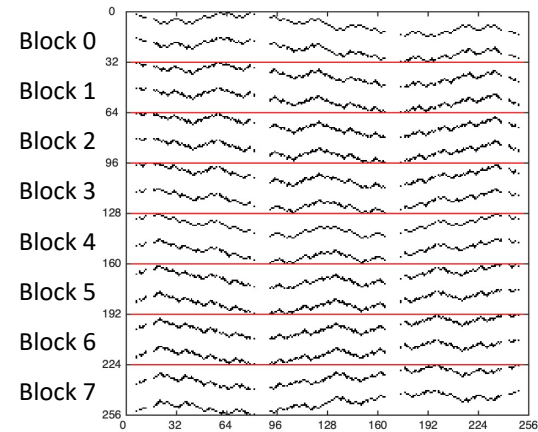


Row Reordering



Data Reuse: 4.44

Column Reordering

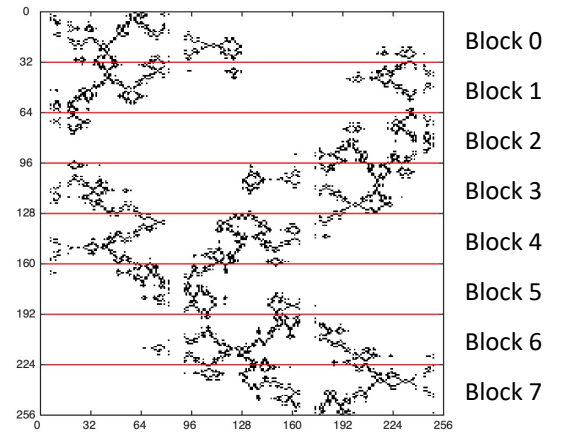


Data Reuse: 2.52

Row Reordering

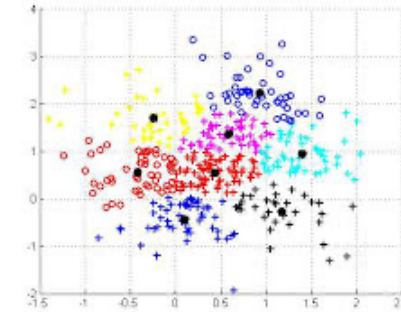


Column Reordering



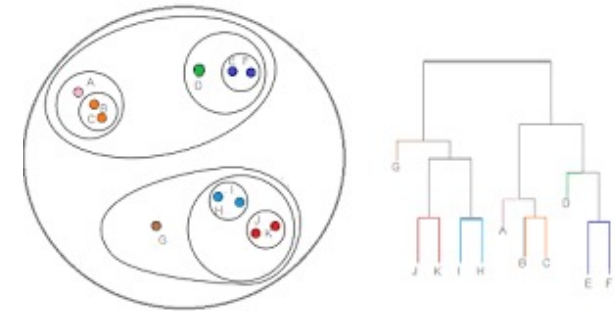
Data Reuse: 4.44

K-Means Clustering

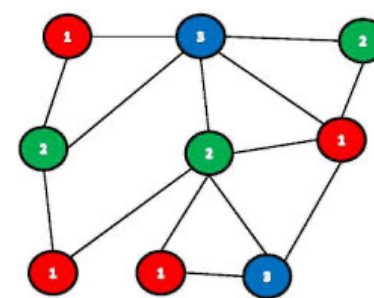


$O(kNM)$

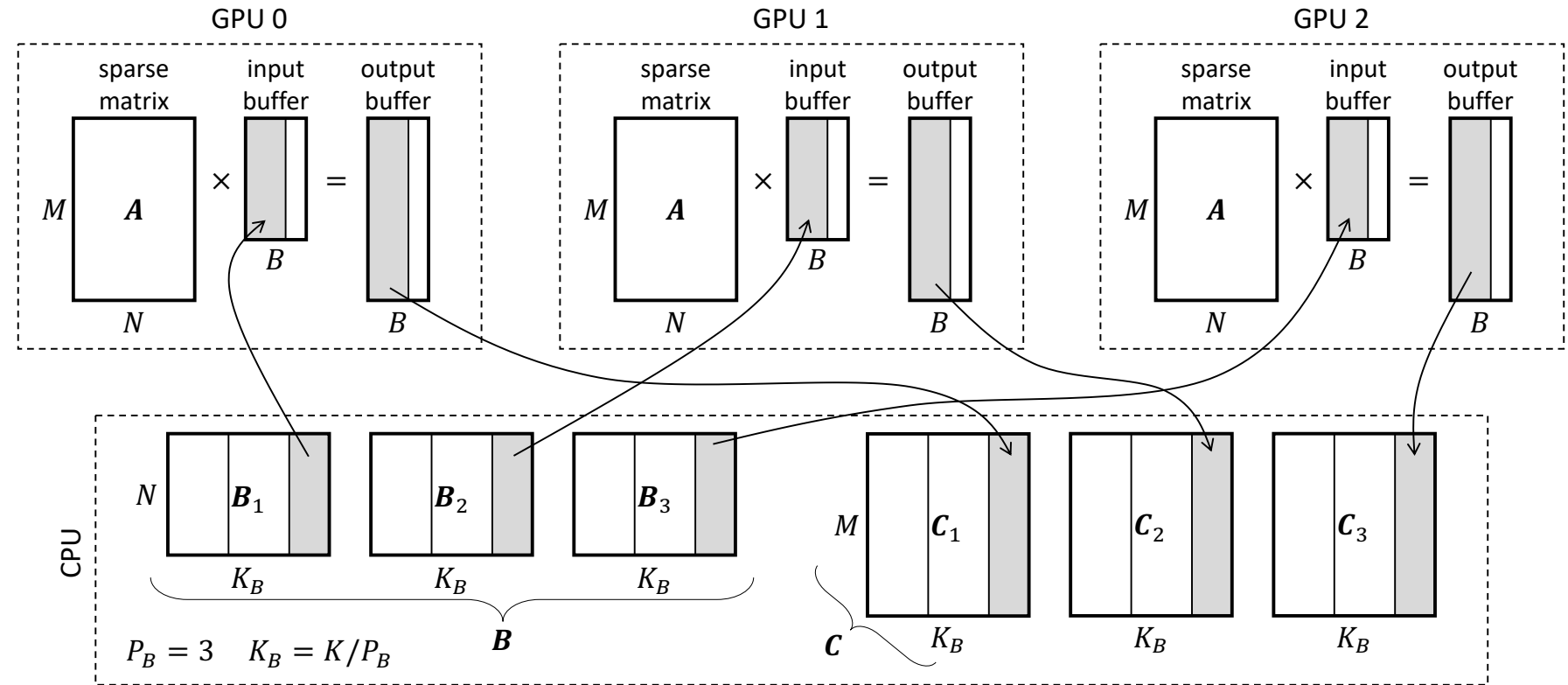
Hierarchical Clustering



Graph Coloring



Partitioning SpMM: Batch Parallelization & Streaming



SpMM: $A \times B = C$

A : $M \times N$ Sparse

B : $N \times K$ Dense (Col.-Major)

C : $M \times K$ Dense (Col.-Major)

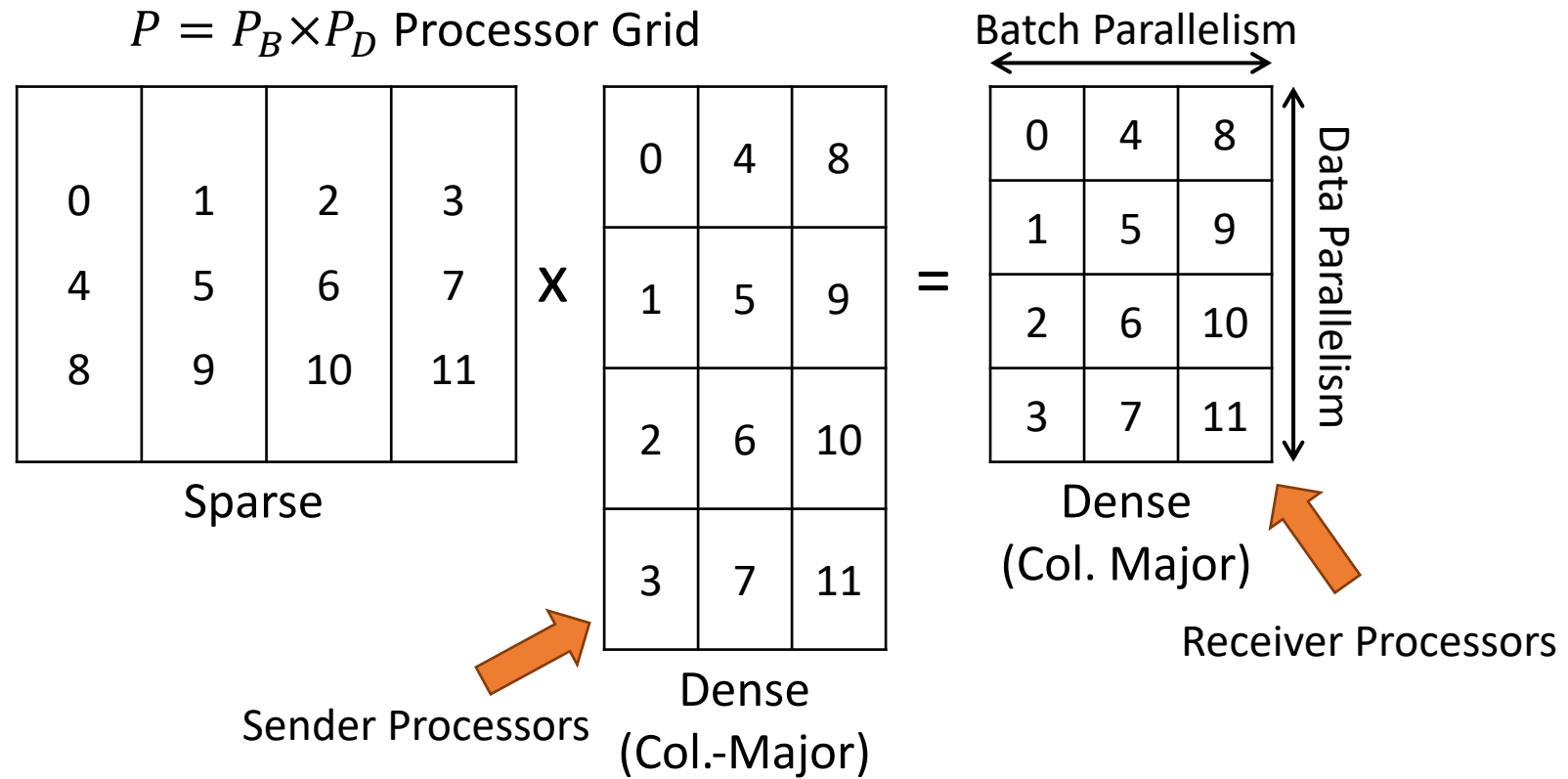
- Batch parallelism duplicates the partitions

Per-process memory —

Total Memory ↑

Communications —

Partitioning SpMM: Data Parallelization



- **Batch parallelism duplicates the partitions**

Per-process memory



Total Memory



Communications



- **Data parallelism partitions the matrix**

Per-process memory



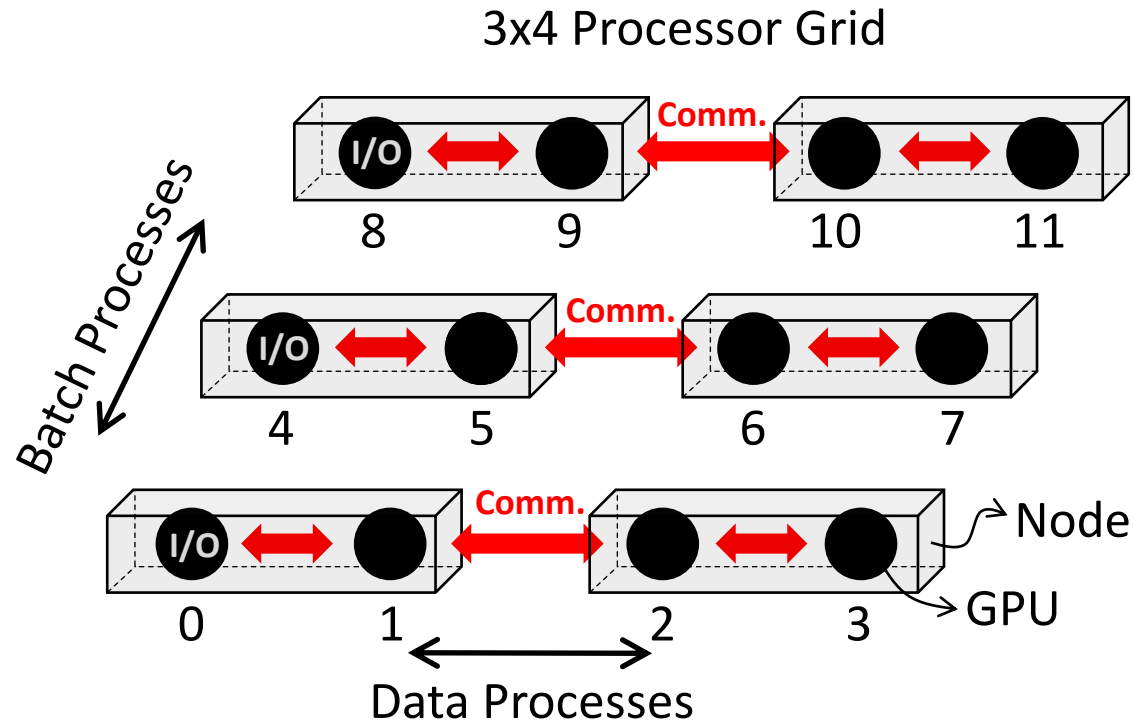
Total Memory



Communications



Partitioning SpMM: Topology-Aware Rank Placement



Defining Orthogonal Communicators

```
MPI_Comm_split( MPI_Comm comm, int
color, int key, MPI_Comm* newcomm)
```

```
MPI_COMM_WORLD
{0, 1, 2, 3, 4, 5,
6, 7, 8, 9, 10, 11}
    MPI_COMM_BATCH
    {0, 4, 8} {2, 6, 10}
    {1, 5, 9} {3, 7, 11}
    {2, 6, 10}
    MPI_COMM_DATA
    {0, 1, 2, 3}
    {4, 5, 6, 7}
    {8, 9, 10, 11}
```

- Batch parallelism duplicates the partitions

Per-process memory —

Total Memory ↑

Communications —

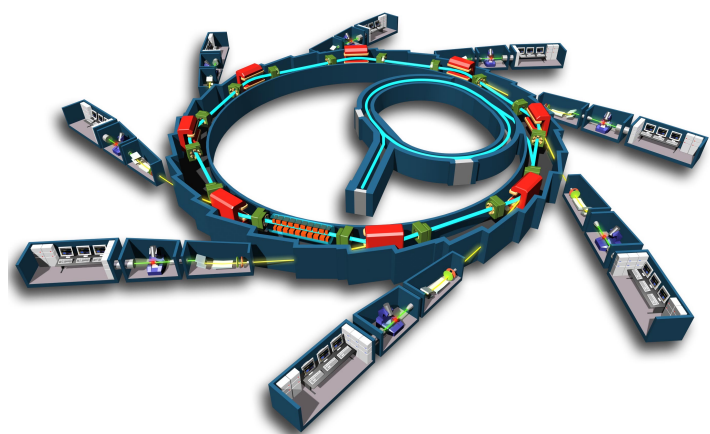
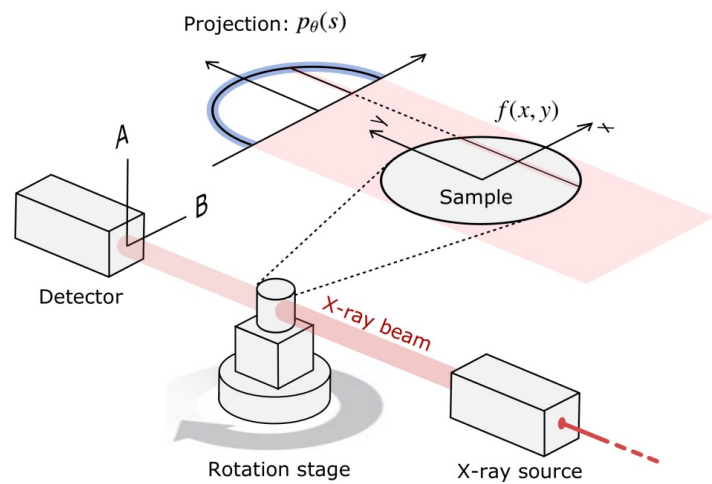
- Data parallelism partitions the matrix

Per-process memory ↓

Total Memory —

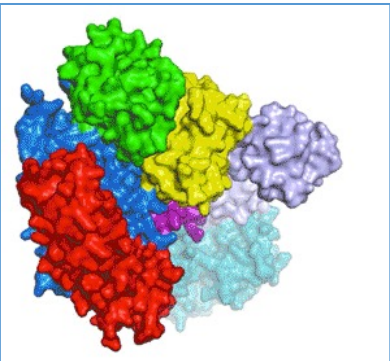
Communications ↑

Application: X-Ray Imaging

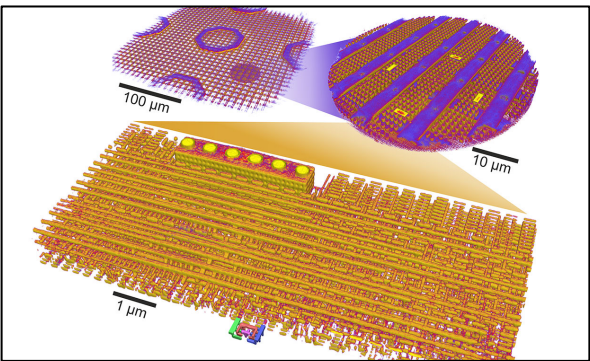


Soleil Light Source Beamlines
Paris, France

Molecular Reactions



Chip Imaging

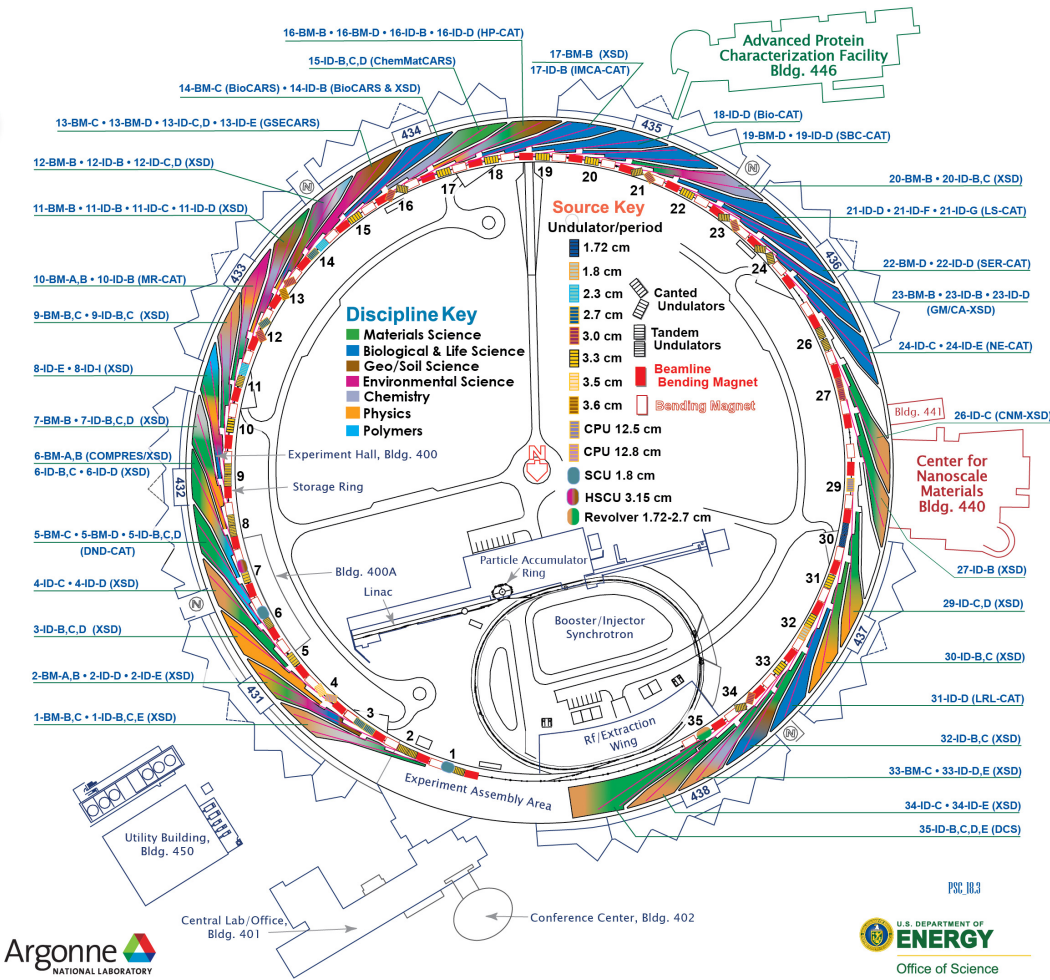


ARGONNE NATIONAL LABORATORY 400-AREA FACILITIES

ADVANCED PHOTON SOURCE
(Beamlines, Disciplines, and Source Configuration)

ADVANCED PROTEIN CHARACTERIZATION FACILITY

CENTER FOR NANOSCALE MATERIALS

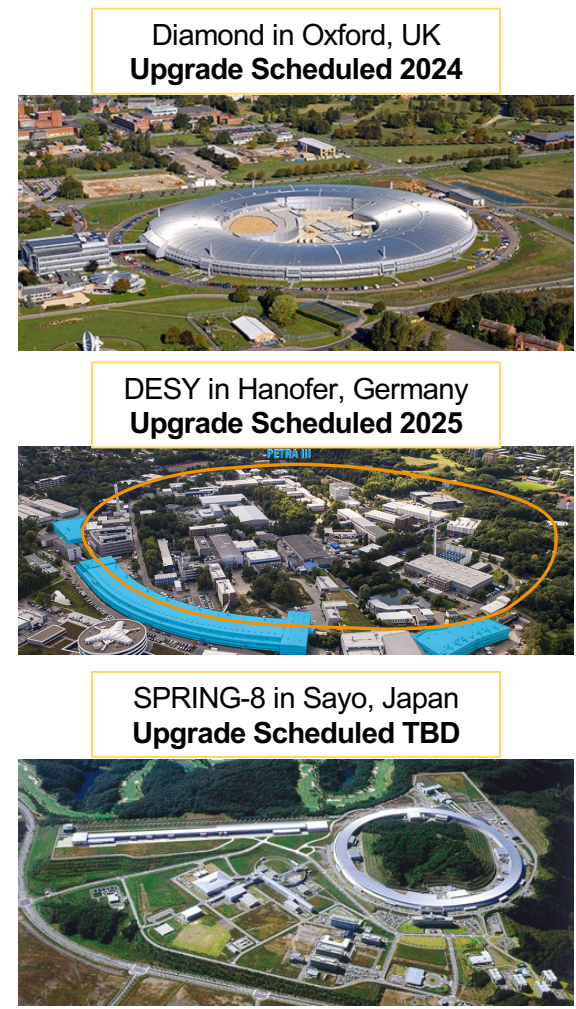
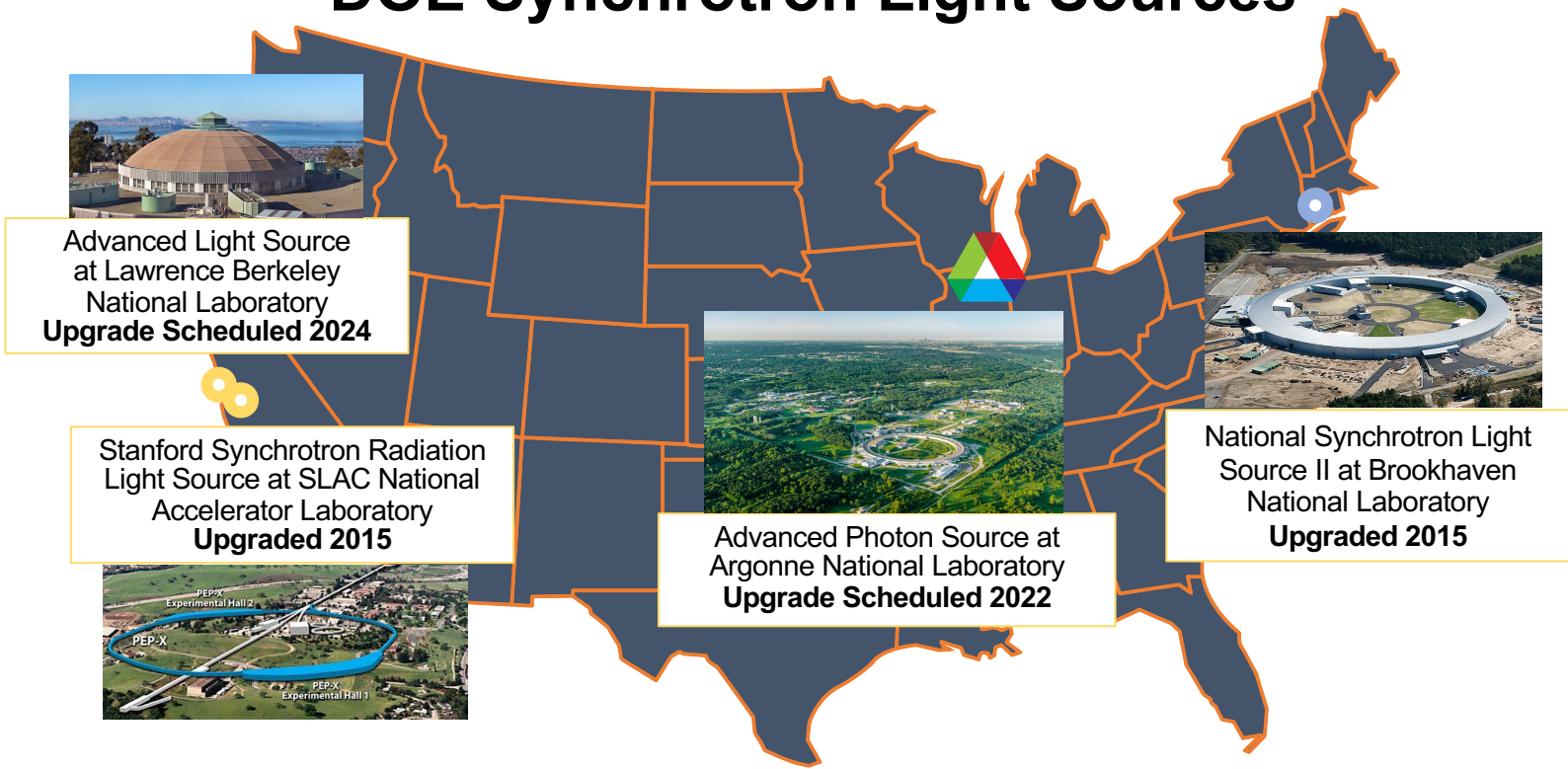


Argonne
NATIONAL LABORATORY

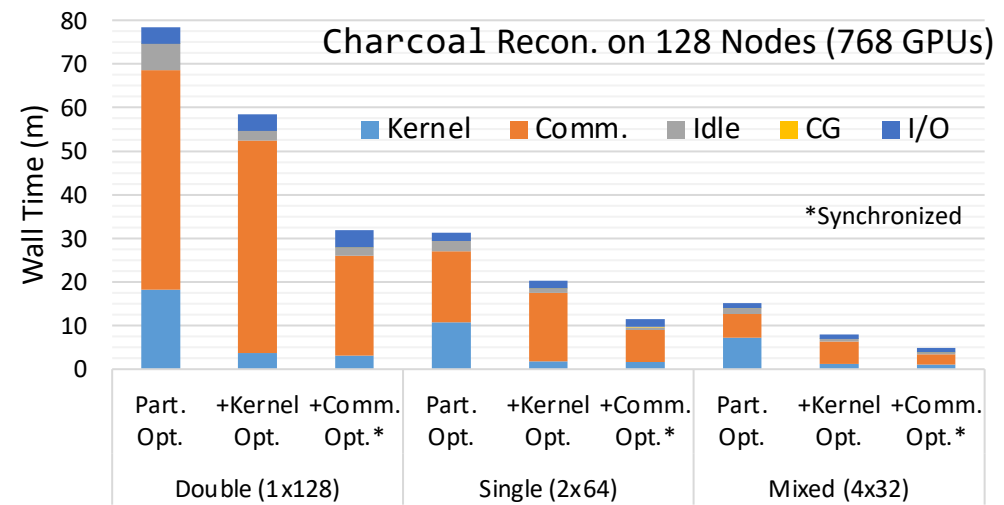
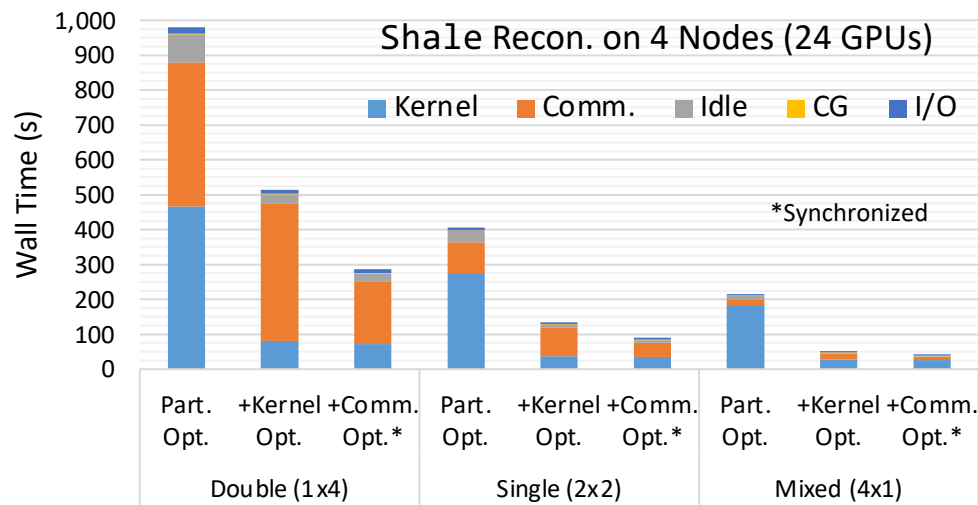
U.S. DEPARTMENT OF
ENERGY
Office of Science

Application Performance: X-Ray Imaging

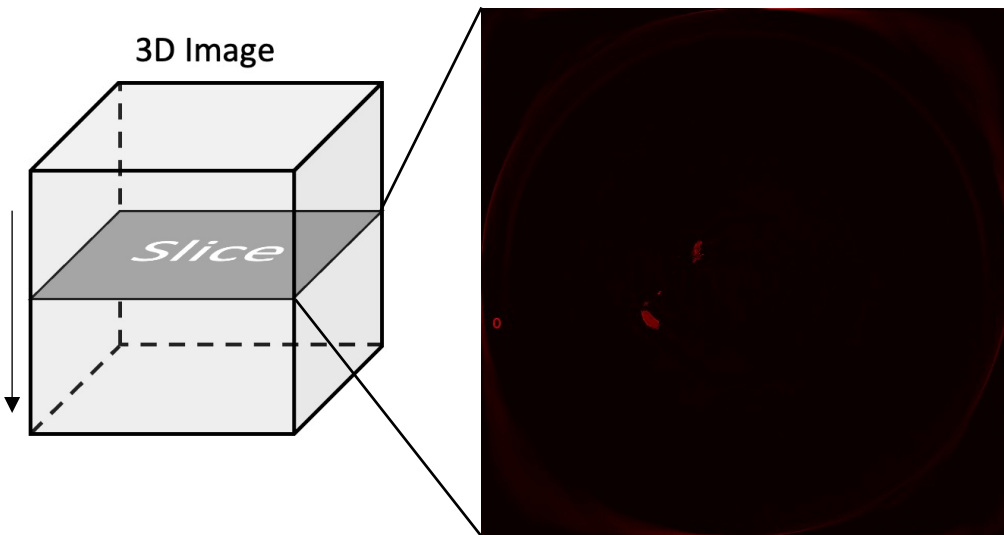
DOE Synchrotron Light Sources



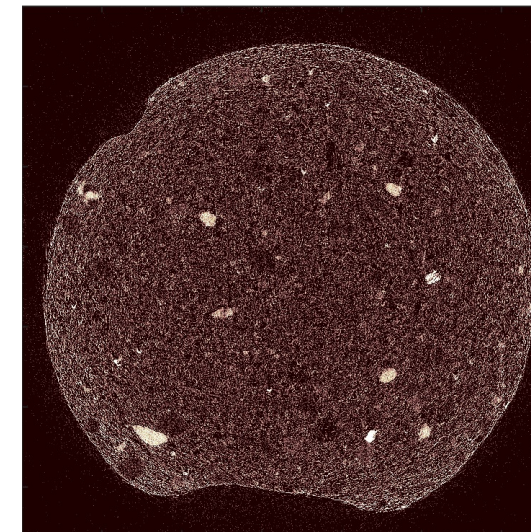
Communication Bottleneck



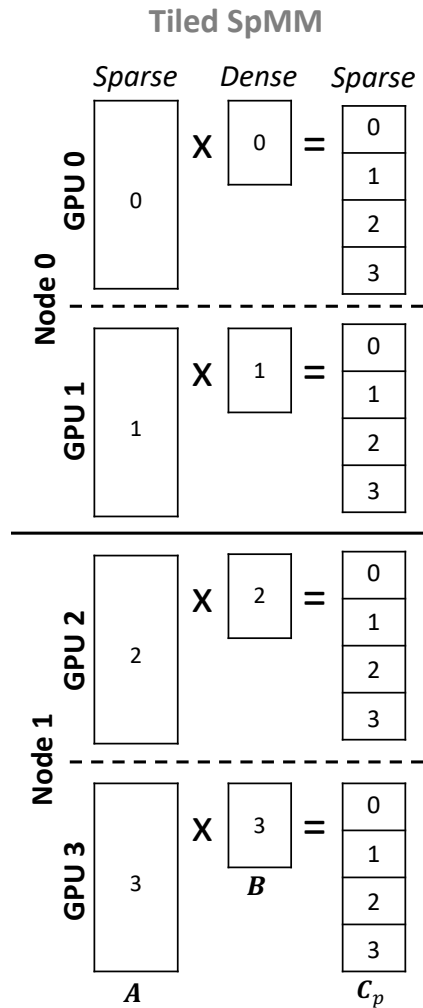
1792 x 2048 x 2048



4198 x 6613 x 6613

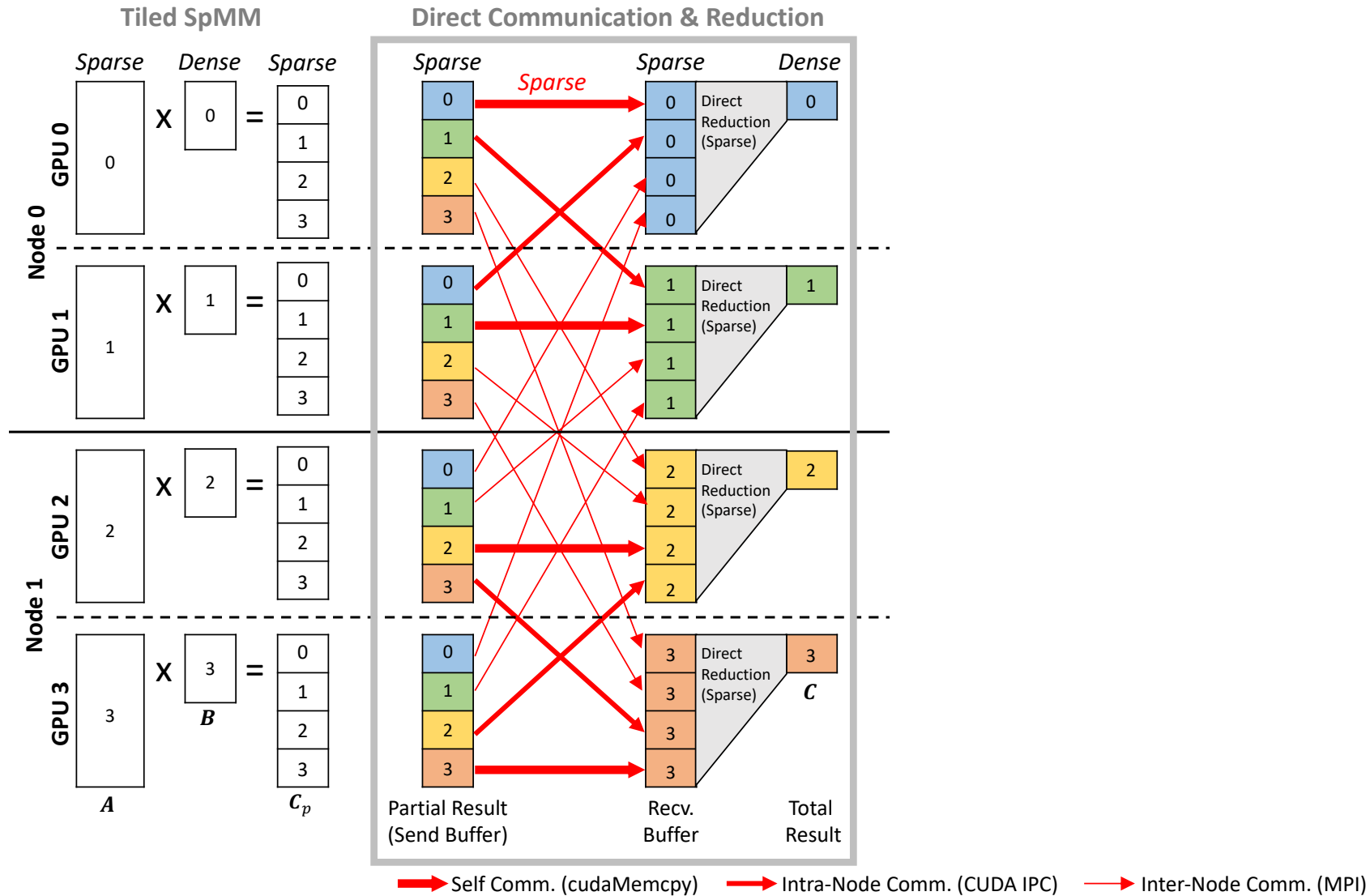


Hierarchical Communications: Overview

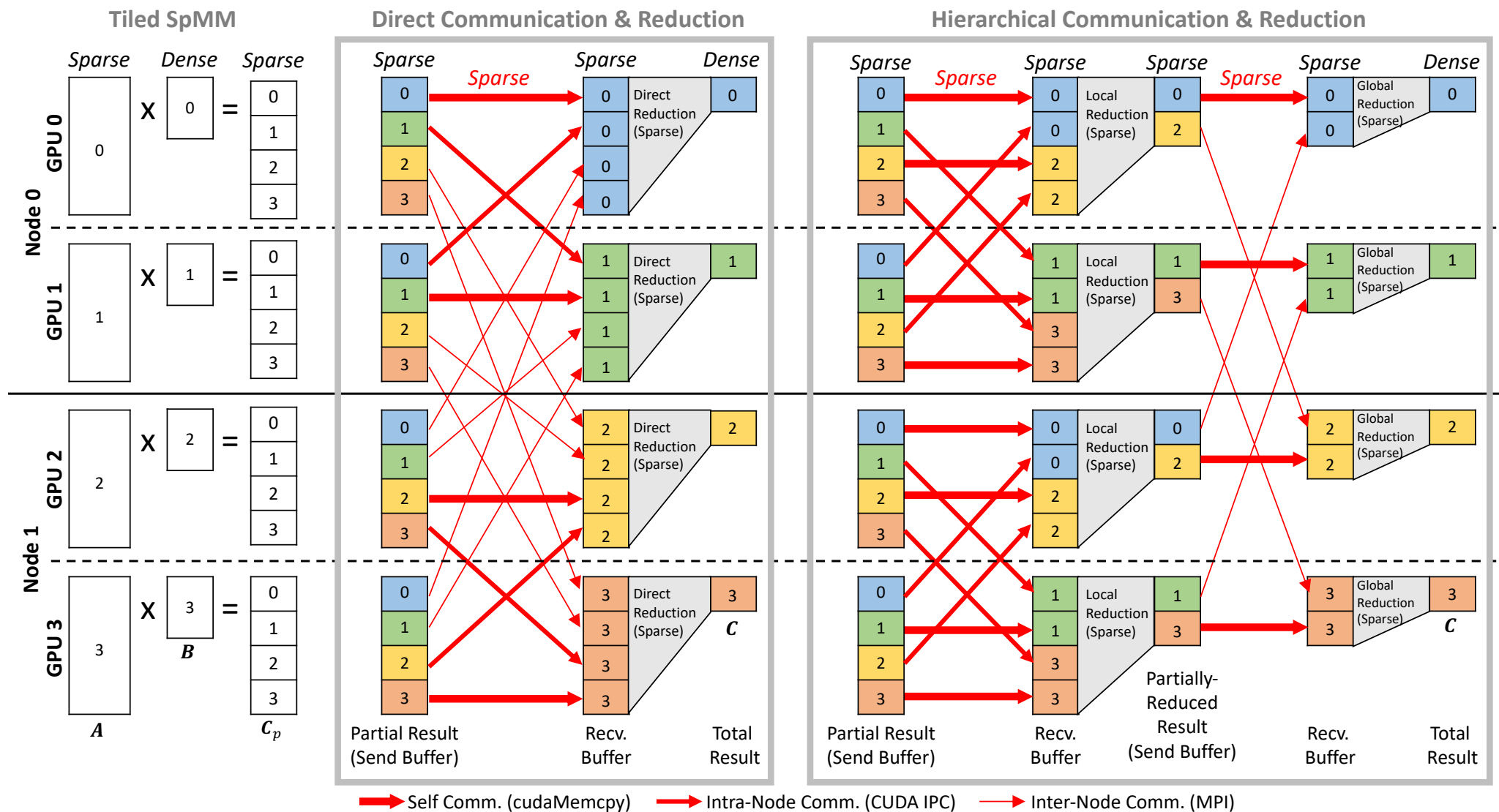


`MPI_Reduce_scatter`
(but sparse)

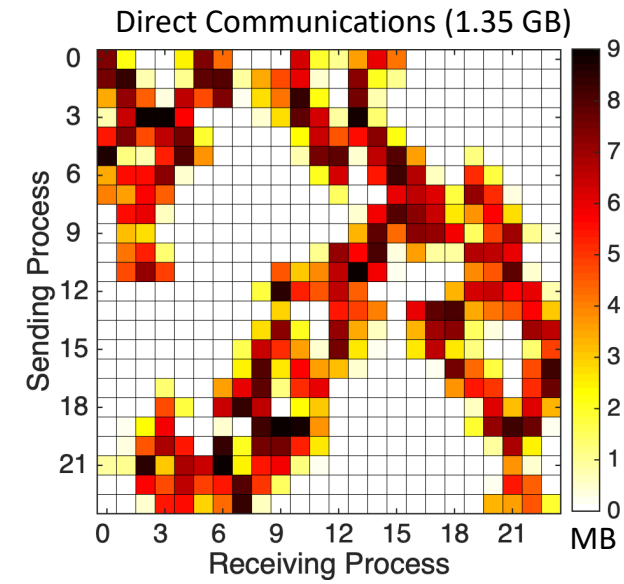
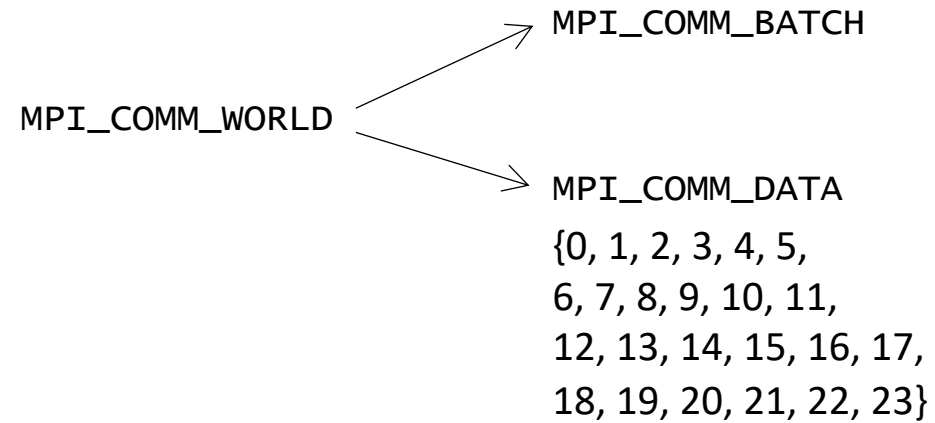
Hierarchical Communications: Overview



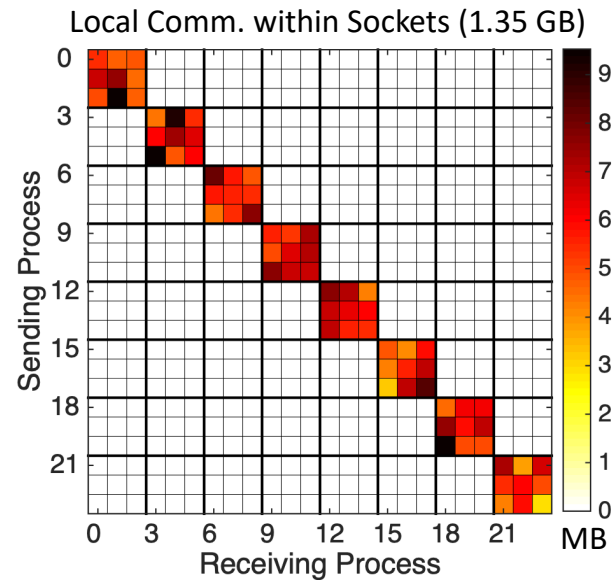
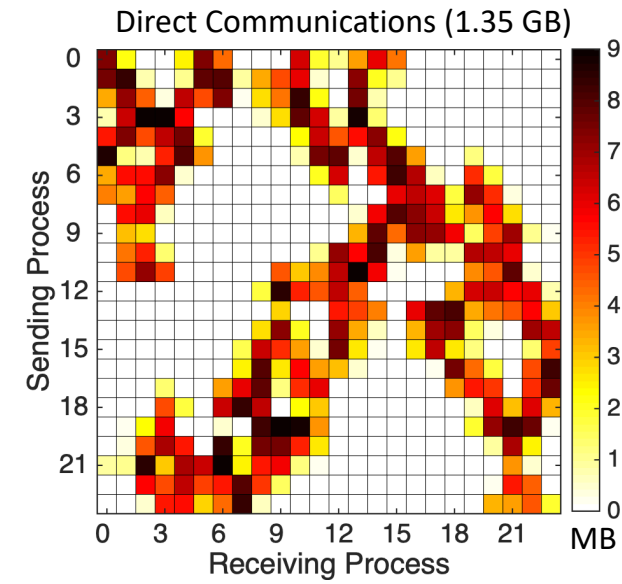
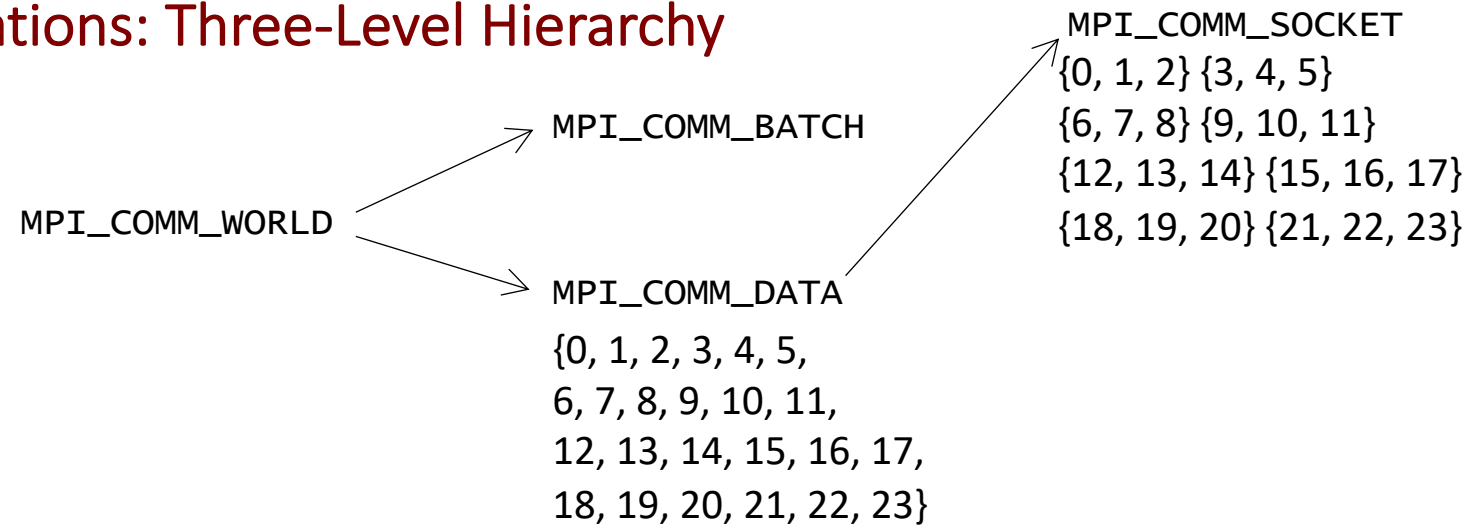
Hierarchical Communications: Overview



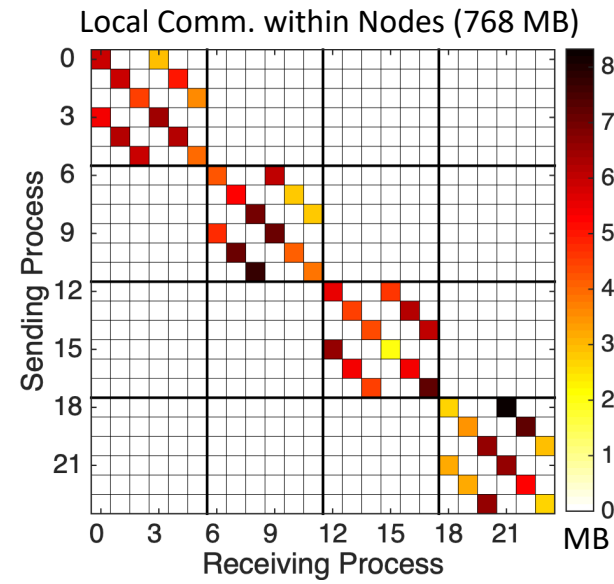
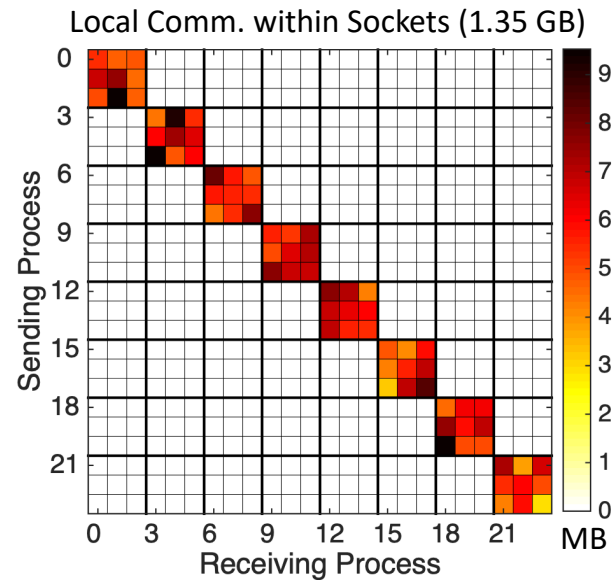
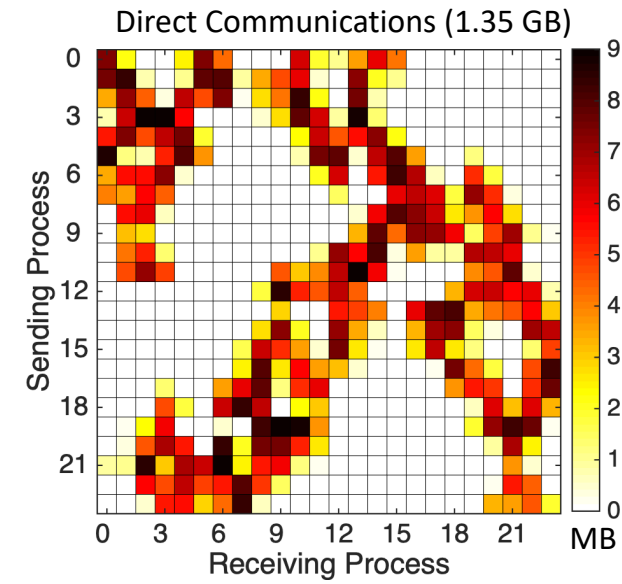
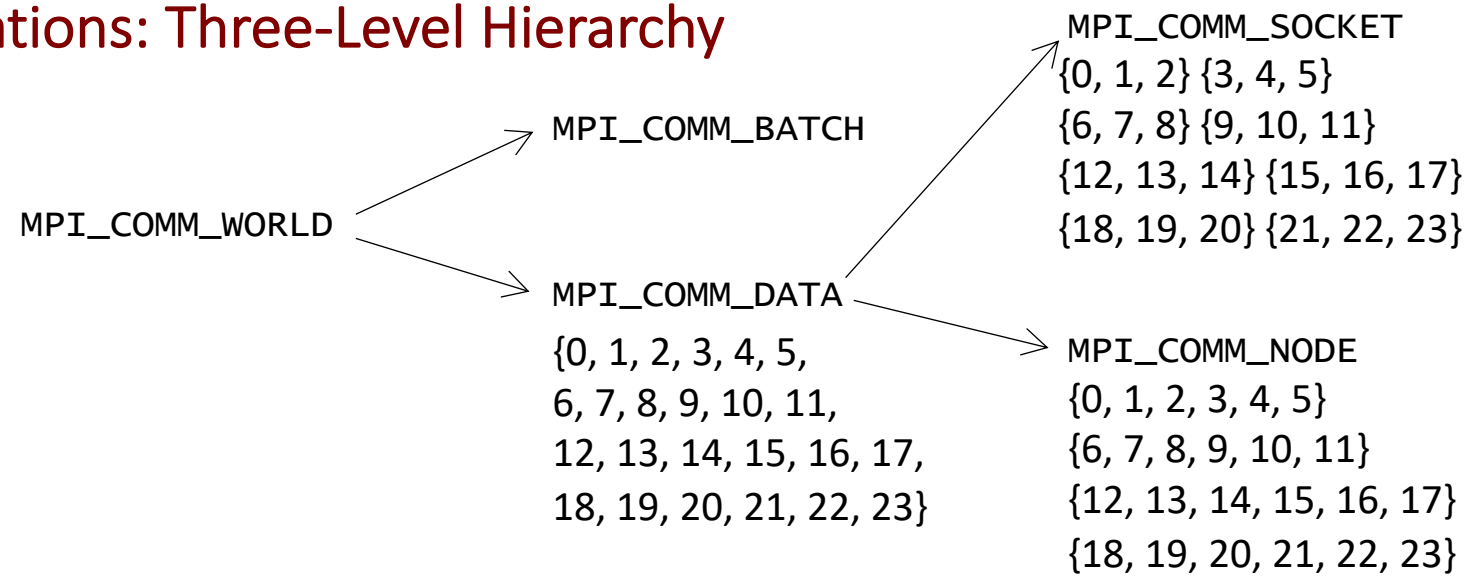
Hierarchical Communications: Three-Level Hierarchy



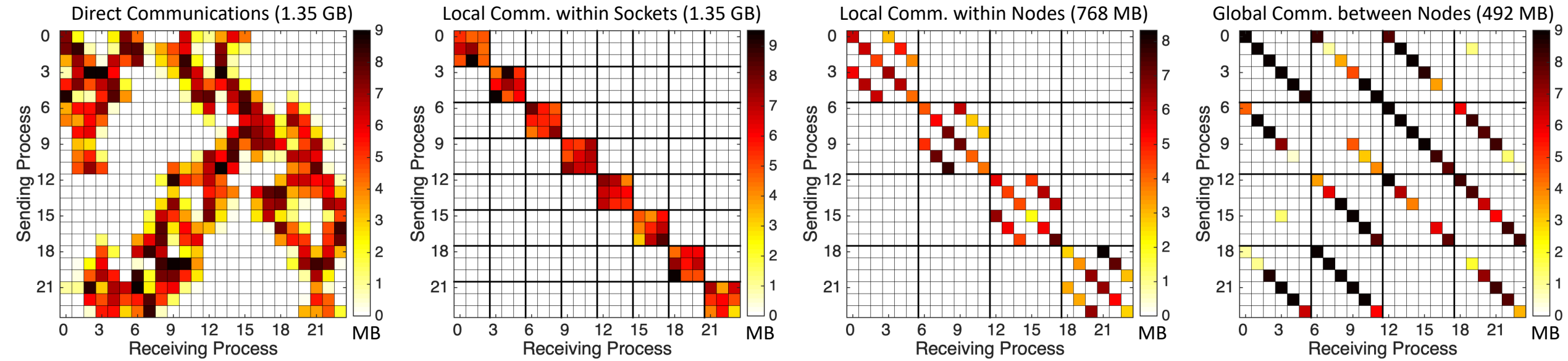
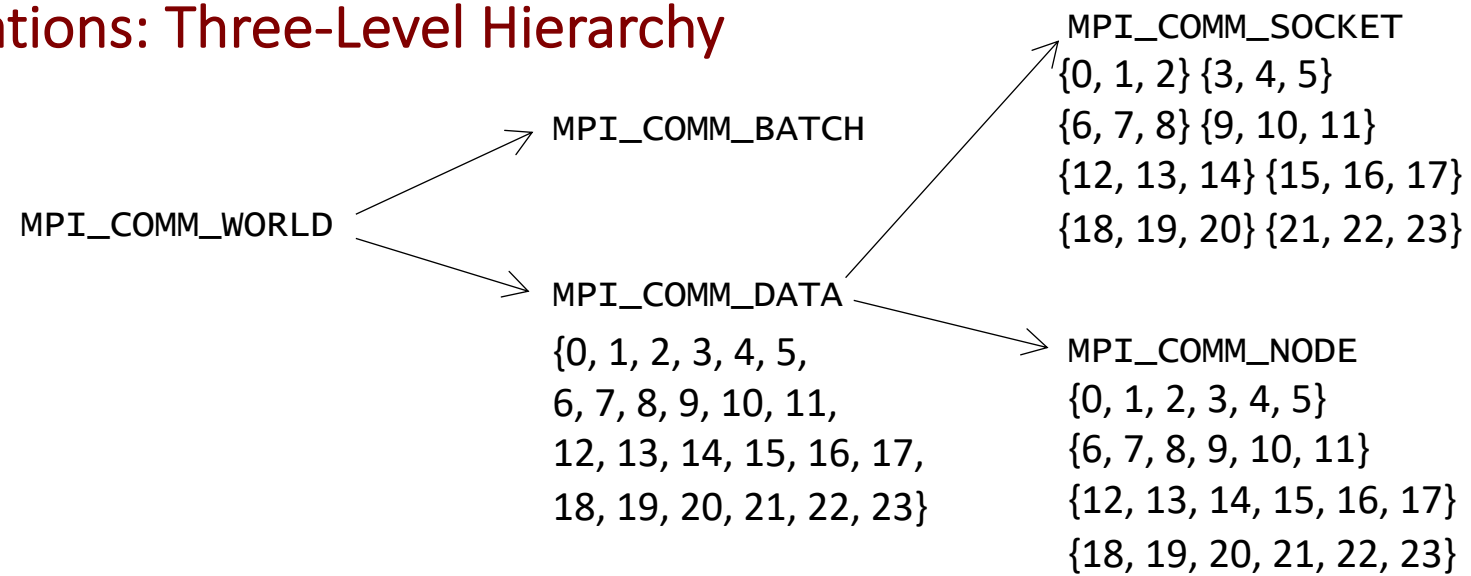
Hierarchical Communications: Three-Level Hierarchy



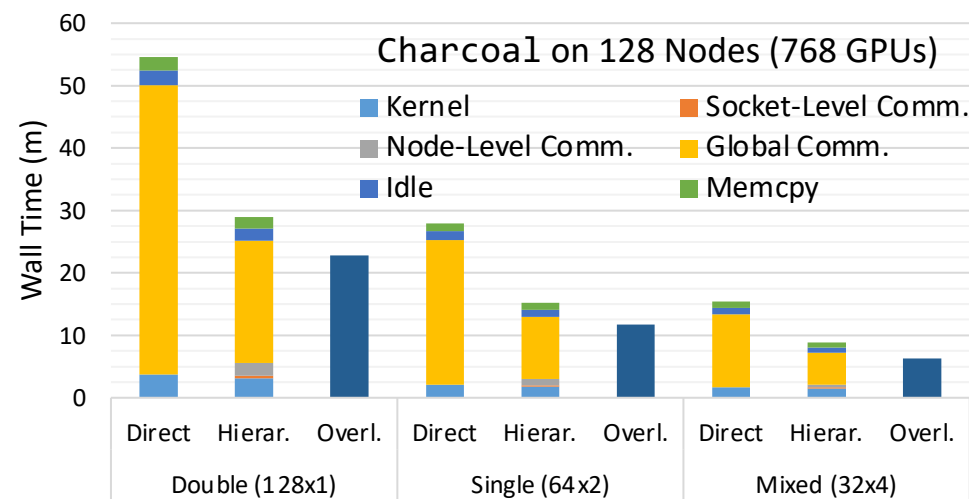
Hierarchical Communications: Three-Level Hierarchy



Hierarchical Communications: Three-Level Hierarchy



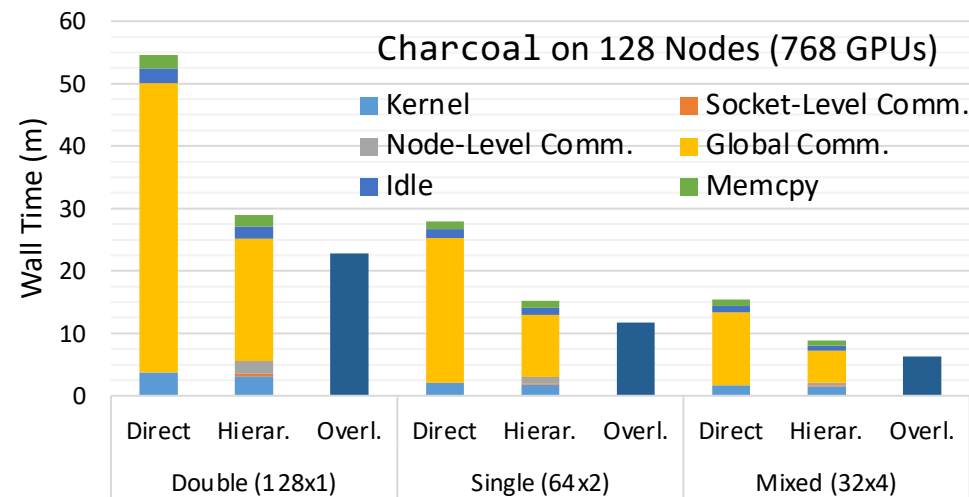
Hierarchical Communications: Benchmarking on Summit



Communication Volume and Effective Bandwidth

	Prec.	Socket-Level Comm.		Node-Level Comm.		Global Comm.		Memcpy B/W
		Data	B/W	Data	B/W	Data	B/W	
Direct	Double	N/A		N/A		36.6 TB	1.61 TB/s	35.2 TB/s
	Single					18.3 TB	1.61 TB/s	34.9 TB/s
	Mixed					9.16 TB	1.59 TB/s	34.6 TB/s
Hierar.	Double	36.6 TB	174 TB/s	21.4 TB	21.3 TB/s	15.2 TB	1.58 TB/s	34.9 TB/s
	Single	18.3 TB	170 TB/s	10.7 TB	22.8 TB/s	7.58 TB	1.55 TB/s	34.5 TB/s
	Mixed	9.16 TB	164 TB/s	5.35 TB	23.5 TB/s	3.79 TB	1.49 TB/s	33.6 TB/s

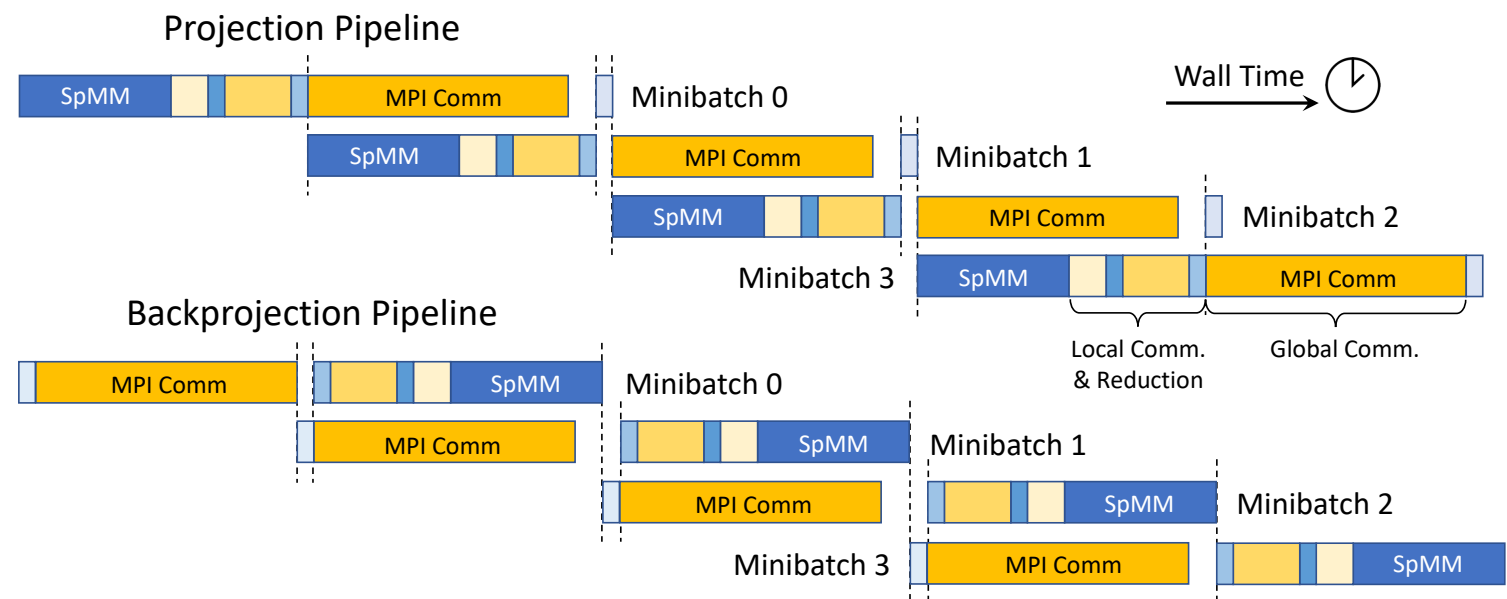
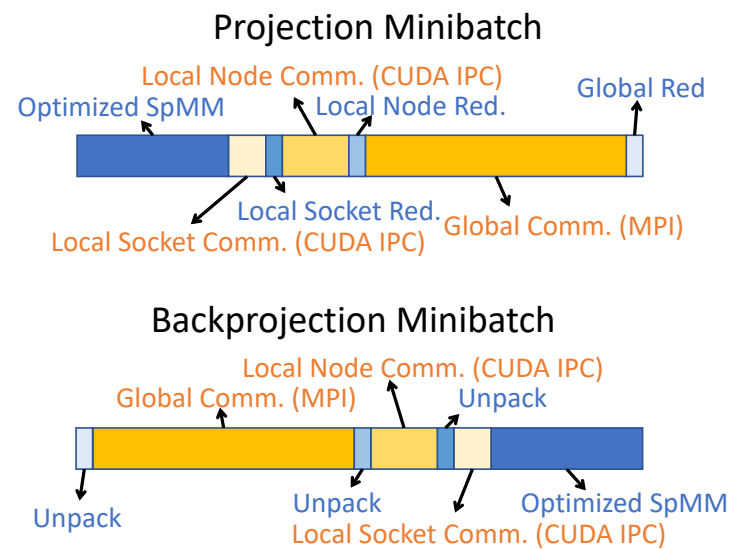
Hierarchical Communications: Benchmarking on Summit



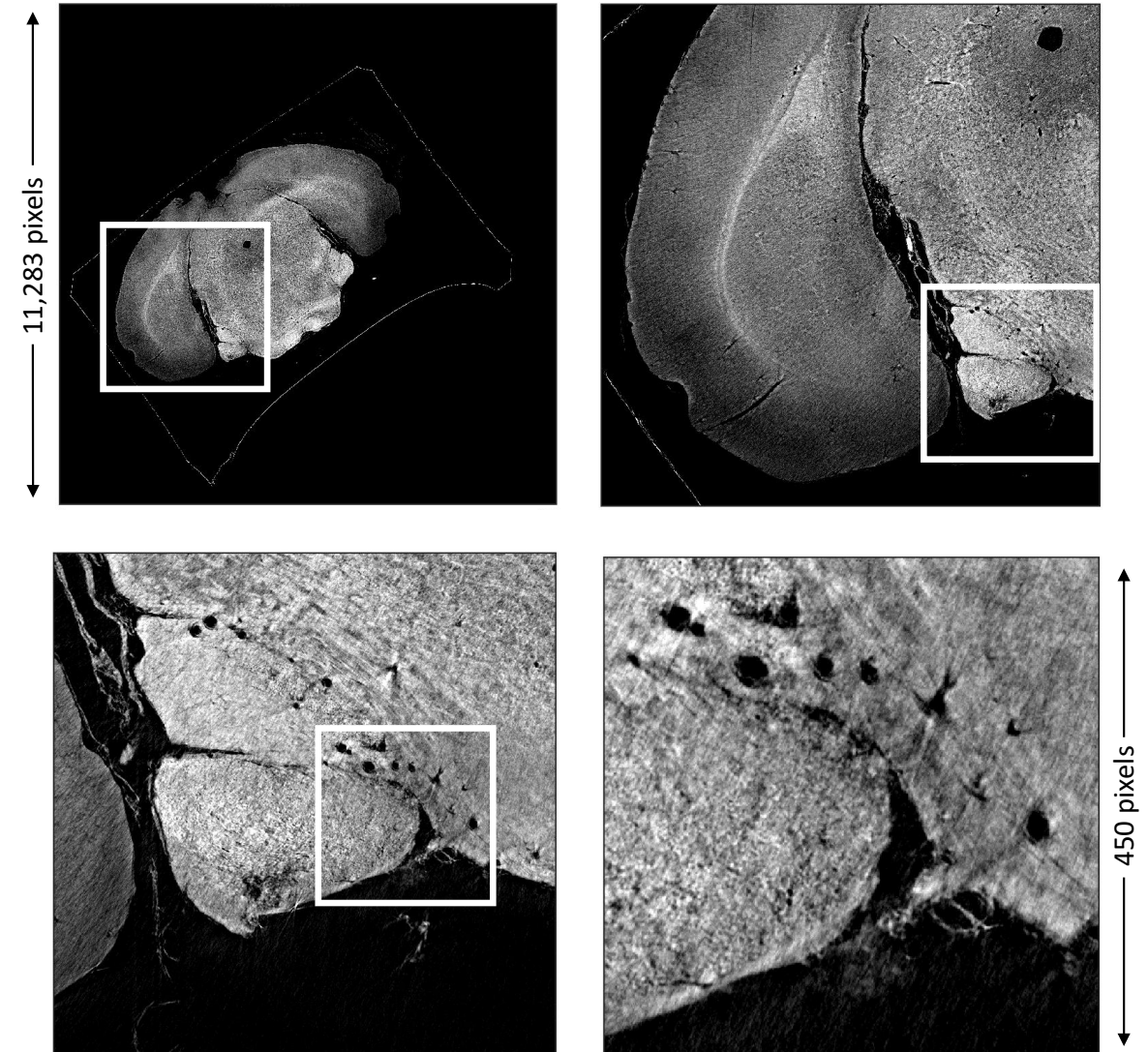
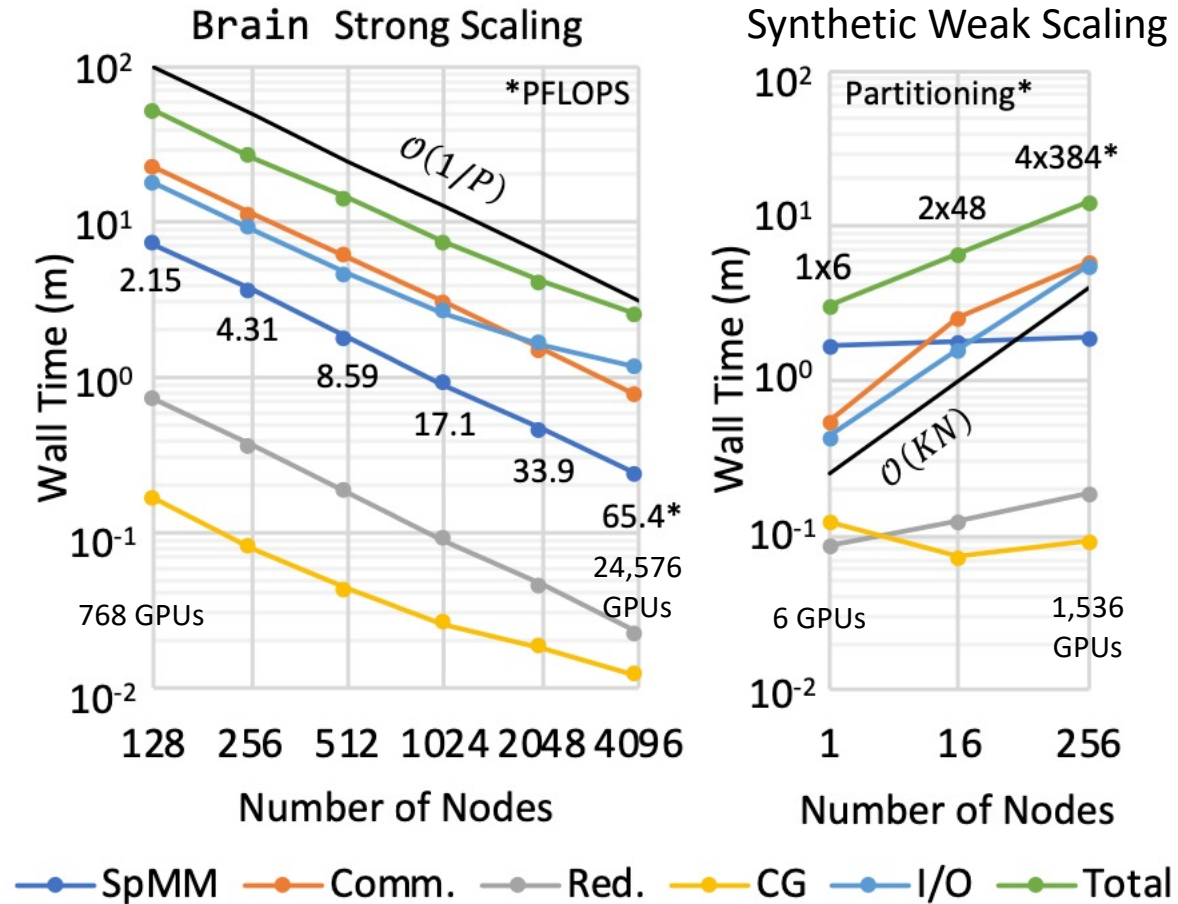
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Pipelining Batch Processing



Hierarchical Communications: Scaling on Summit



We thank Bobby Kasthuri of UChicago/Argonne, Rafael Vescovi and Ming Du of Argonne for sharing the mouse brain dataset.

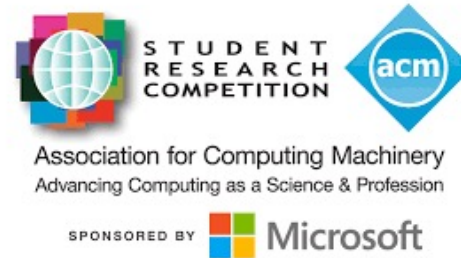
Recognition: Best Paper @ SC20

SC20 Student Cluster Reproducibility Committee Chooses Benchmark Wisely

April 15, 2020

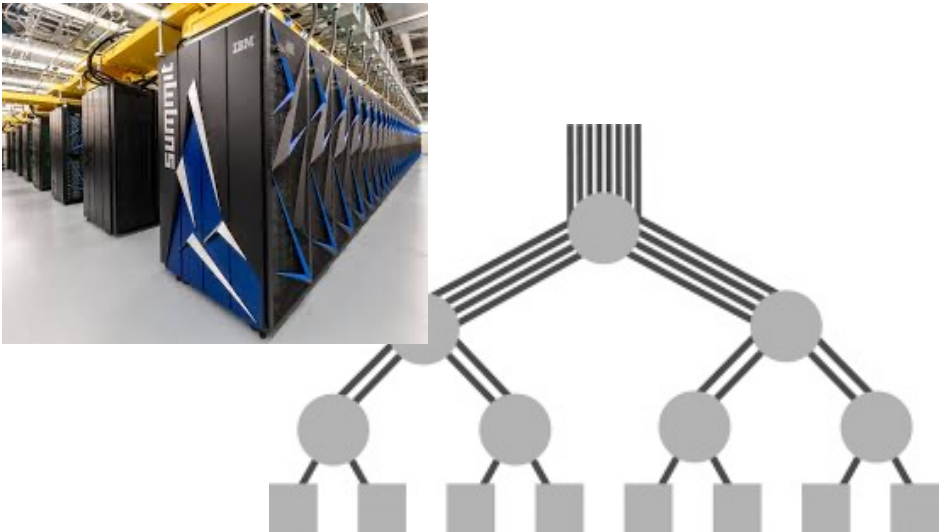
<https://github.com/merthidayetoglu/MemXCT-GPU>

We are excited to announce that the SC20 Reproducibility Committee has selected the SC19 paper "MemXCT: Memory-Centric X-ray CT Reconstruction with Massive Parallelization", by Mert Hidayetoğlu, Tekin Biçer, Simon Garcia de Gonzalo, Bin Ren, Doğa Gürsoy, Rajkumar Kettimuthu, Ian T. Foster, and Wen-mei W. Hwu, to serve as the Student Cluster Competition (SCC) benchmark for the Reproducibility Challenge this year. A team of reviewers selected the paper from 45 finalists, based on the paper's Artifact Descriptor (AD) and its suitability to the SCC. The authors and the Reproducibility Committee have been working to create a reproducible benchmark that builds on the paper's results. At SC20, the sixteen SCC teams will be asked to run the benchmark, replicating the findings from the original paper under different settings and with different datasets.



Open Problems: Extending Comm. Hierarchy for Inter-Node Communication

Fat-Tree: OLCF Summit



Tofu: RIKEN Fugaku

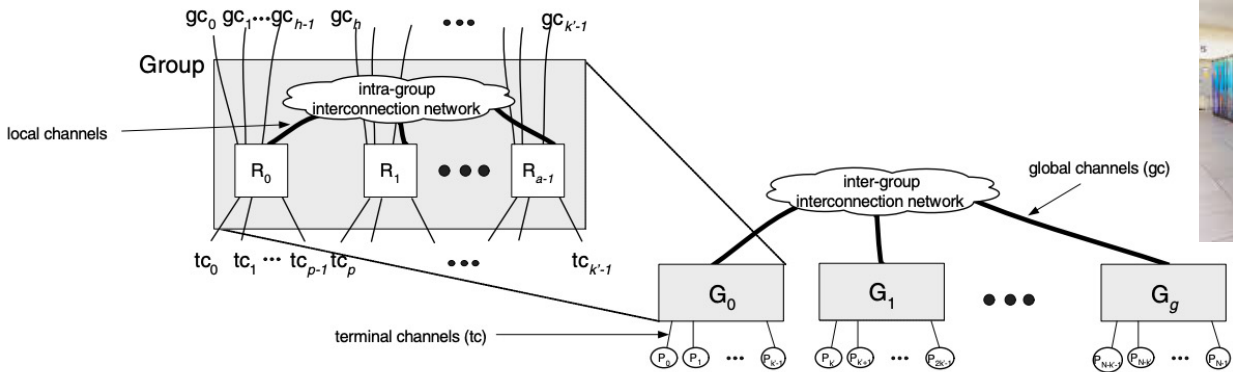
6D Mesh/Torus Network

- Six coordinate axes: X, Y, Z, A, B, C
 - X, Y, Z: the size varies according to the system configuration
 - A, B, C: the size is fixed to $2 \times 3 \times 2$
- Tofu stands for "torus fusion": $(X, Y, Z) \times (A, B, C)$

The diagram shows a 3D representation of the 6D mesh network. It features a central cube with axes X, Y, and Z. Surrounding this are additional dimensions A, B, and C, represented by colored spheres and arrows. The overall structure is a complex, multi-layered mesh.

The photograph shows the RIKEN Fugaku supercomputer racks, which are densely packed and feature a distinctive blue and white color scheme.

Dragonfly: ALCF Theta



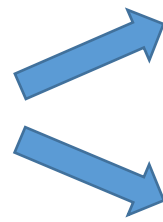
Conclusions

Large-Scale Sparse Applications

Conclusions

Large-Scale Sparse Applications

Multi-GPU Node Architecture



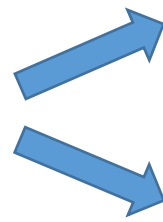
Single GPU: Tiled SpMM

GPU Cluster: Hierarchical Comm.

Conclusions

Large-Scale Sparse Applications

Multi-GPU Node Architecture



Single GPU: Tiled SpMM

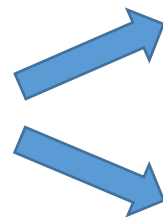
GPU Cluster: Hierarchical Comm.

Possible Contributions: cuSPARSE, MPI Collectives, NCCL

Conclusions

Large-Scale Sparse Applications

Multi-GPU Node Architecture



Single GPU: Tiled SpMM

GPU Cluster: Hierarchical Comm.

Possible Contributions: cuSPARSE, MPI Collectives, NCCL

Further Dissertation Research

